Effect of ionic substitutions on the structure and dielectric properties of hafnia: A first principles study

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First principles calculations were used to study the effects of Si, Ti, Zr, and Ta (+N) substitutional impurities on the structure and dielectric properties of crystalline HfO$_2$. The dielectric constant of monoclinic HfO$_2$ can be enhanced by substituting more polarizable ions for Hf, but the band gap is decreased. Enhancing the permittivity without decreasing the band gap requires forming the tetragonal or cubic phase of HfO$_2$. Among the ions studied, Si alone is found to stabilize a nonmonoclinic phase of HfO$_2$ relative to the monoclinic phase, but only at an atomic concentration above about 20%. Various experiments have reported the formation of nonmonoclinic phases of HfO$_2$ with increased permittivity when other ions are substituted for Hf. It is concluded that these structures are, in general, either metastable or are stabilized by extrinsic factors or by a layered arrangement of the substitutional cations. © 2008 American Institute of Physics. [DOI: 10.1063/1.2903870]

I. INTRODUCTION

The properties of HfO$_2$, including the fact that it has a higher static dielectric permittivity $\kappa_s$ than SiO$_2$, make it one of the leading candidates for an alternate gate dielectric material. In addition to having a high permittivity, a practical gate dielectric material must exhibit phase stability in contact with Si, have low leakage current, have appropriate band offsets and threshold voltage stability, and maintain sufficient channel electron and hole mobility, etc. Drawbacks of HfO$_2$ as a gate dielectric material include an unstable threshold voltage and low channel mobility.

It is natural to attempt to improve the properties of HfO$_2$ by the substitutional addition, or “doping,” of different ions. Improved properties have been reported with the addition of Al, Y, La, other rare earth elements, Si, Ti, Zr, and Ta plus N. Generally, the reports show higher threshold stability, implying fewer charge trapping defects, while maintaining a sufficiently low leakage current. Furthermore, numerous studies show that $\kappa_s$ can be substantially increased, from roughly 15 to roughly 30 by the addition of other ions and appropriate heat treatment. Substitutional addition of other ions to HfO$_2$ is thus a promising avenue to practical gate dielectrics for advanced semiconductor applications.

Pure HfO$_2$ has three polymorphs as a function of temperature (Fig. 1). At high temperatures, it has the cubic fluorite structure with the Hf coordinated with a cube of eight O and the O coordinated with a tetrahedron of four Hf; at intermediate temperatures, a tetragonal distorted fluorite structure, and at low temperatures, a monoclinic phase with the Hf sevenfold coordinated, half of the O fourfold coordinated and half threefold coordinated. The phase transformation between tetragonal and monoclinic is first order by symmetry. The phase transformation between cubic and tetragonal order is also first order, although it is not constrained to be so by symmetry. In those experiments where the permittivity of HfO$_2$ is enhanced by doping, the increase in $\kappa_s$ is always associated with a change of symmetry from the monoclinic phase of HfO$_2$ to the tetragonal or cubic one.

The most stable phases (or two-phase mixtures) for HfO$_2$ with ionic substitutions are given in the published equilibrium phase diagrams. The maximum solubilities of the above-mentioned ions in the low-temperature monoclinic HfO$_2$ structure are given in Table I. Except for ZrO$_2$, which is isostructural with HfO$_2$, the solubilities are generally small (order 1%–10%) and decrease with decreasing temperature. Table II contains one oxynitride, TaON. This structure has not been studied much, but it is essentially isostructural with HfO$_2$ (Fig. 2) except that the N all go on the fourfold oxygen sites of HfO$_2$. Given the structural similarities between HfO$_2$ and TaON, it is quite possible that they form a complete solid solution series.

Contrast that with the experimental results showing (1) much greater concentrations of dopants in HfO$_2$ than is possible under thermodynamic equilibrium and (2) the formation of phases other than monoclinic, such as amorphous structures and higher-permittivity tetragonal or cubic phase of HfO$_2$. Given that these oxides are typically deposited at room temperature and annealed at temperatures no higher than 1000 °C, it is likely that compositionally metastable structures are being produced. As the familiar examples of glass and diamond show, however, metastability of a structure does not preclude its usefulness, provided that the barriers to decomposition or structural transformation are sufficiently large to prevent the structure from transforming over the lifetime of the device in which it is used.

