Dimensional evolution of spin correlations in the magnetic pyrochlore Yb$_2$Ti$_2$O$_7$


1Department of Physics and Astronomy, McMaster University, Hamilton, Ontario, L8S 4M1, Canada
2Department of Physics and Astronomy and Guelph-Waterloo Physics Institute, University of Waterloo, Waterloo, ON, N2L 3G1, Canada
3Institute for Quantum Computing, University of Waterloo, Waterloo, ON, N2L 3G1, Canada
4Materials Research Division, Risø DTU, Technical University of Denmark, DK-4000 Roskilde, Denmark
5Nano-Science Center, Niels Bohr Institute, University of Copenhagen, DK-2100 Köbenhavn, Denmark
6Laboratory for Neutron Scattering, Paul Scherrer Institut, 5232 Villigen PSI, Switzerland
7Indiana University, 2401 Milo B. Sampson Lane, Bloomington, Indiana 47408, USA
8National Institute of Standards and Technology, 100 Bureau Drive, MS 6102, Gaithersburg, Maryland 20899-6102, USA
9Dept. of Materials Science and Engineering, University of Maryland, College Park, Maryland 20742
10Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA
11Spallation Neutron Source, Experimental Facilities Division, Oak Ridge National Laboratory, P.O. Box 2008, Oak Ridge, Tennessee 37831, USA
12Brockhouse Institute for Materials Research, McMaster University, Hamilton, Ontario, L8S 4M1, Canada
13Canadian Institute for Advanced Research, 180 Dundas St. W., Toronto, Ontario, MSG 1Z8, Canada

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The pyrochlore material Yb$_2$Ti$_2$O$_7$ displays unexpected quasi-two-dimensional (2D) magnetic correlations within a cubic lattice environment at low temperatures, before entering an exotic disordered ground state below $T = 265$ mK. We report neutron scattering measurements of the thermal evolution of the 2D spin correlations in space and time. Short-range three-dimensional (3D) spin correlations develop below 400 mK, accompanied by a suppression in the quasielastic (QE) scattering below $\sim 0.2$ meV. These show a slowly fluctuating ground state with spins correlated over short distances within a kagome-triangular-kagome (KTK) stack along [111], which evolves to isolated kagome spin stars at higher temperatures. Furthermore, low-temperature specific heat results indicate a sample dependence to the putative transition temperature that is bounded by 265 mK, which we discuss in the context of recent mean field theoretical analysis.

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I. INTRODUCTION

The corner-sharing tetrahedral geometry of the pyrochlore lattice favors strong geometric frustration, wherein a competition of exchange interactions between localized magnetic moments results directly from their arrangement within the lattice. This phenomenon tends to suppress transitions to magnetic long-range order (LRO), leaving in their place unusual short-range magnetic correlations at low temperatures. The form of such correlations varies between frustrated systems, with ground states typically determined by subleading terms in the relevant Hamiltonian, such as dipole interactions, further neighbor exchange, and structural distortions within the underlying crystal lattice.\cite{1,2} The rare-earth titanate series of materials, which have the chemical formula R$_2$Ti$_2$O$_7$ with R being a trivalent magnetic rare-earth ion, crystallize into the face-centered-cubic (fcc) space group Fd$\overline{3}$m, which characterizes the pyrochlore lattice. This series provides excellent examples of the variety of exotic ground states that can emerge in nearly identical chemical environments when geometric frustration is at play. Several of the rare-earth titanates exhibit disordered ground states that persist down to 30 mK, namely, the spin ices Dy$_2$Ti$_2$O$_7$ and Ho$_2$Ti$_2$O$_7$\cite{5,5} and the enigmatic spin liquid Tb$_2$Ti$_2$O$_7$\cite{6,7}. Others in the series do order magnetically, such as Gd$_2$Ti$_2$O$_7$\cite{8,10} and Er$_2$Ti$_2$O$_7$\cite{11,12}, but the nature of the ordering is unusual in both cases. In all of these cases, the source of the frustration (or lack thereof) is well understood in terms of the spin interactions and the single-ion anisotropy imposed by the crystal electric field. In particular, the spin ices combine effective ferromagnetic (FM) exchange with strong Ising-like anisotropy, such that the moments are constrained to point into or out of each tetrahedron.

