Single bead detection with an NMR microcapillary probe

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We have developed a nuclear magnetic resonance (NMR) microcapillary probe for the detection of single magnetic microbeads. The geometry of the probe has been optimized so that the signal from the background water has a similar magnitude compared to the signal from the dephased water nearby a single magnetic bead within the probe detector coil. In addition, the RF field of the coil must be uniform within the effective range of the magnetic bead. Three different RF probes were tested in a 7 T (300 MHz) pulsed NMR spectrometer with sample volumes ranging from 5 nL down to 1 nL. The 1 nL probe had a single-shot signal-to-noise ratio (SNR) for pure water of 27 and a volume resolution that exhibits a 600-fold improvement over a conventional (5 mm tube) NMR probe with a sample volume of 18 μL. This allowed for the detection of a 1 μm magnetite/polystyrene bead (m = 2 × 10^-14 A m^2) with an estimated experimental SNR of 30. Simulations of the NMR spectra for the different coil geometries and positions of the bead within the coil were developed that include the B_0 shift near a single bead, the inhomogeneity of the coils, the local coil sensitivity, the skin effect of the coil conductor, and quantitated estimates of the proximity effect between coil windings.

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1. Introduction

Iron oxide particles have a strong effect on the transverse relaxation time (T_2) of nearby water protons and thus are useful as magnetic resonance imaging (MRI) contrast agents [1]. Single cell [2] and single magnetic particle detection [3] have been demonstrated via MRI, but quantitative measurements are limited by the image voxel dimensions and the precise location of the particle within the voxel. Microcoil NMR spectroscopy has the potential to further characterize the details of the NMR signature of isolated magnetic particles in water, but improving upon state-of-the-art probe designs is necessary.

Sillerud et al. have shown that concentrations as low as 10 beads/nL of 1 μm magnetic beads can be detected by 1H NMR at 1 T in a 264 nL sample [4] by measuring frequency shifts and line broadening. Single particle detection, on the other hand, requires a specialized NMR probe, one capable of detecting the difference between background water and water within the range of influence of the bead. In this paper, we present an NMR probe for single bead detection that is based on the pioneering work of Olson et al. [5]. We numerically analyze the magnetic field around a single bead to estimate the volume of water affected by a single bead as well as the distribution of the B_0 field within that volume. The RF uniformity as a function of the number of turns of the microcoil is calculated to determine an optimum configuration. Simulated NMR spectra for the different RF coil geometries and bead positions are also calculated. Three different probes were fabricated and tested with sample volumes ranging from 5 nL down to 1 nL.

2. Probe design

The NMR spectrometer signal-to-noise ratio (SNR) is fundamentally limited by the RF coil characteristics. Hoult and Richards report a general expression for SNR [6], and Peck et al. have adopted it specifically for microcoil NMR [7], finding that:

\[
SNR = K \frac{\gamma I}{h N} \left( \frac{I}{I_0} \right) \left( \frac{k_b V_{sample}}{V_{noise}} \right).
\]

Here
K = N \gamma h^2 I / (I_0 + 3/2 k_b T_s),
where N is the spin density, γ is the gyromagnetic ratio, h is reduced Planck’s constant, I is spin quantum number, k_b is Boltzmann’s constant, T_s is temperature of sample, and k_0 is a scaling constant to account for the RF inhomogeneity of the B_1 field. V_{noise} is the electrical noise associated with the NMR detection circuit, which is mainly the Johnson noise of the RF coil. V_{noise} = √(4k_b T_s R A), where T_s is the temperature of the coil and R is its resistance, and A is the measurement spectral bandwidth. More importantly, we see that the SNR is proportional to the sample volume, V_{sample}. For single bead detection, V_{sample} is...
separated into two volumes: the background fluid volume, $V_{\text{back}}$, and the volume of the fluid affected by a single bead, $V_{\text{aff}}$. When $V_{\text{aff}}$ is relatively small compared to $V_{\text{back}}$, the spectrum shape is dominated by the background signal. Furthermore, by definition, if $V_{\text{aff}}$ is smaller than $V_{\text{sample}}$, the NMR signal from $V_{\text{aff}}$ will be buried in the noise. In short, $V_{\text{sample}}/\text{SNR}$ determines the detection limit volume for an SNR = 1. To maximize the NMR signal for single bead detection, we need to increase the RF strength per unit current ($i$).

We estimate the magnetic moment of a uniformly magnetized 1 µm diameter polystyrene bead to be $m = 2.3 \times 10^{-14} \text{ A m}^2$, based on a saturation magnetization of $4.3 \times 10^4 \text{ A m}^{-1}$, as provided by the manufacturer. Given these values, the $\Delta B_0$ field contours near the bead can be determined by calculation. The results are shown in Fig. 1. They define the effective range of a bead for significant shifts in the proton Larmor frequency within the bandwidth of the spectrometer. Shifts of at least 10 Hz are observed within a 50 µm region surrounding the bead; shifts of at least 1 Hz are observed within a 120 µm region; and shifts of at least 0.1 Hz are within a 250 µm region.

