

1                   **A Dual Concentric Ring Test for Evaluating Residual Stress Development**  
2                                   **Due to Restrained Volume Change**

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5  
6                   **Abstract**

7                   A new test is being developed to evaluate the performance of concretes undergoing both  
8                   expansion and shrinkage during hydration and/or temperature changes under mechanically  
9                   restrained conditions. The standard restrained ring test (ASTM 1581-09) is a simple,  
10                  economical method to evaluate a concrete mixture's susceptibility to develop shrinkage cracking  
11                  when it is restrained. Unfortunately, the test only provides restraint against samples that shrink  
12                  and cannot be used to characterize materials undergoing expansion. Further, the conventional  
13                  restrained ring test does not apply in cases in which the concrete undergoes large variations in  
14                  temperature, since the restraint changes dimension under heating and cooling. This paper  
15                  describes a test that was designed to overcome both of these limitations. The new dual  
16                  concentric ring test provides restraint for both shrinkage and expansion, and has incorporated  
17                  the ability to study thermal stresses by using a restraining ring having a very low thermal  
18                  expansion coefficient. This paper will discuss the design and construction of the test device and  
19                  will present preliminary data that characterizes its ability to quantify and evaluate restrained  
20                  expansive, shrinkage, and thermal stresses.

21  
22                  Keywords: Restrained Ring Test, Dual Ring Test, Concrete, Thermal Cracking, Shrinkage,  
23                  Expansion, Internal curing, Autogenous Shrinkage

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39 **1.0 Introduction**

40 Cementitious materials undergo volume change at early ages due to chemical reactions, self  
41 desiccation, external drying, and thermal changes [1-9]. Residual stress develops in the  
42 cementitious material when this volume change is restrained [9-12]. If the residual tensile stress  
43 becomes too large, cracking may occur. This cracking is significant as it inhibits otherwise  
44 durable concrete from reaching its potential service life by allowing deleterious materials to  
45 enter the cracks, thereby accelerating degradation [13, 14]. .

46 The concerns associated with early-age cracking have spurred the development of many tests  
47 to assess a material's cracking potential. Tests based on uniaxial restraint such as cracking  
48 frames and temperature-stress testing machines have been implemented by Kovler [15],  
49 Springenschmid [16], Lange [17], Marchand [18], and van Breugel [19]. Another common  
50 method that has been used to quantify a mixture's performance is the restrained ring method  
51 [20]. This approach has been used for nearly a century, and recently the restrained ring test  
52 (ASTM C 1581-04) [21] has been standardized as a procedure to assess the shrinkage cracking  
53 potential of cementitious mixtures. This test is performed by casting an annulus of a  
54 cementitious mixture (paste, mortar, or concrete) around a steel ring. Residual tensile stress is  
55 generated in the sample when it attempts to shrink but is restrained by the inner steel ring. A  
56 crack results if the residual stress exceeds the developing tensile strength. This is observed to  
57 correspond with a sudden drop in the measured strain. Stresses and cracking time in the  
58 sample are determined by instrumenting the ring with strain gauges.

59 The vast majority of concrete used in the field is restrained; however, the extent to which this  
60 restraint occurs varies. Slabs-on-grade are restrained by the subgrade, concrete bridge decks  
61 are restrained by beams, girders, or abutments and elevated composite slabs are restrained by  
62 the structural steel supporting girders. One question when developing a restrained shrinkage  
63 test is the level of restraint that should be provided to limit the movement of the concrete. The  
64 amount of restraint provided is commonly quantified using a term called the degree of restraint  
65 (DOR). The DOR describes the percentage of concrete shrinkage or expansion deformation  
66 that is prevented by the restraining elements. When all the deformation of a member is  
67 prevented it can be considered to be 100% restrained (i.e., a degree of restraint of 1). Free  
68 shrinkage corresponds to a 0% degree of restraint. Partial restraint occurs when the DOR is  
69 between 100% and 0%. This partial restraint can be calculated using the geometry and  
70 stiffness of the concrete and the restraining element [22, 23].

71

72 **2.0 Research Significance**

73 The conventional restrained ring test has been widely used to evaluate the restrained shrinkage  
74 cracking potential of concrete mixtures but is limited in two significant ways. First, the test can  
75 only measure net shrinkage due to its configuration where expanding samples come out of  
76 contact with the restraining ring. This limitation becomes significant when studying expansive  
77 cements [24], shrinkage reducing admixtures [25], and internal curing [26] as these technologies  
78 may result in early age expansion. The second limitation of the restrained ring test is that it

79 must operate at a constant temperature since the ASTM A53 Grade B steel pipe that is typically  
80 used for the restraining rings will expand or contract if the temperature changes. As a result, a  
81 temperature change would alter the level of restraint experienced by the cementitious annulus.

82 This paper proposes a test method that can evaluate materials that may expand and that can  
83 operate while varying temperature. This test, called the dual concentric ring test, uses two  
84 concentric restraining rings; one on the outside of the sample and one on the inside of the  
85 sample. This enables restraint in both expansion and contraction and measurement of the  
86 strain in the restraining elements as samples shrink and expand. The rings are constructed  
87 from Invar, a metal with an extremely low coefficient of thermal expansion that allows the  
88 temperature to be varied without dramatically altering the degree of restraint. This enables the  
89 study of thermally induced volume changes in addition to volume change from autogenous  
90 shrinkage. A wide variety of temperature profiles can be selected to simulate most field  
91 conditions. The ability of the test to induce thermal residual stresses has the potential to  
92 quantify the restrained cracking capacity of a mixture at any desired time. This can lead to an  
93 approach where a mixture could be tested multiple times in the dual ring and purposely cracked  
94 at various ages with temperature reduction to develop a cracking curve.