Yb$_2$Ti$_2$O$_7$ provides an intriguing contrast to the spin ices. It is known to combine FM exchange ($\theta_{\text{CW}} \sim 600$ to $800$ mK\cite{13,14}) with XY anisotropy.\cite{15-18} The continuous degree of freedom provided by the XY anisotropy leads one to naively expect an ordered FM ground state. However, despite what appears to be a transition near 200 mK,\cite{15,19,20} most experimental evidence suggests that Yb$_2$Ti$_2$O$_7$ displays a disordered ground state down to 30 mK in zero magnetic field.\cite{15,19} Application of a modest magnetic field along [110] at 30 mK induces a transition to a polarized, ordered phase with well defined spin-wave excitations.\cite{21} Using anisotropic exchange Hamiltonians, recent theoretical studies have sought to understand the spin-wave dispersions in the magnetic-field-induced ordered state\cite{22} as well as the diffuse scattering at relatively high temperatures in zero field\cite{23} and the local spin susceptibility.\cite{17,24} Interestingly, some of these studies indicate that the dominant exchange interaction is the Ising component, which may explain the lack of simple FM behavior in Yb$_2$Ti$_2$O$_7$, making it an exchange analog to the spin ices.\cite{17,22}

An early heat capacity ($C_p$) measurement showed an anomaly at $T = 214$ mK, indicating a possible phase transition, in addition to a broad Schottky-like hump at 2 K.\cite{19} The putative transition, whose temperature varies somewhat...
in the literature and which we henceforth label $T_c$, has previously been explored through several techniques. Much of this characterization is consistent with the absence of conventional LRO below $T_c$, although single-crystal neutron diffraction and ac susceptibility results presented in Ref. 26, suggest a collinear FM ground state. Hodges et al. found a discontinuous change in the spin fluctuation frequency at $T_c = 240$ mK as measured by Mössbauer and $\mu$SR, along with an absence of magnetic Bragg peaks in neutron powder diffraction. The specific heat of the sample used in Ref. 15 was found to display a sharp anomaly at 250 mK, close to the observed first-order drop in the spin fluctuation rate. Single-crystal neutron scattering studies revealed a pattern of diffuse scattering, which is present both above and below $T_c$, but a qualitative difference was observed between 500 and 30 mK that indicated short-range 3D spin correlations at the lowest temperatures. The observed change was that the rod of scattering became more strongly peaked near the (111) zone center, moving from a featureless rod at 500 mK to a rod with structure at 30 mK. The conventional interpretation of a flat rod of scattering in any diffraction pattern is the presence of 2D correlations. Though the rod of scattering is flat at 500 mK, this interpretation is striking in the present case, as it implies a magnetic decomposition of the 3D pyrochlore structure into a stacking of alternating kagome and triangular planes along the (111) directions, with a characteristic QE energy scale of 0.3 meV. This diffuse scattering, which indicates short-range spin correlations, is present both above and below $T_c$, but a qualitative difference was observed between 500 and 30 mK that indicated short-range 3D spin correlations at the lowest temperatures. The observed change was that the rod of scattering became more strongly peaked near the (111) zone center, moving from a featureless rod at 500 mK to a rod with structure at 30 mK. The conventional interpretation of a flat rod of scattering in any diffraction pattern is the presence of 2D correlations. Though the rod of scattering is flat at 500 mK, this interpretation is striking in the present case, as it implies a magnetic decomposition of the 3D pyrochlore structure into a stacking of alternating kagome and triangular planes along the (111) directions, breaking the underlying cubic symmetry.

It should be noted that in Ref. 23, where exchange parameters were extracted by fitting a modified measurement of the diffuse scattering pattern in the HHL plane at 1.4 K, the real-space spin correlations derived from these parameters were reported to show a more nuanced anisotropic behavior. However, their calculated spin correlation functions do display some decoupling of the kagome planes with pronounced correlations along near neighbor [110] directions.