First principles calculations provide tools for exploring the relative stability of different structures and for calculating the dielectric constants of these structures. The dielectric constants of the tetragonal and cubic phases of HfO$_2$ were...
found to be higher than that of the monoclinic phase\textsuperscript{15–17} providing a natural explanation of how the formation of these phases by ionic substitution in HfO\textsubscript{2} could raise the permittivity. On the other hand, the issues of tetragonal and cubic phase metastability makes it worthwhile to explore whether the permittivity can be increased within the monoclinic phase, for example, by substituting more polarizable ions for Hf.

This work uses first principles calculations to address (1) whether ionic substitution in HfO\textsubscript{2} can make the tetragonal or cubic phase of HfO\textsubscript{2} stable relative to the monoclinic phase, or whether the monoclinic phase remains the most stable, (2) the relative importance of ionic polarizability, local structure, and global symmetry on the dielectric permittivity of HfO\textsubscript{2} with ionic substitutions, and (3) whether the substitution of ions into HfO\textsubscript{2} produces infrared or Raman active phonons whose characteristic frequencies could be experimentally detected. For simplicity, this work focuses on substitutions that do not change the total number of atoms, namely Si, Ti, and Zr substitution for Hf, and the substitution of a Ta–N pair for a Hf–O pair.

II. METHODS

Density-functional theory (DFT) electronic structure calculations for total energies, force constants, and Born effective charges were performed using the Vienna \textit{ab initio} simulation package (VASP).\textsuperscript{18,19} A plane wave basis set was used for electronic wave functions. Projector augmented wave (PAW) pseudopotentials were used for Hf, O, and the substitutional ions.\textsuperscript{20,21} The Hf, Ta, Zr, and Ti PAW pseudopotentials included semicore $p$ states as valence electrons. The local density approximation (LDA) was used for the exchange-correlation functional. The electronic contribution to the dielectric response $\kappa_{\text{elec}}$ was calculated using the DFT package ABINIT,\textsuperscript{22} with Hartwigsen–Goedecker–Hutter pseudopotentials,\textsuperscript{23} and the LDA.

Calculations were performed for various 12, 24, 48, and 96 atom cells or supercells of HfO\textsubscript{2} (Fig. 3) containing one substitution or pair substitution for the case of Ta–N. The dopant concentration is given by $x$, yielding the chemical formulae Hf\textsubscript{1−$x$}M\textsubscript{$x$}O\textsubscript{2} for single ion substitution M, and Hf\textsubscript{1−$x$}Ta\textsubscript{$x$}O\textsubscript{2−$x$}N\textsubscript{$x$} for Ta (+N) substitution. Full details of the calculations are given in Ref. 24. The calculations were performed at two levels of convergence: relaxations to find (meta)stable structures were performed using a plane wave cutoff energy of 353 eV, an augmentation charge cutoff energy of 1500 eV, and a Monkhorst Pack grid equivalent to a $6 \times 6 \times 6$ grid on a primitive 12-atom HfO\textsubscript{2} cell. Calculations of phonon frequencies and ionic effective charges were done via the frozen phonon method,\textsuperscript{25} with a 248 eV plane wave cutoff energy, 1050 eV augmentation charge cutoff energy, and a Monkhorst Pack grid equivalent to a $2 \times 2 \times 2$ grid on a primitive HfO\textsubscript{2} cell.

The small cutoff energy for the phonon and effective charge calculations was a necessary tradeoff between speed and accuracy, given the large number of atoms and low symmetry of the largest monoclinic cells. The convergence errors for the lower cutoff energy calculations were tested for pure HfO\textsubscript{2} and determined to be only $\pm 5 \text{ cm}^{-1}$ for phonon frequencies, $\pm 0.01$ for effective charges, and $\pm 0.05$ for $\kappa_{\text{elec}}$ while the lower precision calculations were about 40 times faster than the higher precision ones.