95

### 96 **3.0 Experimental Equipment**

#### 97 3.1 Restraining Ring Material and Geometry

98 The restraining rings were fabricated from an Invar Steel alloy instead of conventional ASTM  
99 A53 Grade B steel (used for the standard ASTM C 1581-09 single ring test) in order to minimize  
100 the effects of temperature variation on the degree of restraint. Invar is a steel nickel alloy with a  
101 coefficient of thermal expansion (CTE) at or less than  $1.3 \times 10^{-6} \text{ } \epsilon/^{\circ}\text{C}$  [27-29], compared to  
102  $12.0 \times 10^{-6} \text{ } \epsilon/^{\circ}\text{C}$  for conventional steel [30]. For reference, the coefficient of thermal expansion of  
103 early age mortar varies [31-33], but is typically within the range of  $8 \times 10^{-6} \text{ } \epsilon/^{\circ}\text{C}$  to  $10 \times 10^{-6} \text{ } \epsilon/^{\circ}\text{C}$ .  
104 The thermal deformation of the restraining ring directly affects the degree of restraint of the  
105 sample during a temperature change. Larger restraining ring CTE values will produce a greater  
106 reduction in the degree of restraint which results in less residual stress development in the  
107 sample. This effect is significant because studying the restrained thermal behavior of the  
108 sample relies on developing residual stress in the sample during a temperature change. The  
109 lower CTE of an Invar restraining ring overcomes this limitation by stabilizing the degree of  
110 restraint during a temperature change and allows residual stress to be induced and measured.

111 The dual ring geometry is presented in Figure 1 where  $R_{OC}$  and  $R_{IC}$  are the outer face and inner  
112 face radii of the specimen respectively,  $R_{OO}$  is the outer face of the outer restraining ring radius,  
113  $R_{II}$  is the inner face of the inner restraining ring radius, and  $t$  is the thickness of each restraining  
114 ring. The dimensions are as follows:  $R_{OC} = 203 \text{ mm} \pm 3 \text{ mm}$  ( $8.0'' \pm 0.12''$ ),  $R_{IC} = 165 \text{ mm} \pm 3$   
115  $\text{mm}$  ( $6.5'' \pm 0.12''$ ),  $R_{OO} = 222 \text{ mm} \pm 3 \text{ mm}$  ( $8.75'' \pm 0.12''$ ),  $R_{II} = 146 \text{ mm} \pm 3 \text{ mm}$  ( $5.75'' \pm 0.12''$ ),  $t$   
116  $= 19 \text{ mm} \pm 3 \text{ mm}$  ( $0.75'' \pm 0.12''$ ), and  $76.2 \text{ mm} \pm 3 \text{ mm}$  ( $3'' \pm 0.12''$ ) tall. The measured weight of  
117 the inner ring is 11.5 kg (25.4 lb) and that of the outer ring is 16.0 kg (35.2 lb).

118 It should be noted that the thickness of the restraining ring is slightly different than the current  
 119 ASTM standard. This difference is intentional since the elastic modulus of Invar<sup>®</sup>  $E_{INVAR}=141$   
 120 GPa (20450 ksi) [27] is less than that of the conventional steel,  $E_{STEEL}=200$  GPa (29000 ksi). As  
 121 a result, an Invar ring of the same size as the standard steel ring would provide less restraint to  
 122 shrinkage. The goal of the design of the ring for this study was to match the degree of restraint  
 123 of the dual ring to that of the conventional ASTM C 1581-09 restrained ring test. The degree of  
 124 restraint of a restraining ring can be calculated by Equation 1 [22]:

$$\Psi = 1 - \frac{E_c}{E_s} \cdot \frac{1}{\frac{E_c}{E_s} \cdot \frac{1 - \left(\frac{R_{II}}{R_{IC}}\right)^2 \left[ (1 + \nu_c) \cdot \left(\frac{R_{OC}}{R_{IC}}\right)^2 + (1 - \nu_c) \right]}{1 - \left(\frac{R_{OC}}{R_{IC}}\right)^2 \left[ (1 + \nu_s) \cdot \left(\frac{R_{II}}{R_{IC}}\right)^2 + (1 - \nu_s) \right]}} \quad (1)$$

125  
 126 where  $E_c$  represents the elastic modulus of the cementitious mixture,  $E_s$  represents the elastic  
 127 modulus of the ring metal,  $\nu_c$  represents Poisson's ratio for concrete,  $\nu_s$  represents Poisson's  
 128 ratio for the ring metal, and  $\Psi$  is the degree of restraint. In order to compare ring geometries,  
 129 the modulus of elasticity and Poisson's ratio for the sample were assumed as constant values of  
 130  $E_c = 32$  GPa (4641ksi), and  $\nu_c = 0.18$ . Poisson's ratio for both the steel and Invar were selected  
 131 as  $\nu_s = 0.3$ .

132 Figure 2 shows the relationship between the Invar ring thickness and the degree of restraint  
 133 calculated with Equation 1 and the above mentioned specimen values. The degree of restraint  
 134 increases as the restraining ring is thickened. The Invar ring thickness that corresponds to a  
 135 degree of restraint equal to that of the ASTM C 1581-09 (72%) was found to be 19 mm.

136  
 137 **3.2 Instrumentation and Data Acquisition**

138 The stress that develops within the cementitious sample is determined by measuring the strain  
 139 in the Invar rings. Both of the Invar rings were instrumented with four opposing CEA-00 series  
 140 strain gauges [34] that were mounted at mid height. Figure 1 illustrates gauge locations. The  
 141 inner ring gauges were installed at mid height on the inner face of the inner ring while outer ring  
 142 gauges were installed at mid height on the outer face of the outer ring. All gauges are operated  
 143 as shunt calibrated quarter bridge circuits. The gauges have a grid resistance equal to  $120 \pm$   
 144  $0.3\% \Omega$ , Gage Factor  $2.05 \pm 0.5 \%$  at  $24 \text{ }^\circ\text{C}$ , temperature correction of Gage Factor  $+1.2 \pm$   
 145  $0.2$ , and an operating temperature range of  $-75 \text{ }^\circ\text{C}$  to  $+175 \text{ }^\circ\text{C}$  [34].

146 The gauges were installed with a Vishay<sup>®</sup> installation kit [35, 36]. Each mounting area was  
 147 sanded smooth and cleaned with an acidic solution. After neutralizing the area treated with  
 148 acid, the gauges were installed with M-Bond-200 modified alkyl cyanoacrylate adhesive. The

149 gauges were covered with Teflon tape, butyl rubber sealant, neoprene rubber, and sealed with  
150 aluminum tape. Strain relief folds were applied to the gauge lead wires.

