Probing single nanometer-scale pores with polymeric molecular rulers

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We previously demonstrated that individual molecules of single-stranded DNA can be driven electrophoretically through a single Staphylococcus aureus α-hemolysin ion channel. Polynucleotides thread through the channel as extended chains and the polymer-induced ionic current blockades exhibit stable modes during the interactions. We show here that polynucleotides can be used to probe structural features of the α-hemolysin channel itself. Specifically, both the pore length and channel aperture profile can be estimated. The results are consistent with the channel crystal structure and suggest that polymer-based “molecular rulers” may prove useful in deducing the structures of nanometer-scale pores in general.

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I. INTRODUCTION

High-resolution x-ray crystal structures of proteins are invaluable tools for basic research in biology, biophysics, and biotechnology.1 Although there are notable exceptions (e.g., Refs. 2 and 3), membrane-bound proteins are difficult to crystallize compared to their water-soluble counterparts. Thus, other methods are usually needed to reveal the salient features of transmembrane proteins.

Ion channels lend themselves to simple structure determination techniques because their functional aspect can be probed by conductance measurements. For example, scanning cysteine mutagenesis and covalent chemical modification were used to identify amino acid side chains that line the pore of the nicotinic acetylcholine receptor channel,5 the Staphylococcus aureus α-hemolysin (αHL) channel,6–14 and the active form of Bacillus anthracis protective antigen (i.e., PA63).15,16

Nonelectrolyte water soluble polymers have been used to deduce channel structural features. For example, in the pioneering study by Zimmerberg and Parsegian,17 pore-impermeant poly(ethylene glycol) (PEGs) molecules were used to estimate the change in volume that occurs when the voltage dependent anion channel18 gates between two pre-dominant conductance states. In addition, Krasilnikov and others used PEGs to estimate the radii of ion channels from the ability of size-selected PEGs to partition into the channel pore.11,19–36

Protein translocation across membranes, which plays a key role in many biological processes, can be facilitated by ion channels.37–39 Other biomolecules can be detected as they transport through ion channels. For example, we demonstrated that individual molecules of single-stranded DNA (ssDNA) could be characterized as they are driven electrophoretically into and through a single αHL channel.40 Because the mobility of negatively charged polynucleotides is less than that of monovalent ions (i.e., K+, Na+, and Cl−) in those solutions, the channel conductance decreases significantly when the anionic polymer is inside the pore. The mean lifetime of the polynucleotide-induced current blockades is proportional to the polymer contour length,40 which suggested that the polymer threads through the pore as a linear chain, as illustrated schematically in Fig. 1. Theoretical models and Monte-Carlo simulations that describe the transport of polynucleotides and idealized polymers through idealized nanoscale pores have been developed.41–55 In addition, the ability of another ion channel to catalyze DNA transport has been identified by Szabo and colleagues.56

The rate at which polynucleotides enter the αHL channel is voltage dependent.57 Assuming that the interaction between the polymer and the pore could be treated as a chemical reaction, a Van’t Hoff–Arrhenius rate law was used to estimate the height of the energy barrier for polymer entry into the pore57 and a more detailed stochastic simulation to describe this effect was developed by Ambjörnsson and colleagues.58 We demonstrate here how polynucleotides can be used as molecular rulers to better understand the interaction of a nanopore with individual polymers, and to determine the location of the energy barriers to polynucleotide transport.

II. MATERIALS AND METHODS

The ability of polynucleotides to partition into a nanometer-scale pore was studied by measuring the polymer-induced effects on the ionic current flowing through a single αHL channel in a planar lipid bilayer membrane.8,10 The current was measured before and after the addition of polymer to the bulk aqueous phase on one side of the membrane.
Polynucleotides were driven into the channel pore by an applied electrical potential of the appropriate polarity. Individual polynucleotides that enter the pore cause transient blockades in the single channel current.40 These events were digitally recorded and the lifetime, amplitude, and pattern of the ssDNA-induced current blockades were measured.59–61

A. Membrane and channel formation

Solvent-free planar lipid bilayer membranes62 were formed from diphytanoyl phosphatidylcholine (Avanti Polar Lipids, Inc., Alabaster, AL) in pentane (Burdick and Jackson, Muskegon, MI). The membranes were made on 50–120 μm diameter holes in a 17 μm thick Teflon partition that separates two identical Teflon chambers. The hole was pretreated with a solution of 10% (v/v) hexadecane (Aldrich) in pentane. Both chambers contained 1 M KCl (Mallinckrodt, Paris, KY), 5 mM HEPES (Calbiochem, San Diego, CA), titrated to pH 7.5 with concentrated NaOH (Mallinckrodt).