III. RESULTS

A. Relative stability of phases

For each structure and each substitution, the energies of the cubic, tetragonal, and monoclinic phases were calculated

<table>
<thead>
<tr>
<th>Substitution</th>
<th>$x$</th>
<th>Symm.</th>
<th>$\Delta V$ (Å$^3$)</th>
<th>Coordination</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Pure HfO\textsubscript{2})</td>
<td>0</td>
<td>$m$</td>
<td>0</td>
<td>7</td>
</tr>
<tr>
<td>Si</td>
<td>0.03125</td>
<td>$m$</td>
<td>−6.10</td>
<td>6</td>
</tr>
<tr>
<td>Si</td>
<td>0.25</td>
<td>$c$</td>
<td>−5.31</td>
<td>4</td>
</tr>
<tr>
<td>Ti</td>
<td>0.03125</td>
<td>$m$</td>
<td>−4.71</td>
<td>7</td>
</tr>
<tr>
<td>Ti</td>
<td>0.25</td>
<td>$m$</td>
<td>−4.70</td>
<td>7</td>
</tr>
<tr>
<td>Zr</td>
<td>0.03125</td>
<td>$m$</td>
<td>+1.84</td>
<td>7</td>
</tr>
<tr>
<td>Zr</td>
<td>0.25</td>
<td>$m$</td>
<td>+1.64</td>
<td>7</td>
</tr>
<tr>
<td>(Ta+N)</td>
<td>0.03125</td>
<td>$m$</td>
<td>−0.82</td>
<td>7</td>
</tr>
<tr>
<td>(Ta+N)</td>
<td>0.25</td>
<td>$m$</td>
<td>−1.32</td>
<td>7</td>
</tr>
<tr>
<td>(Pure TaON)</td>
<td>1.00</td>
<td>$m$</td>
<td>−7.22</td>
<td>7</td>
</tr>
</tbody>
</table>

TABLE II. Crystalline properties of HfO\textsubscript{2} with various atomic substitutions. Only lowest-energy phase is shown for the given substitution and concentration $x$. Symmetry is symmetry of the parent HfO\textsubscript{2} phase. $m$=monoclinic and $c$=cubic. $\Delta V$ is the change in volume relative to the parent HfO\textsubscript{2} structure. Coordination is number of anions in the nearest neighbor shell of the substitutional cation.

![Figure 3](http://jap.aip.org/jap/copyright.jsp)
at various compositions. A HfO$_2$ supercell was created for each phase, the appropriate ionic substitutions were made, and the structure relaxed. All symmetries are described in terms of the parent HfO$_2$ phase, although the ionic substitution lowers the symmetry in many cases.

For the simultaneous substitution of a Ta–N pair for a Hf–O pair, many distinct configurations are possible depending upon the distance between the Ta and the N. Figure 4 shows the relative energy of the monoclinic structure as a function of the Ta–N distance. The energy is lowest if N occupies one of the four fourfold O positions nearest to the Ta. The lowest energy is found for N occupying the closest fourfold site. In the remainder of this work, N always replaces the fourfold oxygen closest to Ta.

With Si substitution in the cubic phase, the energy of the system is reduced if four of the neighbors arranged in a tetrahedron moved inward to a distance of 0.160 nm and the other four moved away (see Fig. 5). While tetrahedral oxygen coordination is familiar for Si, similar symmetry breaking, to a lesser degree, lowers the energy for all substitutions tested, except Ta (+N). Remarkably, even the energy of HfO$_2$ itself is lowered relative to the high symmetry cubic structure of Fig. 1 under the distortion of Fig. 5. The tetragonal and distorted cubic structures are related. Phonon analysis of the cubic HfO$_2$ structure of Fig. 1 shows a triplet instability. Freezing one component of this instability gives the tetragonal structure of Fig. 1(b) with a select axis $c$. Freezing a particular superposition of all three components leads to the distorted cubic structure of Fig. 5. For HfO$_2$, the ordering of the energies for the system studied, from lowest to highest, is monoclinic, tetragonal, distorted cubic, and high-symmetry cubic. The monoclinic, tetragonal, and high-symmetry cubic phases are in the same order as expected from experiment. Unlike the high-symmetry cubic structure, the tetragonal and distorted cubic structures are metastable, i.e., while they are not ground state structures, normal mode analysis shows that all of their modes are stable.