151 A Vishay<sup>®</sup> system 5000 data scanner paired with Strain Smart<sup>®</sup> software was used to  
152 automatically record strain gauge data at five minute intervals. Data recording initiates  
153 immediately after the specimen is sealed in the insulation chamber which typically occurs about  
154 30 min after water contacts cement during mixing.

155

### 156 3.3 Strain Gauge Temperature Calibration

157 General practice shows that output from bonded strain gauges can change significantly when  
158 exposed solely to a temperature change [37, 38]. This is caused by the concurrent effects of  
159 changes in the gauge's grid resistivity and the mismatch in thermal expansion coefficients  
160 between the strain gage and substrate (in this case the ring). Therefore, even though the Invar  
161 ring dimensions are nominally stable throughout the test's temperature range, the gauges still  
162 require thermal correction. It should be noted that the gauges used in this test are specifically  
163 designed for use on substrates with low thermal coefficients to minimize error caused by  
164 temperature change. Several methods are available to correct thermal output with varying  
165 degrees of confidence and accuracy. First hand corrective measurement was chosen to correct  
166 the dual rings because it is the most accurate method of thermal correction as it accounts for  
167 many gauge specific issues [37, 38]. This involved generating a correction curve for each gauge  
168 by varying the temperature of the rings in the unstressed state and recording the resulting  
169 output. Figure 3a and Figure 3b illustrate the strain correction curves for gauges on the inner  
170 and outer rings, respectively. It should be noted that the curved shape of the plot is expected  
171 and is typical [37]. Strain Smart<sup>®</sup> has a function that corrects the strain output based on these  
172 curves from temperature readings taken on the ring surface. This is accomplished by taping a  
173 type T twisted pair thermocouple to the surface of the ring. Since the thermal uniformity of the  
174 rings is high, as discussed later in this paper, it is not necessary to measure temperature at  
175 every strain gauge. The correction curves were verified by subjecting the rings to a temperature  
176 change without a sample. Figure 3c illustrates the corrected output, and it can be seen that  
177 once the correction is applied the gauge output varied less than 4  $\mu\epsilon$  when subjected to a 45 °C  
178 temperature change.

179

### 180 3.4 Insulating chamber

181 An insulation chamber was constructed to control temperature and provide options for semi-  
182 adiabatic studies. Figure 4a shows the general view of the test setup in the insulation chamber.  
183 The restraining rings rest on a circular section of plywood base lined with an acetate sheet to  
184 provide a sealed, low friction surface. Four eye bolt lugs mounted to the base allow the  
185 assembly to be lifted in and out of the chamber. The rings are surrounded on all sides by a  
186 minimum of 50 mm (2") thick microporous insulation with a thermal conductivity of 0.019 W/m·K

187 at 20 °C (approximately half that of conventional glass fiber insulation). The top portion of  
188 insulation is removable to provide access to the chamber.

189

### 190 3.5 Temperature Control System

191 Temperature control is provided via a programmable 28 liter water bath system pumping an  
192 ethylene glycol water mixture at 24 liters/min through a looped copper coil inside the chamber.  
193 The ethylene glycol mixture enables the bath temperature to be lowered below freezing to  
194 approximately -20 °C. Figure 4b shows the placement of this coil on top of the restraining rings.  
195 A circular 3.2 mm (1/8”) thick sheet of aluminum is placed on top of the rings to provide a rigid  
196 platform for the coil. The water bath continuously monitors the temperature delivered to the  
197 chamber by using an external probe mounted on the inlet of the coil. This enables the system  
198 to automatically compensate for heat loss or gain through the tubing connecting the bath to the  
199 chamber. In-line valves are installed on the external tubing to allow the user to turn the coil flow  
200 on or off.

201 The system’s heating and cooling capabilities were determined by placing four type T  
202 thermocouples on an aged mortar sample at room temperature and varying the bath  
203 temperature as quickly as possible. The heating test targeted an end temperature of 50 °C and  
204 it can be seen in Figure 5a that the maximum temperature change the system can generate is  
205 about 1.8 °C per hour at a 20 degree differential between the bath and sample. The cooling test  
206 targeted an end temperature of 13 °C as shown in Figure 5a. It can be seen the temperature  
207 change rate decreases as the difference between bath and sample temperature decreases.  
208 The maximum thermal differential recorded in the sample during forced heating and cooling  
209 between two points spaced vertically or horizontally on the ring was 0.3 °C. This indicates that  
210 forced heating and cooling produces uniform temperatures in the sample.

211

### 212 4.0 Semi Adiabatic Properties of Chamber

213 The insulating properties of the chamber were examined by heating or cooling a well aged  
214 mortar sample with the coil and then allowing it to naturally return to ambient room temperature.  
215 The resulting temperature change was monitored with a type T thermocouple embedded in the  
216 sample. Figure 5b illustrates the free heating and cooling curves of the sample in the chamber.  
217 It can be seen, similar to forced heating and cooling, a larger temperature difference between  
218 the sample and ambient air will produce a faster temperature reduction or increase.

219 The heat transfer coefficient of the system was determined to quantify effectiveness of the  
220 insulation chamber and to provide a method to extrapolate the measured semi-adiabatic case to  
221 a theoretical adiabatic condition. First the amount of heat flowing into or out of the chamber was  
222 calculated from the free heating and cooling thermal profiles and Equation 2:

$$Q = (M_{RINGS}C_{P,RINGS} + M_{SAMPLE}C_{P,SPECIMEN})\Delta T \quad (2)$$

223 where Q represents the total heat flow (kJ),  $M_{RINGS}$  is the combined mass of the two Invar rings  
224 (27.5 kg),  $M_{SAMPLE}$  is the mass of the sample (1.7 kg),  $C_{P\_RINGS}$  is the heat capacity of Invar  
225 (0.460 kJ/kg/°C),  $C_{P\_SAMPLE}$  is the heat capacity of concrete (1.00 kJ/kg/°C) and  $\Delta T$  (°C) is the  
226 change in sample temperature over a 10 hour interval. Total heat transfer was calculated as -  
227 54.1 kJ for the free cooling curve and 16.3 kJ for the free heating curve.