Single channels were formed by adding approximately 0.4 μg of αHL to a chamber on one side of the partition (herein called cis), which contained approximately 2 ml of 1 M KCl aqueous buffer solution. After a single channel formed, the cis chamber was rapidly perfused with fresh buffer to prevent further channel incorporation. An electrical potential of −120 mV, which drives anions from the cis to the trans side, was applied using Ag–AgCl electrodes in 3 M KCl, 1.5% (w/v) agar bridges. The current was converted to voltage and amplified using an Axopatch 200A patch-clamp amplifier and a CV 201 AU headstage (Axon Instruments, Foster City, CA). The signal was filtered using a Frequency Devices 9002 low-pass Bessel filter (Haverhill, MA) with a corner frequency set to 3/8 the sampling rate of either a National Instruments AT-MIO-16X 16-bit analog to digital converter board (Austin, TX) or an Axon Instruments analog to digital converter. The temperature was 23 °C ± 1 °C.

B. Polynucleotides and other reagents

The polynucleotides were purchased from Midland Certified Reagents (Midland, TX). The final concentrations of the polynucleotides in the cis and trans chambers were ~400 nM, unless otherwise noted. Neutravidin (Pierce Biochemicals), streptavidin (Molecular Probes) or α-BRDU polyclonal antibody (Fitzgerald Industries International Inc., Concord, MA) was added to cis or trans sides as noted.

III. RESULTS AND DISCUSSION

A. Polynucleotides partition into single αHL channels

Figure 2 illustrates typical blockades of the single αHL channel ionic current caused by individual molecules of singe-stranded DNA. This and previous work demonstrated that the lifetimes of polynucleotide transits are typically 1–10 μs per base.40,59,63,64

B. Location of polynucleotide transport barrier

Previously, we demonstrated that the addition of a large protein cap at one end of a polynucleotide would inhibit the complete translocation of the polymer through the αHL channel.57,59,65 Here, we provide more detailed experimental results that show how different length polymers can act as semiquantitative “molecular rulers” to determine how far the polymer must thread into the pore before it is committed to transport through the channel.

Different length biotinylated poly[dC] (i.e., bT-poly[dC]) molecules were added to the cis side in separate experiments. For illustrative purposes, the effects of 20 and 30-nucleotide long bT-poly[dC] are shown on the single channel current recordings (Fig. 3, top right). As expected, both polymers cause transient current blockades (Fig. 3 top, two single channel recordings, minus avidin). After adding avidin, the results show that the complex between avidin:bT-poly[dC]30, but not avidin:bT-poly[dC]20, occluded the pore virtually indefinitely [Fig. 3(a), plus avidin]. Similar experiments with
different length bT-poly[dC] molecules showed that polymers containing more than 25 nucleotides occlude the pore in the presence of avidin (data not shown). Qualitatively similar results are observed when both biotinylated single-stranded DNA (ssDNA) and avidin are added to the trans side (Fig. 3, bottom). However, in that case, the minimum-length capped poly[dC] that occluded the pore is between 10 and 20 nucleotides. A statistical mechanical description for the interaction between a stretched polymer and an attractive well (which keeps the polymers beyond a critical length in the pore) is outlined in the Appendix.

The results shown in Fig. 3 suggest that the barrier to polynucleotide transport is approximately 25 and 15 nucleotides from the cis and trans pore entrances, respectively. The barrier probably corresponds to the smallest geometric constriction inside the pore near the amino acid side chain M113. Indeed, the steepest gradient of the electrostatic potential occurs over the region with the smallest cross-sectional area inside the αHL pore.