At sufficiently high concentrations, substitution of small Si or Ti cations stabilizes the distorted cubic structure with respect to the tetragonal one. Because of the complicated competition between cubic, distorted cubic, and tetragonal phases upon ionic substitution, this work reports only the energy differences between the monoclinic phase and the lowest-energy nonmonoclinic phase found as a function of composition. As shown in Fig. 6, ionic substitution lowers the gap in energy between the monoclinic and nonmonoclinic structure of Fig. 1(b) with a select axis $c$. Freezing a particular superposition of all three components leads to the distorted cubic structure of Fig. 5. For HfO$_2$, the ordering of the energies for the system studied, from lowest to highest, is monoclinic, tetragonal, distorted cubic, and high-symmetry cubic. The monoclinic, tetragonal, and high-symmetry cubic phases are in the same order as expected from experiment. Unlike the high-symmetry cubic structure, the tetragonal and distorted cubic structures are metastable, i.e., while they are not ground state structures, normal mode analysis shows that all of their modes are stable.
clinic phases for all substitutions studied. Only for Si substitution above about 20%, however, is the lowest nonmonoclinic phase actually stabilized relative to the monoclinic phase. As these results involve the competition between phases of significantly different volume, significant quantitative errors are possible due to the local density approximation. Nonetheless, it is concluded that most experimental studies where ionic substitution produces the tetragonal or cubic phase have either formed a structurally metastable phase or else the nonmonoclinic phase is stabilized by some other factor such as epitaxial strain.

B. Electronic and dielectric properties

Table III lists the LDA band gap, average squared Born effective charge $Z_e^* \bar{Z}_e^2$, total static dielectric constant $\kappa_s$, and the electronic and ionic contributions to $\kappa_s$, $\kappa_s = \kappa_{elec} + \kappa_{ion}$. The scalar dielectric constant $\kappa_s$ is defined as $\kappa_s = 1/3 \text{ Tr } \kappa_s$, where $\kappa_s$ is the full dielectric tensor. The average squared Born effective charge is defined as the invariant $\bar{Z}_e^2 = 1/(3N) \text{ Tr } [(\mathbf{Z}_e^*)^T \mathbf{Z}_e^*]$, where $\mathbf{Z}_e^*$ is the Born effective charge tensor for ion $i$ and the sum runs over the $N$ ions of the unit cell. The results are presented for all of the atomic substitutions at concentrations $x=0.03125$ and $x=0.25$, as well as for pure TaON. $\kappa_{ion}$ is related to the phonon properties and Born effective charges of the ions. The relationship is expressed here in the simplified form

$$\kappa_s = \kappa_{elec} + \frac{Z_e^2}{VC},$$

where $V$ is the volume per ion and $C$ is proportional to the average force constant in the structure weighted appropriately.

Consider first the effects of small dopant concentration. Substitution of Zr for Hf has very little effect, which is not surprising, given the chemical similarities between Zr and Hf. The other ions studied are less similar to Hf, and can be arranged, in order of increasing polarizability, as Si, Hf, Ti, and Ta. The relative polarizabilities of the different ions are consistent with the results in Table III. As the polarizability increases, $\kappa_{elec}$ and $\bar{Z}_e^2$ increase. Nonetheless, the total $\kappa_s$ is increased at $x=0.03125$ whether Si, Ti, or Ta (+N) are substituted. From Eq. (1), it can be concluded that the addition of Si to HfO$_2$ decreases the volume and softens the lattice enough to more than make up for its smaller polarizability.

More significant changes in $\kappa_s$ occur when the dopant concentration is higher. The highest $\kappa_s$ is predicted for monoclinic HfO$_2$ upon ionic substitution and relaxation.

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**TABLE III.** Electronic and dielectric properties of HfO$_2$ with various atomic substitutions. In some cases, the components of $\kappa_s$ do not appear to correctly add due to roundoff error.