The nature of the transition near 200 mK, and the resulting ground state of Yb$_2$Ti$_2$O$_7$ remains a matter of debate. Most of the experimental studies indicate a disordered ground state. This is supported by a recent theoretical study that makes use of the measured high-field spin-wave spectrum to determine microscopic exchange parameters. The parameters are highly anisotropic, favoring a local (111) exchange. From a mean-field perspective, these parameters predict an ordered ferromagnetic state below 3.2 K. The real-space spin correlations derived from these parameters were reported to show a more nuanced anisotropic behavior. However, their calculated spin correlation functions do display some decoupling of the kagome planes with pronounced correlations along near neighbor [110] directions.

The specific heat measurements were performed on this and one other crystal prepared under identical conditions. The starting material for these growths, a pressed polycrystalline sample, was prepared by mixing Yb$_2$O$_3$ and TiO$_2$ in stoichiometric ratio and annealing at 1200 °C for 24 hours, with a warming and cooling rate of 100 °C/h. The specific heat of this polycrystalline material was measured for comparison to the single crystals.

The single-crystal time-of-flight neutron scattering measurements were carried out using the Disk Chopper Spectrometer (DCS) at the National Institute of Standards and Technology (NIST), with 5-Å incident neutrons, giving an energy resolution of 0.09 meV. Triple-axis neutron scattering experiments were also performed at NIST, using SPINS. For the triple-axis measurements, a pyrolytic graphite (PG) monochromator provided an incident energy of 5 meV, and an energy resolution $\delta E$ of approximately 0.25 meV. Elastically scattered neutrons were selected using five flat PG analyzer blades. Due to the aforementioned energy resolution, the nominal elastic scattering in fact integrates over much of the quasielastic component of the diffuse scattering located in Ref. 21. A cooled Be filter was used to remove higher-order wavelengths from the scattered beam, and was followed by an 80-inch radial collimator.

A neutron powder diffraction experiment was performed on two samples of Yb$_2$Ti$_2$O$_7$, using the Neutron Powder Diffractometer (NPDF) instrument at the Lujan Neutron Scattering Center. One sample studied was a polycrystalline material for these growths, a pressed polycrystalline sample, prepared by mixing Yb$_2$O$_3$ and TiO$_2$ in stoichiometric ratio and annealing at 1200 °C for 24 hours, with a warming and cooling rate of 100 °C/h. The specific heat of this polycrystalline material was measured for comparison to the single crystals.
the single-crystal neutron experiments. Both samples were subsequently crushed using a Fritsch Pulverisette 2 mortar grinder for 20 minutes per sample.

The heat capacity measurements were performed using the quasiadiabatic method (see Ref. 31 for details) with a 1-kΩ RuO2 thermometer and 10-kΩ heater mounted directly on the thermally isolated sample. A weak thermal link to the mixing chamber of a dilution refrigerator was made using Pt-W (92% Pt, 8% W) wire for the smaller single-crystal piece, A (142.3 mg) and polycrystalline sample (24.37 mg), and yellow brass foil for the 7.0515 g crystal, B, used in the neutron scattering experiments. The time constant of relaxation provided by the weak link was several hours, much longer than the internal relaxation time of the samples, minimizing thermal gradients and ensuring that the sample cooled slowly into an equilibrium state. The addenda contributed less than 0.1% to the specific heat of the system.

III. RESULTS

A. Diffuse magnetic neutron scattering

Figure 1(a) shows the temperature dependence of the intensity of elastically scattered neutrons at two Q points using SPINS. One point is near the fcc zone center and structurally allowed (111) Bragg peak (Q_{1.07} = [1.07, 1.07, 1.07]), while the other is near the fcc Brillouin zone boundary (Q_{1.54} = [1.54, 1.54, 1.54]). Figure 1(b) locates these two points relative to the rod of diffuse scattering along [111] and the Brillouin zone boundaries, using reciprocal space maps of the elastic scattering at 30 and 500 mK measured with DCS. These two intensities track each other at relatively high temperatures, but they separate below ~400 mK, with the scattering near the zone center (at Q_{1.07}) growing more strongly before leveling off at the lowest temperatures. The inset of Fig. 1(a) shows the difference between the elastic intensities at Q_{1.07} and at Q_{1.54}, and this resembles conventional order-parameter behavior with a phase transition near 400 mK.