C. Length of the αHL channel

To deduce additional structural information about the αHL channel, we used polynucleotides that can be capped at both ends. These polymers have binding sites for large macromolecules at both the 5′ and 3′ ends of the polynucleotide (e.g., 5′-BRDU-poly[dC]-bT-3′; where BRDU is brominated deoxy U). In the absence of the polymers, the single channel recordings are quiescent (Fig. 4, left). The addition of uncapped polymer to the cis side causes transient current blockades as illustrated in Fig. 4 (+polymer, top). A relatively large capping protein (e.g., α-BRDU) that binds to one end of the polymer is subsequently added to the cis side. The polymers that complex with the cap protein occlude the pore (Fig. 4, +cap 1 cis). Once occluded, the capped polymer can be cleared from the pore by momentarily reversing the sign of the applied potential (Fig. 4, +cap 1 cis, V+/−, top). If the capped polymer is long enough to extend past the trans pore entrance, that uncapped end interacts with a second ligand or cap (e.g., avidin) subsequently added to the trans side. The doubly capped polymer is thus trapped within the pore (Fig. 4, +cap 2 trans, top). Similar experiments using shorter polymers (e.g., Fig. 4, bottom) show that the ssDNA homopolymers must contain between 45 to 50 nucleotides of either thymine or cytosine to span the entire pore’s length.

These results demonstrate conclusively that ssDNA can partition into and thread completely through the pore, in agreement with results from our earlier study. Also, because the αHL pore is 10 nm long, the relative length of each nucleotide in the pore is ~0.22 nm, consistent with the structures of polynucleotides in solution. Because 45 nucleotides are sufficient to traverse the pore, the region inside the pore that commits the DNA to traversing the channel is approximately 5 nucleotides long. This zone corresponds to the narrowest segment inside the channel as determined by x-ray crystallography.

D. Geometry of the αHL channel probed with ssDNA

The single channel recordings in Fig. 5 show that the state structure is particularly rich for poly[dT]100 induced blockades. Still, the signals are simple enough to be tractable. These data demonstrate that the signal state structure depends on the direction of polynucleotide transport through the pore. Note that poly[dT]100 occasionally causes step structures that depend on the direction of transport and, as we show below, this provides information about the pore geometry.

Moreover, for events with lifetimes ≈2 ms (Fig. 6) the amplitude distributions for polymer entry from the cis and trans sides can each be modeled using five-kernel, and four-kernel gaussian mixture models (GMMs), respectively. These states (i.e., Gaussian kernels) are enumerated in Fig. 6. The general form of these models is:

\[
p(x|A,M,\Sigma) = \sum_{k=1}^{N} \frac{\alpha_k}{\sqrt{2\pi} \sigma_k} e^{-\frac{1}{2}(x - \mu_k)(x - \mu_k)^T \Sigma^{-1}},
\]

where \(x\) is the ionic conductance amplitude, \(N\) is the number of Gaussian kernels in the mixture sum, \(A\) is the set of positive mixture weights that sum to one, \(M\) is the set of kernel means, and \(\Sigma\) is the set of kernel standard deviations. We obtained two distinct GMMs, one for each transport direction. The kernels for cis and trans occluded states are num-

![Image](https://example.com/image.png)
bered 1, 2, 2a, 3, and 1’, 2’, 3’, respectively.

The Gaussian mixture parameters, estimated as described below, result in a mixture probability density function that cannot be rejected at the 0.05 probability level using the Kolmogorov–Smirnov goodness of fit test. They are subsequently incorporated as output distributions of a hidden Markov model (HMM) with a persistent, but ergodic, transition matrix.60,61

Interestingly, the blockade structure for cis to trans polymer transport evolves with increasing event duration, as shown in Fig. 7. Qualitatively similar results were obtained with events caused by polymer transport from the trans to the cis side (data not shown). The morphologies are mostly confined to state 1 for the short lifetimes, bifurcate to state 1 or state 3 for intermediate lengths, and show a characteristic event step from state 1 to state 3 within events for longer blockade lifetimes [Fig. 5(a)]. This is consistent with the polymer entering the cis-side vestibule, being dislodged in the short events, and progressively exploring the narrower apertures further in the channel for events with increasing lifetimes. Very long-lived events (sometimes up to seconds, data not shown) tend to show an irregular transition between these and additional states, and are more difficult to interpret.