228 Once the heat flow was determined, the heat transfer coefficient was calculated with Equation 3:

$$U = \frac{Q}{A(T_{SAMPLE} - T_{AMBIENT})\Delta t} \quad (3)$$

229 where U represents the heat transfer coefficient in units of W/m<sup>2</sup>/K, A is the measured surface  
230 area of insulation exposed to the inner chamber holding the rings/sample (0.511 m<sup>2</sup>),  $T_{SAMPLE}$  is  
231 the temperature of the sample at an instant in time,  $T_{AMBIENT}$  is the ambient air temperature  
232 outside of the chamber, and  $\Delta t$  is the duration of time in seconds. The resulting heat transfer  
233 coefficient was approximately 0.03 W/m<sup>2</sup>/K and provides reasonable agreement with the given  
234 thermal conductivity of the insulation and its thickness.

235 In addition to investigating the heating and cooling recovery characteristics of the chamber, the  
236 early age semi-adiabatic behavior of a fresh mortar was determined. A mixture designated as  
237 M-0 (as detailed later in Table 1) was allowed to freely heat and cool in the chamber and was  
238 instrumented with type T thermocouples to determine its thermal history and uniformity. The  
239 temperature at four points within the chamber was monitored for five days. Three  
240 thermocouples were equally spaced around the ring and embedded in the top quarter of the  
241 sample. One thermocouple was placed directly beneath the sample. A fifth monitored the room  
242 ambient air temperature. The results of this test are illustrated in Figure 5c, and it can be seen  
243 that the maximum difference between thermocouples inside the chamber was only 0.2 °C,  
244 indicating a high degree of thermal uniformity throughout the sample. The temperature peaked  
245 at 38.8 °C ± 0.5 °C at an age of 20 h and then began cooling towards room temperature. As  
246 expected, the cooling curve closely matches the free cooling curve in Figure 5b.

247

## 248 **5.0 Materials and Experimental Procedures**

### 249 **5.1 Mixture Proportions**

250 Three mortar mixtures with varying shrinkage performance were chosen to study several  
251 capabilities of the dual ring test. They are designated M-0, M-11, and M-24 with their  
252 proportions provided in Table 1. M-0 was a plain mortar while M-11 and M-24 utilized internal  
253 curing with pre-wetted fine lightweight aggregate (FLWA). All mixtures had a water-to-cement  
254 ratio of 0.30 by mass ( $w/c = 0.30$ ) and a paste volume of 45 %. The internally cured mixtures  
255 M-11 and M-24 had 11 % and 23.7 % of the total mixture volume comprised of FLWA,  
256 respectively. It should be noted the 23.7 % replacement value corresponds to the theoretical  
257 value of internal curing water that is required to match the chemical shrinkage [39].

258

259

Table 1 - SSD Mixture Proportions

	M-0 Plain Mortar	M-11 FLWA	M-24 FLWA
<b>Material</b>	<b>(kg/m<sup>3</sup>)</b>	<b>(kg/m<sup>3</sup>)</b>	<b>(kg/m<sup>3</sup>)</b>
Cement (Type I)	728	728	728
Water	218	218	218
Fine Aggregate	1444	1133	821
FLWA (SSD)	0	204	409

260

261 5.2 Materials

262 Type I ordinary portland cement was used (ASTM C 150-05) with a Blaine fineness of  
 263 370 m<sup>2</sup>/kg, and an estimated Bogue composition of a 56 % C<sub>3</sub>S, 16 % C<sub>2</sub>S, 12 % C<sub>3</sub>A and 7 %  
 264 C<sub>4</sub>AF. Normal weight river sand was used with a fineness modulus of 2.71 and an oven dry  
 265 specific gravity of 2.58. The lightweight aggregate used in M-11 and M-24 was a manufactured  
 266 rotary kiln expanded shale with a fineness modulus of 4.3, an oven dry specific gravity of 1.56,  
 267 and a 24 hour absorption value of 10.5 % by mass. A high-range water-reducing admixture  
 268 (HRWRA) was added at a rate of 1 g mass per 100 g of cement. Mix water consisted of tap  
 269 water conditioned to 23 °C ± 1 °C.

270

271 5.3 Mixing Procedure

272

273 Aggregate for each mixture was batched in the oven dry state. FLWA was presoaked for 24 h ±  
 274 0.5 h in the mix water (including the water for prewetting) while sealed in a container. Mixing  
 275 was performed in accordance with ASTM C 192-07. First aggregate was loaded into the  
 276 “buttered” mixer. Where applicable, the mixing water was decanted from the FLWA. The mixer  
 277 was started and 50% of the total water was added. The cement and remaining mix water  
 278 containing the HRWRA were then added. The mortar was mixed for 3 min, then rested for 3  
 279 min while the sides of the mixer were scraped, then mixed for a final 2 min.

280

281 5.4 Unrestrained Linear Autogenous Deformation – Corrugated Tube Protocol

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283 Linear autogenous strain of each mortar was measured using a technique where the fresh  
 284 mortar was placed in corrugated polyethylene molds per ASTM C 1698-09 [40]. The  
 285 corrugations in the mold produce greater stiffness in the radial direction than the longitudinal  
 286 thereby forcing shrinkage to occur along the length of the tube. This technique is designed to  
 287 minimize restraint and yields the free shrinkage profile of each mixture. The single laboratory  
 288 precision stated in the standard for mortar samples is 28 µε.

289

290 Each mortar mixture was cast into two corrugated tubes, vibrated, capped, and placed in the  
 291 dilatometer. Length change of each tube was measured with two linear variable differential  
 292 transformer (LVDT) displacement transducers and was recorded by the data acquisition system  
 293 at 5 minute intervals. The recorded values were zeroed to the time of final set as determined by  
 294 ASTM C 403-08.

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298 5.5 Restrained Shrinkage – Dual Ring Test

299

300 The instrumented rings were prepared by coating the surfaces that would make contact with the  
 301 sample with form release and a layer of acetate sheet in order to minimize friction on the  
 302 sample. The fresh mortar was then cast between the two rings in two layers. A handheld  
 303 vibrator was used to consolidate each layer. The top of the sample was struck level with the top  
 304 of the ring and then capped with the separator plate and temperature control coil. The top  
 305 layers of insulation and chamber cap were then installed to effectively seal the specimen in the  
 306 chamber to control its temperature and to prevent drying shrinkage.