<table>
<thead>
<tr>
<th>Substitution</th>
<th>$x$</th>
<th>LDA band gap (eV)</th>
<th>$\bar{Z}_e^2$</th>
<th>$\kappa_{elec}$</th>
<th>$\kappa_{ion}$</th>
<th>$\kappa_s$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pure HfO$_2$</td>
<td>0</td>
<td>4.04</td>
<td>13.68</td>
<td>4.9</td>
<td>11.6</td>
<td>16.5</td>
</tr>
<tr>
<td>Si</td>
<td>0.03125</td>
<td>4.01</td>
<td>13.48</td>
<td>4.9</td>
<td>12.2</td>
<td>17.1</td>
</tr>
<tr>
<td>Si</td>
<td>0.25</td>
<td>4.38</td>
<td>12.11</td>
<td>4.8</td>
<td>13.7</td>
<td>18.6</td>
</tr>
<tr>
<td>Ti</td>
<td>0.03125</td>
<td>3.08</td>
<td>13.75</td>
<td>5.0</td>
<td>11.9</td>
<td>16.9</td>
</tr>
<tr>
<td>Ti</td>
<td>0.25</td>
<td>2.90</td>
<td>14.35</td>
<td>5.2</td>
<td>14.2</td>
<td>19.5</td>
</tr>
<tr>
<td>Zr</td>
<td>0.03125</td>
<td>3.00</td>
<td>13.70</td>
<td>4.9</td>
<td>11.6</td>
<td>16.5</td>
</tr>
<tr>
<td>Zr</td>
<td>0.25</td>
<td>3.83</td>
<td>13.94</td>
<td>5.0</td>
<td>11.6</td>
<td>16.5</td>
</tr>
<tr>
<td>Ta(+N)</td>
<td>0.03125</td>
<td>3.69</td>
<td>13.92</td>
<td>5.1</td>
<td>11.8</td>
<td>16.9</td>
</tr>
<tr>
<td>Ta(+N)</td>
<td>0.25</td>
<td>2.95</td>
<td>15.92</td>
<td>5.6</td>
<td>13.5</td>
<td>19.1</td>
</tr>
<tr>
<td>Pure TaON</td>
<td>1.00</td>
<td>3.01</td>
<td>22.25</td>
<td>8.3</td>
<td>16.4</td>
<td>24.8</td>
</tr>
</tbody>
</table>
The highest valence band states in HfO\(_2\) are inherently lowered by the electronic states of the substituents. For certain ionic substitutions, the band gap is of a gate dielectric is detrimental to maintaining sufficient gap. For example, the experimental band gap\(^{27}\) for HfO\(_2\) is 5.7 eV, versus the calculated value of 4.0 eV in Table III. Nonetheless, one expects the clinic phase of HfO\(_2\). The band gap decreases as the Si–O bonding states lie well below the valence band maximum and Si–O antibonding states lie well above the conduction band minimum.

![Figure 7](image)

**FIG. 7.** Local density approximation band gap vs \(\kappa_s\) for HfO\(_2\) and HfO\(_2\) with atomic substitutions. All structures on and below the trendline are based on the monoclinic HfO\(_2\) structure, while those above are based on the tetragonal or cubic HfO\(_2\) structure. Solid symbols represent configurations that are structurally stable. Open symbols are calculated to be metastable with respect to a structural transformation to the monoclinic structure.

The one structure of Table III that increases both the dielectric constant and the band gap relative to HfO\(_2\) is Hf\(_{0.75}\)Si\(_{0.25}\)O\(_2\). This structure differs from the others in that it is cubic, not monoclinic. To better understand how the change in phase from monoclinic to higher symmetry affects the dielectric properties of HfO\(_2\)-based systems, additional calculations were performed on the higher-symmetry polymorphs of HfO\(_2\). The results are shown in Table IV. The calculated increase in \(\kappa_s\) from monoclinic to cubic to tetragonal agrees with previous reports,\(^{15,17}\) as does the finding the the permittivity of tetragonal HfO\(_2\) is smallest along the c axis. In addition, results are presented for HfO2 with a 12 atom unit cell and the distorted cubic structure shown in Fig. 5. The calculated dielectric constant of this phase is intermediate between that of the cubic and tetragonal phases. Table IV shows that increasing the symmetry of HfO\(_2\) increases the band gap, lowers the average Born effective charge, and has little effect on \(\kappa_{\text{elec}}\). From Eq. (1), the enhancement of \(\kappa_s\) must thus be due to a softer lattice.

These results support the typical experimental observation that the enhancement of dielectric constant of HfO\(_2\) with the addition of dopants is due to the formation of the tetragonal or cubic phase. Tomida, Kita, and Toriumi\(^{9}\) (TKT) shows clear x-ray diffraction evidence for the formation of a tetragonal phase in Hf\(_{1-x}\)Si\(_x\)O\(_2\), 0.04 < \(x\) < 0.10, and a maximum dielectric constant \(\kappa_s \approx 27.\) This presents a puzzle, as first principles total energy calculations show that Hf\(_{1-x}\)Si\(_x\)O\(_2\) at \(x=0.0625\) should transform from the tetragonal to four-coordinated cubic phase with no energy barrier. This discrepancy could be resolved if the the distribution of Si is not isotropic. Therefore, dielectric calculations were performed on Hf\(_{1-x}\)Si\(_x\)O\(_2\) at \(x=0.0625\) with the nonisotropic distribution of Si-rich layers alternating with Hf-only layers shown in Fig. 3(c). The results (Table IV) show (1) that the metastable nonmonoclinic structure has tetragonal symmetry (calculated \(c/a=1.009\) versus calculated \(c/a=1.016\) for tetragonal HfO\(_2\)) and (2) that its calculated dielectric constant 30 is in very good agreement with the TKT experimental result. Such layered structures with alternating Hf-rich and Hf-poor planes are expected when the experimental procedure consists of the alternating atomic layer deposition of HfO\(_2\) and other metal oxides.\(^{1}\)