Figure 8 illustrates the MAP state sequence decoded using the signal amplitude Gaussian mixtures as the output distributions of our HMM, and the statistical decoding procedure based on that of Viterbi.68 This results in a state sequence of the current blockades in terms of the GMM amplitude distribution kernels. Partial-then-deep blockade for cis polymer entry and a deep-then-partial blockade for trans polymer entry emerge as common patterns. The results are consistent with the channel structure because the cis-side vestibule is larger than the pore trans side.2

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**FIG. 4.** The length of the αHL channel determined using differing length polynucleotides. The leftmost time series shows the open channel current. The addition of different polynucleotides (top: 5’-BRDU-poly[dT]20-bT-3’; bottom: 5’-bT-poly[dT]20-bT-3’) cause transient blockades in the current. Subsequent addition of a large cap protein that binds to one end of the polymer occludes the pore until the potential is reversed. A second cap protein, which can bind to the free end of the polynucleotide, is then added to the trans side. The 40-mer (bottom right), but not the 50-mer (top right) can be cleared from the pore by reversing the applied potential. This result suggests the 40-mer does not completely span the channel and that the 50-mer does.

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**FIG. 5.** Representative ionic current blockades for poly[dT]100 interactions with the αHL channel. The polymer is added to either the (a) cis or (b) trans side and the applied potential is \( V = -120 \) or +120 mV, respectively. The patterns of the blockades, which illustrate the states of the bimolecular interactions, are consistent across large ensembles and can be classified. The blockade morphologies correlate with the geometry of the channel. Most of the open channel current recording between events is removed for clarity.

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**FIG. 6.** A diagram illustrating the different states of the αHL channel. The channel is in the open state at the top and transitions to the blocked state at the bottom.

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**FIG. 7.** A diagram illustrating the different states of the αHL channel. The channel is in the open state at the top and transitions to the blocked state at the bottom.

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**FIG. 8.** A diagram illustrating the different states of the αHL channel. The channel is in the open state at the top and transitions to the blocked state at the bottom.
long events show a bimodal conductance morphology. Sixty microsecond events show a state 1 conductance level; ades stratified by duration show that the event structure evolves in a simple channel from the frequency of longer events to best visualize the common event morphology GMM estimates. The Kolmogorov-Smirnov test offers a data driven, because it does not require independently generated ground truth annotations of the training data. Also, the classical Baum–Welsh procedure does not lend itself to a statistical goodness of fit test. In contrast, our signal amplitude GMM allows us to assess the statistical model's accuracy, and thus permits unsupervised state identification.

The detailed nature of the two-state blockades provide additional information about the interaction between poly[dT] and the αHL channel. Figure 9 shows the lifetime distributions for two predominant blocked states; the most common shallow blockade state (state 1) and the deeper blockade state (state 3) are shown in Figs. 9(a) and 9(b), respectively. The state 1 lifetime distribution appears to be approximately exponential \( p(t) = \lambda e^{-\lambda t} \) and thus consistent with the polymer partitioning into, and randomly exploring the cis-side vestibule interior. An exponential lifetime distribution implies a constant hazard rate \( \lambda \), where \( \lambda = p(t)/(1 - P(t)) \), and \( P(t) \) is the cumulative of the density \( p(t) \). State 1 events are followed by the polymer either retreating whence it came (state 1 only events, Figs. 5–8) or threading into the narrower segment of the pore (transition to state 3); which commits the polymer to vectorial transport. In contrast to the exponential distribution [Fig. 9(a)], the more symmetrical mode for the state 3 lifetime distribution [Fig. 9(b)] suggests a more deterministic phenomenon; as would be expected for a population of uniform-length polymers threading through the channel.

IV. CONCLUSIONS

We demonstrated here that steady-state and kinetic information gleaned from the interactions between DNA polymers and a single nanometer-scale pore provide structural information about the latter. Different polynucleotides were used to deduce gross structural details of the αHL channel, such as the pore length and the depth at which a polymer is committed to transport. We also showed that for a given polymer type, the polymer-induced ionic current blockade patterns are consistent with a small set of archetypal exemplars (Figs. 5–9) that most likely correlate with the channel geometry; e.g., poly[dT] current blockade patterns with two steps and three predominant blockade levels (Fig. 5).
One possible interpretation of the latter results, which is illustrated in Fig. 10, is that the degree of ionic current blockade correlates with the amount of poly[dT] mass in the cap domain vestibule (partial blockades), or in the smallest aperture (deeper blockade) between the vestibule and the β-barrel stem region of the pore. This simple hypothesis is consistent with the blockade patterns caused by poly[dT] transport in either direction (Fig. 8) and the lifetime distributions of poly[dT]-induced blockades (Fig. 9). These results, and others shown here, demonstrate that DNA can be used to probe the geometry of αHL channel. By inference, this technique might also prove useful for probing the structures of other nanometer-scale pores, including those in solid-state materials.72–81

We also demonstrated the use of our unsupervised state identification process and subsequent state sequence decoding technique using an HMM-like statistical model to quantify the kinetics of interactions between nanopores and biomolecules. This technique allows us to measure complex multi-state signals generated by this system, and elucidate the information contained therein. It also permits quantification of a large number of events, thus allowing a detailed statistical study of the polynucleotide-nanopore kinetic interactions.