307

308 The temperature control system was operated at 23 °C ± 0.2 °C for a minimum of 8 h prior to  
 309 casting, to bring the rings and chamber to a consistent temperature. It then operated at 23 °C ±  
 310 0.2 °C until the test ended due to the sample cracking or 8 d. After 8 d, the temperature was  
 311 reduced at a rate of 1°C/h, to attempt to induce a crack in the sample by utilizing thermal  
 312 shrinkage to produce additional tensile stress. The minimum temperature applied to the sample  
 313 in this study is -5 °C ± 0.2 °C.

314

315 The strain measured on the inner ring ( $\epsilon_{IN}$ ) and outer ring ( $\epsilon_{OUT}$ ) is reported as the average  
 316 output of the four gauges on each ring. The precision of the average strains from subsequent  
 317 tests of the same mixture deviated less than 6  $\mu\epsilon$ . These strains can be used to determine the  
 318 time of cracking by observing a sudden drop in readings. In addition, they can be used to  
 319 calculate the residual stress that develops in the sample [24, 26]. First the pressure exerted by  
 320 the sample on the inner ring  $P_{IN}$  can be calculated using Equation 4 [22]:

321

$$P_{IN} = -\epsilon_{IN} E_{INVAR} \left( \frac{R_{IC}^2 - R_{II}^2}{2 \cdot R_{IC}^2} \right) \quad (4)$$

322 The pressure exerted by the sample on the outer ring  $P_{OUT}$  is calculated by Equation 5 [22]:

323

$$P_{OUT} = \epsilon_{OUT} E_{INVAR} \left( \frac{R_{OO}^2 - R_{OC}^2}{2 \cdot R_{OC}^2} \right) \quad (5)$$

324 The two pressures obtained from ring strains are then used to calculate the circumferential  
 325 “residual” stress in the sample at  $R_{IC}$  ( $\sigma_s(R_{IC})$ ) by Equation 6a:

326

$$\sigma_{\theta}(R_{IC}) = P_{IN} \left[ \frac{R_{OC}^2 + R_{IC}^2}{(R_{OC}^2 - R_{IC}^2)} \right] - P_{OUT} \left[ \frac{2 \cdot R_{OC}^2}{(R_{OC}^2 - R_{IC}^2)} \right] \quad (6a)$$

327 Substituting Equations 4 and 5 into 6a yields Equation 6b for the ring geometry employed in this  
 328 study. The residual stress ( $\sigma_{\theta}$ ) is output in units of MPa or PSI when units of MPa or PSI are  
 329 used in the  $E_{INVAR}$  terms. The values for  $\epsilon_{IN}$  and  $\epsilon_{OUT}$  are input as actual strain.

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$$\sigma_{\theta}(R_{IC}) = -0.53 \epsilon_{IN} E_{INVAR} - 0.58 \epsilon_{OUT} E_{INVAR} \quad (6b)$$

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## 6.0 Results and Discussion

### 6.1 Results of Unrestrained Shrinkage Test

The unrestrained shrinkage history of the three mixtures during the first 7 days is shown in Figure 6. It can be seen that the plain mortar M-0 shrinks significantly more than the two mixtures M-11 and M-24 that contain the prewetted LWA (internal curing). The M-11 and M-24 mixtures undergo an initial expansion which has been seen by other researchers [41, 42]. After the expansion phase, M-11 begins to shrink while M-24 continues to expand. It should be noted that even though the M-11 mixture shrinks, it does not develop negative strain (tensile).

### 6.2 Results of Dual Ring Test

The inner and outer ring strain history is illustrated in Figures 7a and 7b, respectively. Residual stress development is shown in Figure 8. It can be seen the plain mortar M-0 only develops strain in the inner ring, indicating that it only shrinks. This was anticipated as the free shrinkage curves only exhibit shrinkage. M-0 continues shrinking until it develops a stress of 3.6 MPa (tension) at approximately 4 d, at which time it cracks.

Mixture M-11 develops no expansive stress and develops a residual tensile stress of 1.4 MPa at 8 d while operating at constant  $23\text{ }^{\circ}\text{C} \pm 0.2\text{ }^{\circ}\text{C}$ . The temperature was then decreased at a rate of  $1\text{ }^{\circ}\text{C}/\text{h}$  and the resulting increase in residual stress can be seen until the sample cracks at 3.6 MPa at 8.2 d ( $14.3\text{ }^{\circ}\text{C}$ ). This indicates that the samples restrained shrinkage only developed 39 % of the stress required to induce cracking. Also, approximately  $6\text{ }\mu\epsilon$  of ring strain or 0.2 MPa residual stress in the sample is generated per  $1\text{ }^{\circ}\text{C}$  of temperature change.

It can be seen that mixture M-24 develops a slight expansive strain in the outer ring shortly after the measured time of set of 6 h. The expansion peaks at  $4\text{ }\mu\epsilon$  or 0.15 MPa at 11.8 h and then decreases over a period of 7 h, without producing an opposing reaction on the inner ring. It is likely that this reduction in stress is due to stress relaxation while the modulus of elasticity is low and the creep is high in the sample at early age. Neither shrinkage nor expansion is observed for the remainder of the test while temperature is held at a constant  $23\text{ }^{\circ}\text{C} \pm 0.5\text{ }^{\circ}\text{C}$ . The free shrinkage history during this time shows a subtle expansion which may not be large enough to overcome the rate of creep under restrained conditions. After approximately 8 d, the temperature in the sample is decreased at a rate of  $1\text{ }^{\circ}\text{C}/\text{h}$  and an increase in shrinkage strain and residual tensile stress is observed. It can be seen that the rate of ring strain and residual stress development is the same in both the M-11 and M-24 samples. The M-24 sample does not generate a crack by the time it reaches the minimum temperature limit of  $-5\text{ }^{\circ}\text{C}$ .