![FIG. 1. (Color online) (a) The temperature dependence of neutron scattering intensity at two Q points that lie on the rod of scattering, Q_{1.54} (red crosses) and Q_{1.07} (blue circles) (10 K background subtracted). Bottom inset: the difference of intensities, I_{1.07} – I_{1.54}, with the solid line as a guide to the eye. (b) Elastic time-of-flight neutron scattering data at 30 and 500 mK (reproduced from Ref. 21). Error bars represent ±1σ.](image1)

![FIG. 2. (Color online) (a) (10 K background subtracted) Longitudinal rod scans at T = 60 and 300 mK. Data points at 540 mK are consistent with a Q dependence that follows the Yb^{3+} magnetic form factor (black solid line). (b) Examples of transverse scans across the rod, centered at Q_{1.07} and Q_{1.54}. The insets show the positions of the scans in reciprocal space.](image2)

A longitudinal scan of the elastic scattering along the rod (i.e., along the [H,H,H] direction) shows that the low-temperature buildup of intensity occurs near the (111), but not (222), zone center [see Fig. 2(a)]. Below 400 mK, the scattering peaks up near (111) and the the Q dependence of the longitudinal scattering can be fit to an Ornstein-Zernike (Lorentzian) form, from which an interplane, or “longitudinal,” correlation length ξ_L can be determined. We find ξ_L = 3.2 Å at 60 mK, implying correlated spins over ~6.4 Å in the [111] direction. This indicates that even at the lowest temperatures, 3D correlations do not extend beyond a KTK stack, whose spatial extent is 5.8 Å. Above 400 mK, this interplane correlation vanishes, leaving the Yb^{3+} form factor as the only contribution to the Q dependence of the diffuse scattering along [111] as expected for truly 2D spin correlations.

The scattering normal to the rod probes spin correlations within the kagome and triangular planes. Figure 2(b) shows scans across the rods centered on Q_{1.07} and Q_{1.54}. Representative scans at T = 60 and 540 mK are shown. These data sets were fit to Lorentzian lineshapes, allowing the transverse correlation length and integrated area of the scattering to be determined as a function of temperature. The resolution widths appropriate to the spectrometer are shown as the horizontal bars in Fig. 2(b), and are negligibly small compared to the FWHM of the rod scattering. The results of the Lorentzian fits are plotted in Figs. 3(a) and 3(b). The integrated areas at the two Q positions differ only for $T < 400$ mK [see Fig. 3(b)] consistent with the behavior of the peak intensities along the rod shown in Fig. 1(a).

Meanwhile, the FWHM [see Fig. 3(a)], which is inversely related to the transverse correlation length $\xi_T$, does not depend on the longitudinal position along the rod at any temperature.
Fig. 3. (Color online) (a) Full width at half maxima (FWHM) and (b) integrated area extracted from the Lorentzian fits to the transverse scans shown in Fig. 2(a). (c) The range of $\xi_T$ within the kagome layer. Above 400 mK (black), the correlations are restricted to a single kagome star unit. Below 265 mK (blue), the transverse correlations grow only to encompass the next-near neighbors in the kagome layer. (d) The pyrochlore lattice decomposed into kagome and interleaved triangular layers. Below 400 mK, the longitudinal correlations extend only between a single KTK unit.