The ability to entrap indefinitely an individual polynucleotide in a single nanometer-scale pore may help extract information from the polymer with higher fidelity than is currently possible.70 For example, it has been suggested that averaging the ionic current time series by flossing the polymer back and forth may improve the signal to noise ratio in an averaged ensemble.60,82–85

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APPENDIX: STATISTICAL MECHANICAL DESCRIPTION OF A STRETCHED POLYMER IN AN ATTRACTIVE WELL

Predicting when the current blockade is persistent [Fig. 3(a), 30 mer] or transient [Fig. 3(a), 20 mer] can be approached using statistical mechanics. Suppose the chain is stretched by the electric field as shown in Fig. 3 (left). Then the total potential energy, PE, in the presence of a uniform electric field, $E$, is given by:

$$PE = E\Delta x (1 + 2 + 3 + \ldots + n) = E\Delta xn(n+1)/2,$$

where $\Delta x$ is the distance between monomers and $n$ is the total number of monomers. The rate, $R$, at which the polymer escapes from the well depends on the well depth and is:

$$R = K \exp(-E \Delta x n(n+1)/2kT),$$

where $kT$ has its usual meaning. $R$ diminishes rapidly with increasing $n$. Consequently there is a critical value of $n$ beyond which the rate $R$ is so small that the particle is trapped in the pore.

FIG. 9. Lifetime distributions for both segments of two-state blockades caused by poly[dT]100. The distribution of lifetimes for the lesser blocked states (a) is approximately exponential; whereas that of the deeper blockade state (b) is clearly different. The result suggests the mechanism for the two blockade states are different. The polymer was added to the cis side.

FIG. 10. A toy model to describe the interaction of individual poly[dT] polynucleotides with the αHL ion channel. Illustrations of the polynucleotide entry into and possible transport through the pore (top) and the resulting stylized current blockades (bottom) caused by the presence of a polymer either in the cis vestibule only (left and right) or in the tightest constriction (center). The 3 predominant αHL conductance states caused by poly[dT] probably correspond to the amount of polymer in the pore. The two shallow conductance states (1 and 2) may be caused by significantly different amounts of polymer in a relatively narrow region within the cap. Conductance state 3 most likely is caused by polymer entry into the narrowest segment of the channel, which leads to the subsequent transport of the polymer through the pore. If the conductance in a particular blockade never reaches state 3, the polymer probably exits from the same mouth it entered.
The rate of escape depends on other variables including the pore width. Imagine an enclosure bounded by a cylindrical wall given by \( \rho(z) \) and by horizontal planes at \( z=0 \) and \( z=L \). One end of the polymer is tied to the center of the \( z=0 \) plane and the other monomers of the chain reside within the cylinder as before under the influence of an electric field \( E \). The surfaces can be attractive or repulsive to the monomers. Computer modeling and the relevant thermodynamic properties could be used to determine the partition function \( Q \):

\[
Q = \frac{1}{N} \sum_{\{x\}} \exp \left( \frac{-kT}{ \beta } \right) \theta(E_x) \cdot \exp \left( -\frac{1}{\beta} \int \rho(z) \cdot dz \right)
\]

where \( F = -kT \ln Q \) and \( S = -\beta F/\beta T = U - TS \).

\( R \) will be a function of \( E, n, \) and \( T \), wall attraction if any, and a functional of \( \rho(z) \). Knowledge of \( R \) should allow us to estimate \( \rho(z) \) and \( L \). This problem can be viewed as a generalization of a chromatography problem solved by Cassada (and references therein).

Finally, the chain may undergo a coil-stretch transition. From the formula for the PE, the forces on monomer segments near the point of attachment to the biotinylated blob increase linearly in both \( E \) and \( n \). Thus for long chains, there is a point where the “elastic limit” of the spring constant is reached, which leads to the coil-stretch transition.