Relative cracking potentials of M-11 and M-24 can be determined by comparing the amount of additional residual stress required to crack the sample by decreasing temperature. The M-11 sample required an additional 2.2 MPa of tensile stress to induce cracking, while M-24 requires

376 at least 3.0 MPa since it did not crack. Therefore it can be concluded that M-11 would have a  
377 greater potential to crack than M-24. This can be attributed to the amount of tensile stress in  
378 the sample immediately before the temperature begins to decrease. Since the M-11 sample  
379 begins the cooling period with approximately 1.5 MPa of tensile stress more than that of M-24, it  
380 is closer to its cracking capacity. While the slight early age expansion is generally more desired  
381 than shrinkage as seen in the M-24 sample, it can be seen that the volume stability of the  
382 sample after 12 h has a greater contribution to reducing cracking potential.

383

## 384 **7.0 Conclusions**

385 This paper has described the development of a 'Dual Concentric Ring Testing Device' that  
386 enables the residual stress that develops in concrete rings to be quantified as concrete expands  
387 and contracts due to chemical reaction, hygral shrinkage, or thermal movements. The ring is  
388 designed to provide a similar degree of restraint when compared with the ASTM C 1581-09  
389 standard test geometry; however conceptually any geometry can be used.

390 This paper quantifies the uniformity in temperature that may be expected throughout the ring  
391 and indicates that heating and cooling take place with less than 0.2 °C variance across extreme  
392 points on the sample.

393 The semi-adiabatic overall heat transfer coefficient for the insulation chamber containing the  
394 rings and a typical mortar specimen was calculated as approximately 0.03 W/m<sup>2</sup>/K.

395 The results of cooling a sample indicate that when a temperature reduction is added to  
396 autogenous shrinkage it may result in cracking, while autogenous shrinkage on its own may not.  
397 This may become a useful method to quantify the reserve cracking capacity of mixtures at a  
398 desired age. The direct comparison of crack resistance capacity at specific points in time may  
399 enable future research to set benchmarks for cracking performance.

400 The results from testing show that the dual ring can quantify the behavior of residual  
401 compressive stress during early age expansion. Restrained early age expansion results in  
402 compressive stresses in the sample. These stresses disappear by 24 h. As a result, the  
403 shrinkage performance of the sample after 24 h has a greater effect on cracking potential.

404

## 405 **8.0 Acknowledgements**

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408 The contents of this paper reflect the views and the accuracy of the data presented herein, and  
409 do not necessarily reflect the official views or policies of the Indiana Department of  
410 Transportation, nor do the contents constitute a standard, specification, or regulation.

## 411 **9.0 Disclaimer**

412 Certain commercial equipment, instruments, or materials are identified in this report in order to  
413 foster understanding. Such identification is not intended to imply recommendation or  
414 endorsement by the National Institute of Standards and Technology nor Purdue University, nor  
415 is it intended to imply that the materials or equipment identified are necessarily the best  
416 available for the purpose.

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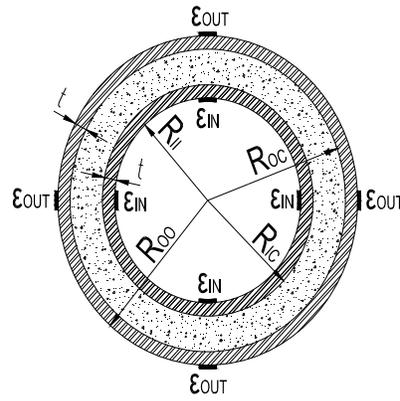
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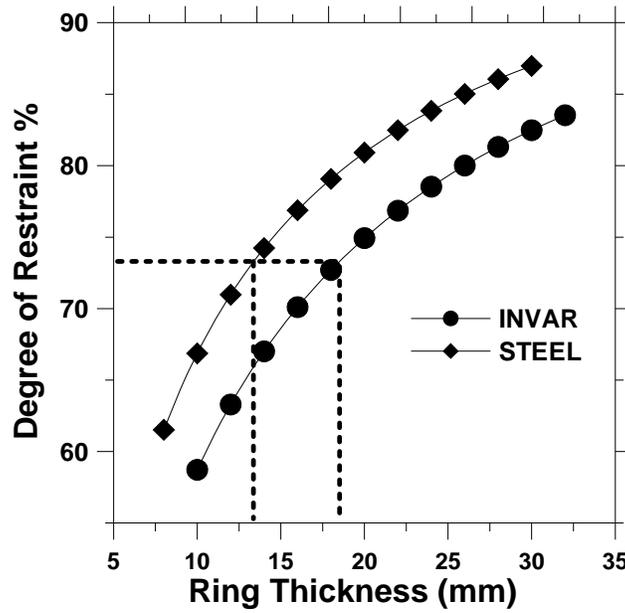
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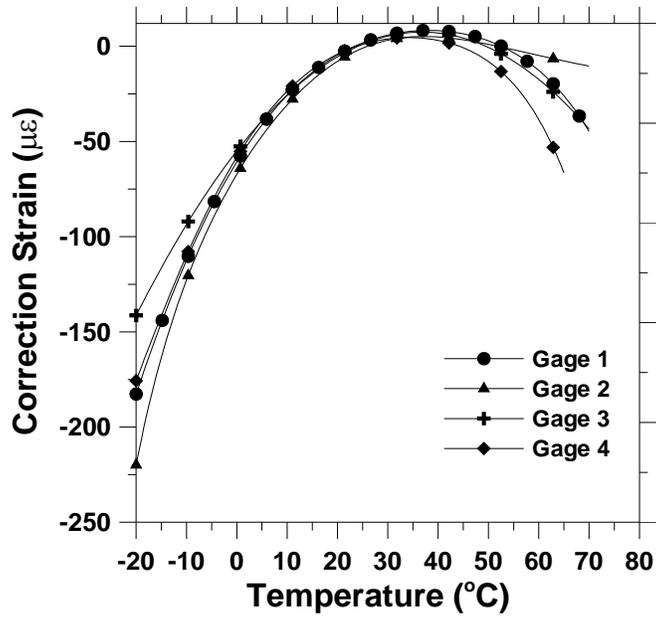
Figure 1 - Geometry of the Dual Ring Test

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Figure 2 – Effect of Invar Ring Thickness on DOR