Below 265 mK, $\xi_T$ is constant at 9.6 Å and it decreases to 7.8 Å above 400 mK, leaving a correlated area corresponding roughly to one kagome “star,” which has a diameter of 15.4 Å. Combined with $\xi_L \sim 0$ above 400 mK, we conclude that for $T > \Theta_{CW}$, the spin system is characterized by uncorrelated kagome stars. Figure 3(c) summarizes the size of the spin-correlated regions in the kagome planes both below 265 mK and above 400 mK. In the ground state, which stabilizes below 265 mK, short 3D spin correlations form along [111], encompassing a single KTK stack of width $\sim 6$ Å, as illustrated by the blue region in Fig. 3(d).

B. Quasielastic neutron scattering

Inelastic magnetic scattering can inform on the dynamics associated with this exotic disordered zero-field ground state. Time-of-flight neutron scattering data are shown in Fig. 4 at both 30 and 500 mK, and at positions both along the [111] rod of scattering and well removed from the rod of scattering. These positions are located in the reciprocal space map of the elastic scattering shown in the Fig. 4 inset. Consistent with earlier work, this shows that for $T > \Theta_{CW}$, the spin system is characterized by uncorrelated kagome stars. Figure 3(c) summarizes the size of the spin-correlated regions in the kagome planes both below 265 mK and above 400 mK. In the ground state, which stabilizes below 265 mK, short 3D spin correlations form along [111], encompassing a single KTK stack of width $\sim 6$ Å, as illustrated by the blue region in Fig. 3(d).

Fig. 4. (Color online) Energy dependence of the diffuse scattering above and below $T_c$, both on and off the rod of scattering. Thick lines are guides to the eye. INSET: range of binning for the on- and off-rod positions. On-rod: $\text{HHH} = [1.2, 1.6]$, $\text{HH-2H} = [0.3, 0.5]$. Off-rod: $\text{HHH} = [1.2, 1.6]$, $\text{HH-2H} = [0.3, 0.5]$.

Below 265 mK, the diffuse scattering. Thus, the data in Fig. 3(c) at 30 mK and 5 T serve as a measure of the background.

Comparison of the of zero-field quasielastic diffuse scattering to the nonmagnetic background revealed in a magnetic field of 5T makes it clear that although diffuse scattering is organized into rods of scattering along [111], there is appreciable diffuse, inelastic scattering throughout the Brillouin zone. This “off-rod” scattering has a relatively flat energy dependence out to 0.6 meV. Furthermore, unlike the rod diffuse scattering along [111], the “off-rod” diffuse scattering shows no temperature dependence between 500 and 30 mK. This implies that a dynamic and essentially uncorrelated component of the spins persists in the zero-field ground state. A similar situation is encountered in the classical spin ice $\text{Ho}_2\text{Ti}_2\text{O}_7$, which retains appreciable elastic diffuse scattering throughout the Brillouin zone at very low temperatures, indicating static zero-field spin correlations that encapsulate at most a single tetrahedron.

C. Specific heat

The specific heat provides insight into the extent to which the entropy changes at temperatures relevant to the diffuse scattering. Figure 5 shows specific heat results of poly- and single-crystalline samples, including the sample from the neutron scattering study. There is significant sample dependence of the low-temperature $C_p$ anomaly, with at least one feature occurring between 150 and 265 mK in all samples. The sharpest anomaly is observed in our powder sample, at a temperature that seems to be the upper limit for all others, $T = 265$ mK. Significantly, our powder $C_p$ peak is sharper by an order of magnitude, and occurs at a higher temperature than both the original powder $C_p$ data by Blöte et al. as well as the powder $C_p$ data by Dalmas de Réotier et al., which displays an anomaly at 250 mK with a peak height of $\sim 9 \text{ J/K mol Yb}$. The neutron scattering sample B exhibits a sharp peak at 265 mK, but also has a broad feature as seen in sample A.
FIG. 5. (Color online) Examples of low-temperature specific heat in Yb$_2$Ti$_2$O$_7$. Significant sample dependence is observed in both powders and single crystals. The powder sample prepared at McMaster University shows the highest temperature (265 mK) and sharpest anomaly. The neutron scattering sample, B, shows a sharp peak at 265 mK similar to the powder, and a broad, low-temperature feature similar to crystal A. None of the samples studied had any feature at 400 mK.