In calculating \(\kappa_{\text{ion}}\), the phonon properties were determined for all of the structures studied. The infrared spectra were calculated and Raman spectra estimated as described in Ref. 24. For the most part, the results show only subtle changes in the spectra when ions are substituted within the monoclinic HfO\(_2\) phase. The spectra become very different when the symmetry becomes tetragonal or monoclinic. In one case, an additional peak is predicted, in Hf\(_{1-x}\)Ta\(_x\)O\(_2\), where x =

### Table IV. Structural, electronic, and dielectric properties of metastable HfO\(_2\) phases and anisotropic metastable Hf\(_{0.637}\)Si\(_{0.363}\)O\(_2\).

<table>
<thead>
<tr>
<th>Substitution</th>
<th>(x)</th>
<th>Symm.</th>
<th>Coordination</th>
<th>LDA band gap (eV)</th>
<th>(Z^2)</th>
<th>(\kappa_{\text{elec}})</th>
<th>(\kappa_{\text{ion}})</th>
<th>(\kappa_s)</th>
<th>((\kappa_s)_{xx})</th>
<th>((\kappa_s)_{zz})</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Pure HfO(_2))</td>
<td>0</td>
<td>c</td>
<td>8</td>
<td>4.06</td>
<td>15.22</td>
<td>4.9</td>
<td>22.0</td>
<td>26.9</td>
<td>10.5</td>
<td>14.4</td>
</tr>
<tr>
<td>(Pure HfO(_2))</td>
<td>0</td>
<td>c</td>
<td>4+4</td>
<td>4.46</td>
<td>14.49</td>
<td>5.0</td>
<td>24.8</td>
<td>29.8</td>
<td>6.0</td>
<td>7.2</td>
</tr>
<tr>
<td>(Pure HfO(_2))</td>
<td>0</td>
<td>t</td>
<td>4+4</td>
<td>4.72</td>
<td>14.37</td>
<td>5.0</td>
<td>34.9</td>
<td>39.9</td>
<td>50.6</td>
<td>54.5</td>
</tr>
<tr>
<td>Si</td>
<td>0.0625</td>
<td>t</td>
<td>4</td>
<td>4.30</td>
<td>13.69</td>
<td>5.0</td>
<td>25.1</td>
<td>30.1</td>
<td>34.0</td>
<td>37.2</td>
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IV. CONCLUSIONS

To enhance the dielectric constant of HfO$_2$ by ionic substitution without significantly decreasing the band gap, the cubic or tetragonal phase must be formed. Of the ionic substitutions studied here, Si is the most intriguing as it is the only one case found where a sufficiently large dopant concentration ($x > 0.2$) is calculated to stabilize a nonmonoclinic phase relative to the monoclinic phase. Otherwise, the nonmonoclinic phases of HfO$_2$ with atomic substitutions reported experimentally are conjectured to be (1) metastable with respect to the monoclinic phase but with an energy barrier to transformation, (2) stabilized by extrinsic effects such as epitaxial strain or grain boundaries, or (3) stabilized by a configuration of deposited atoms that has a more extreme alternation between Hf-rich and Hf-poor regions than was studied in this work.

The same caveats about structural metastability apply to compositional metastability. As noted in Table I, the intrinsic solubility of many metal oxides into the monoclinic HfO$_2$ structure is very small. This does not mean that structurally and/or compositionally metastable structures cannot be made, or that they are useless, but they must satisfy the requirement of not transforming or decomposing over the lifetime of any device in which they are used. The factors that influence the relative stability of these “higher-$\kappa$” phase are a worthwhile area for further research.

13Phase Equilibria Diagrams Database v.3.1.0, NIST SRD 31 (The American Ceramic Society, Westerville, OH, 2005).
19Certain commercial software is identified in this paper to adequately describe the methodology used. Such identification does not imply recommendation or endorsement by the National Institute of Standards and Technology, nor does it imply that the software identified is necessarily the best available for the purpose.
33P. Duran, Ceramurgia Int. 1, 10 (1975).