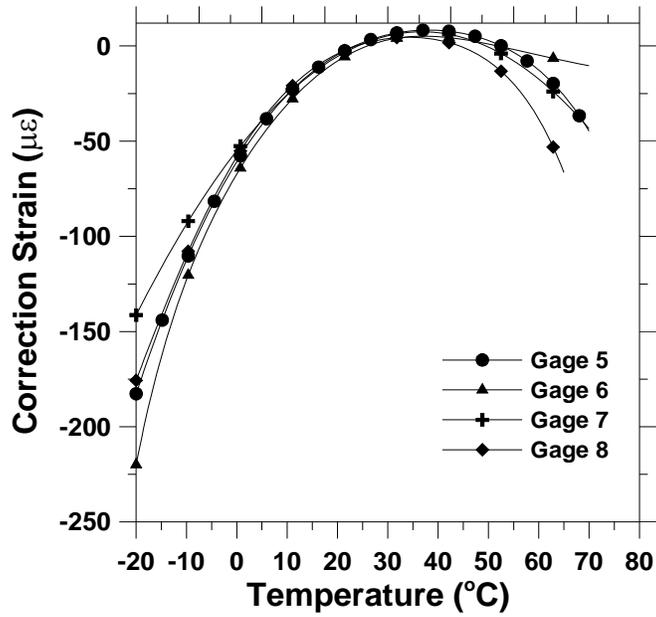
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Figure 3a - Inner Ring Thermal Correction



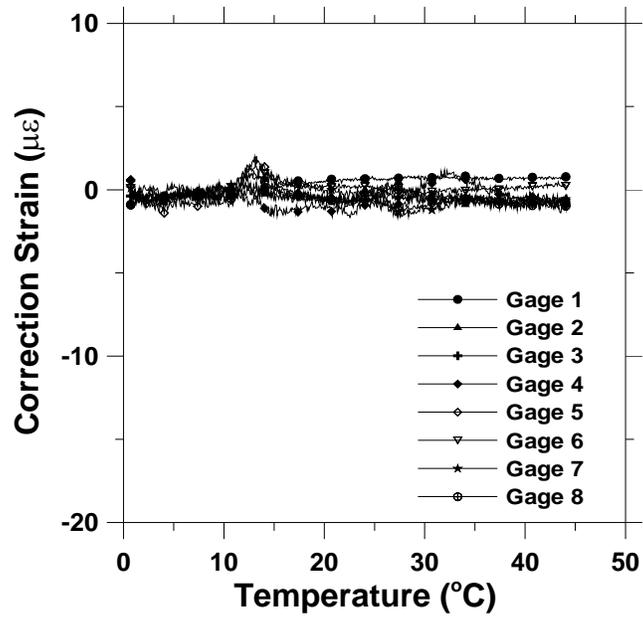
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Figure 3b - Outer Ring Thermal Correction



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*Figure 3c – Strain Thermal Corrections Verified*

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*Figure 4a - Ring in insulation chamber with top insulation removed*

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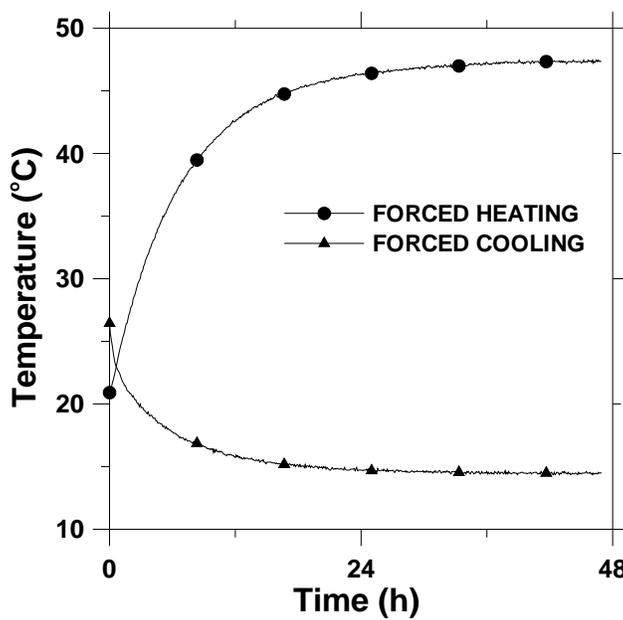


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Figure 4b – Temperature regulation coil

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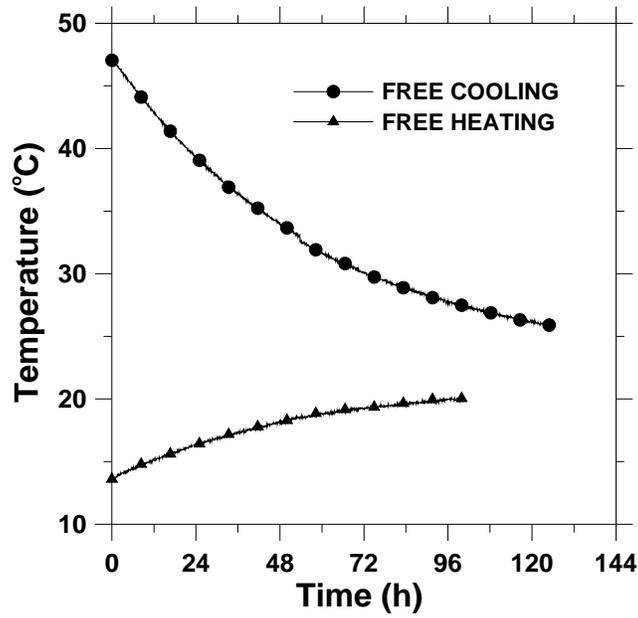


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Figure 5a - Forced Heating and Cooling Profile of Insulation Chamber

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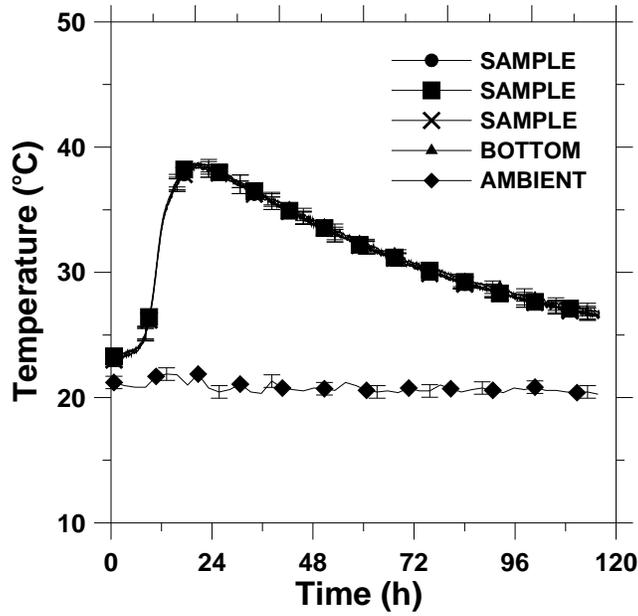
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Figure 5b - Free heating and cooling profile of insulation chamber