The specific heat does not show any indication of a feature at 400 mK. This indicates that the buildup of 3D correlations, as well as the small increase in transverse correlation length, produces, at most, subtle changes in the entropy. This could be another manifestation of the persistently short correlation lengths at all temperatures. However, an important question remains: what is the physical significance of the $C_p$ features at 265 and 200 mK observed in the neutron scattering crystal? Drawing on the large change in spin fluctuation frequency observed by Hodges et al. at 240 mK in their powder sample, we should expect a change in dynamics at these temperatures. As discussed in relation to Fig. 4, we do observe a change in dynamics between 500 and 30 mK but the intermediate temperature regime awaits further study.

D. Structural information

To investigate structural differences between the single crystals as grown by the method described in Sec. II, and the polycrystalline material, which was used as the starting material for these growths (the “sintered powder”), we turn to neutron powder diffraction results. After a successful growth, a single crystal was crushed back into polycrystalline form in order to facilitate direct comparison to the sintered powder. Drawing on the large change in spin fluctuation frequency observed by Hodges et al. at 240 mK in their powder sample, we should expect a change in dynamics at these temperatures. As discussed in relation to Fig. 4, we do observe a change in dynamics between 500 and 30 mK but the intermediate temperature regime awaits further study.

FIG. 6. (Color online) Neutron diffraction data from two samples of Yb$_2$Ti$_2$O$_7$ taken at 250 K: a sintered powder (top) and a crushed single crystal (bottom). The result of Rietveld analysis, using a fully ordered model for Yb$_2$Ti$_2$O$_7$, is shown in red. The difference between the measured and calculated profiles is in black. The data are normalized to the incident time-of-flight spectrum, and corrected for detector efficiency using a vanadium normalization. A Rietveld refinement was performed on both patterns using a fully ordered model of the pyrochlore structure (see, for example, Ref. 33 for details of this structure). The results indicate that both the powder and crushed crystal are described extremely well by the fully ordered model, with $R_p$ values of 2.16% and 2.83%, respectively. Some differences can be observed between the two samples, namely, that the crushed crystal has a larger lattice parameter $a_{\text{crystal}} = 10.02006(2)$ compared to $a_{\text{powder}} = 10.01322(1)$ as well as greater widths of the Bragg peaks, indicating lattice strain. Site substitution between Yb$^{3+}$ and Ti$^{4+}$ was found not to be important for either sample (refinement gives less than 1% substitution in both cases). A detailed, temperature-dependent Rietveld refinement as well as pair distribution function analysis is forthcoming, but these preliminary results already indicate that there are only subtle structural differences between the two forms of Yb$_2$Ti$_2$O$_7$, pointing to random disorder or lattice strain as the root cause for the differences in specific heat.

IV. CONCLUSIONS

In summary, we have explored, using diffuse and inelastic neutron scattering, the transformation of spin correlations as Yb$_2$Ti$_2$O$_7$ enters its exotic ground state at zero field. Within this ground state, we observe slow, short-range 3D correlated fluctuations that extend over single KTK stacks. In contrast, at temperatures characteristic of $\Theta_{\text{CW}}$ and above, the system is comprised of decoupled kagome stars, with 2D spin correlations confined to single kagome units. The temperature $T^* \approx 400$ mK at which correlations lose their 3D nature and also shrink in the 2D kagome plane is found to be much higher than any of the temperatures $T_c < 265$ mK marking anomalies in $C_p$. Random structural disorder or lattice strain may account for the variability in $T_c$ and the sharpness of the associated anomalies, but would seem unlikely to be the factor capping the extremely short range of correlations in the ground state. Both $T^* \approx 400$ mK and the highest $T_c = 265$ mK observed are
an order of magnitude smaller than the predicted mean-field transition temperature, 3.2 K. It is clear that the transition to the exotic ground state, whether this be characterized by $T_c$ and/or $T^*$, is strongly suppressed by geometrical frustration, quantum fluctuations, or both.

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