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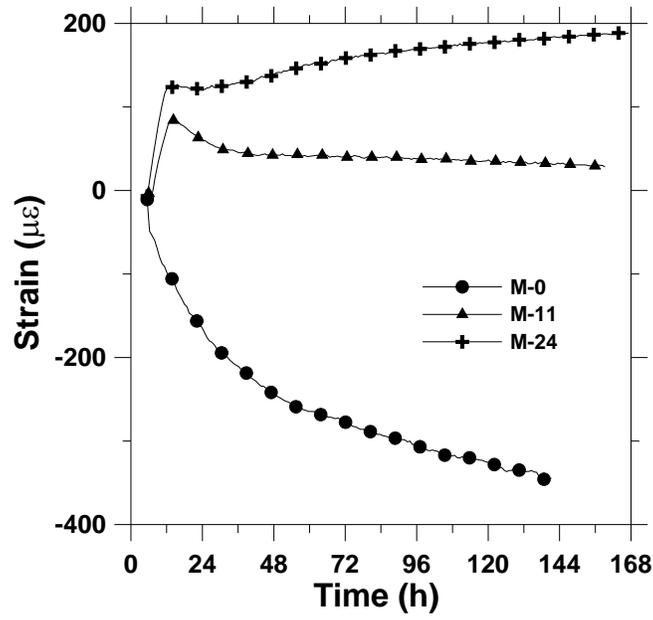
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Figure 5c - Thermal Profile of Semi Adiabatic Plain Mortar

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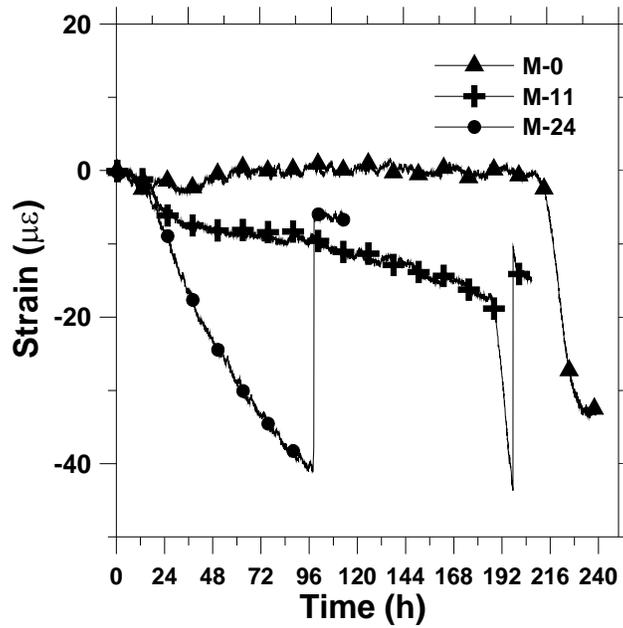


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Figure 6 - Unrestrained Linear Autogenous Shrinkage

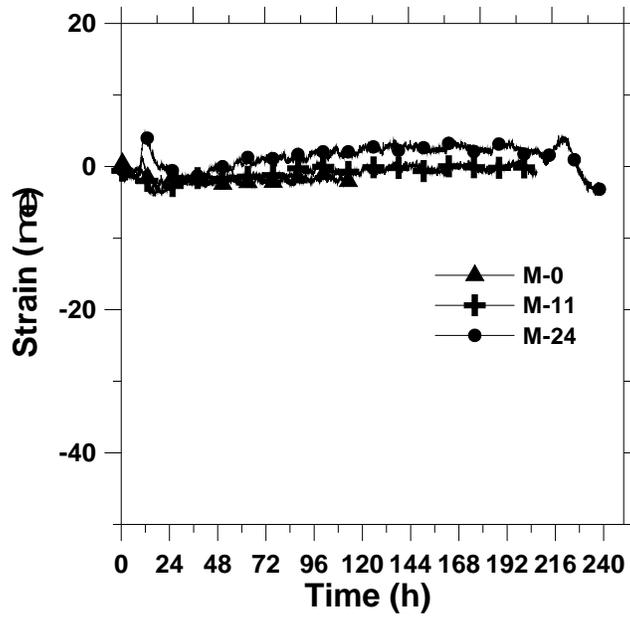
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Figure 7a - Inner Ring Strain History

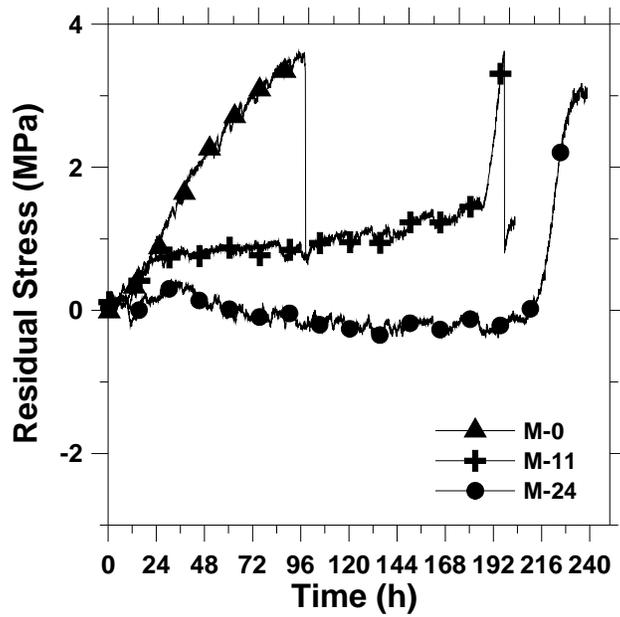


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Figure 7b – Outer Ring Strain History

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Figure 8 – Residual Stress Development in Three Samples

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