To investigate the influence of $V_{\text{sample}}$ on the NMR spectrum, we calculated the magnetic field at each grid point (grid size is $0.5 \times 0.5 \times 0.5 \mu m$) and generated a histogram of the number of volume elements as a function of $\Delta B_0$ within the capillary. The histograms are shown in Fig. 2. Note that the sample volume is defined by the capillary ID, and the effective length of the coil ($l_s$) ranging from 100 µm to 1000 µm along the axis of the capillary, which correspond to $V_{\text{sample}}$ ranges from 0.5 nL to 5 nL. Due to the orientation of the capillary (transverse to $B_0$), the effect of the negative $B_0$ shift region (as shown in Fig. 2) will dominate the NMR spectra. The influence of the bead on the NMR spectrum as it passes through the coil can be increased by changing either the capillary ID or the magnetic moment of the particle. In particular we have used the 0.1 Hz shift (hatched region shown in Fig. 2) as a primary design criterion for optimizing the coil geometry. The spread in $\Delta B_0$ is most obvious for the $l_s = 100 \mu m$, with a corresponding peak shift to $-0.5$ Hz and significant broadening. The peak height becomes 4% of that of the $\Delta B_0$ distribution for pure water because the large frequency shift of water protons in the neighborhood of a bead causes significant line broadening. The $\Delta B_0$ distribution for $l_s = 100 \mu m$ had a 12-fold higher peak than that for $l_s = 100 \mu m$, as well as a peak shift of $-0.1$ Hz and broadening. Note that the $\Delta B_0$ distribution for the $l_s = 200 \mu m$ is virtually the same as the $l_s = 100 \mu m$ outside of the frequency range of $-0.1$ Hz to $-0.7$ Hz. However, there are significantly more spins inside this range for the $l_s = 200 \mu m$ sample owing to additional spins.
Note the following: (1) the each discrete disk volume, from the sample after a 90° pulse, will dominate the histogram. The histogram for the largest sample volume (I = 1000 μm) shows a narrow ΔB0 distribution indicating that the majority of spins in the sample remained unaffected by the bead, as expected. For comparison, the ΔB0 distribution without beads for the I = 100 μm is also shown in Fig. 2d.

The minimum detectable sample volume is determined by the probe SNR limitations, as discussed above. However, since one of the goals of this research is to develop new methods for quantitative measurements of the magnetic moment of single bead, it is important to have a large enough Vsample to capture the details of the ΔB0 distribution. According to this analysis, we estimate the minimum Vsample required to realistically detect a single bead to be 1 nL. In this case, the signal strength is large and the spectrum broadening can be detected. This leads to the conclusion that the NMR RF coil must have a small sample volume, but the volume must also be large enough to cover the effective range of a single magnetic bead for better SNR.

The skin effect of the coil conductor and the proximity effect between the coils make it difficult to calculate the detailed characteristics of the RF coils [7,8]. For this reason we developed an FEM analysis for the B1 inhomogeneity which includes both skin effects and proximity effects for different coil lengths. The FEM analysis was based on a two-dimensional, axis symmetric model at 300 MHz. B1 inhomogeneity plots for 4-, 8-, and 17-turn RF coils, corresponding to l of 240, 490, and 1100 μm and Vsample of 1, 2, and 5 nL within the coil region, are shown in Fig. 3. RF uniformity on the x-axis is given B1(x)/B1(0), where B1(x) is the B1 field produced by the RF coil along the x-axis and B1(0) is the B1 field at the center of the coil. Smallers coils have less RF uniformity. However, B1 distribution in the transverse direction is relatively homogenous in the sample region. In this case the B1 homogeneity of the sample region is determined by the RF uniformity on the x-axis direction. With the 4-turn coil, the B0 distortion range of the bead in the sample volume mostly fits into the 10% error range. With the 8-turn coil, the B0 distortion range is covered in the 5% error range. With the 17-turn coil, the B0 distortion range is fully covered in the 1% error range for the B1 uniformity. Other coil characteristics such as resistance of the coil and RF resistance i as well as the proximity effect is used to determine the coil sensitivity

Based on the calculations described above, we can numerically simulate NMR spectra by convolving the ΔB0 histograms and the natural proton line spectrum with B1 uniformity of coils as follows:

\[
S_{\text{NMR}} = \frac{L(f)}{\text{noise}} \delta_{\text{RF}}(V),
\]

where \(L(f)\) is a natural proton line spectrum given as a Lorentzian function, \(\delta_{\text{RF}}(V)\) is a ΔB0 shift distribution of the induced NMR signal from the sample after a 90° pulse given as a delta function. We divided a sample region into a series of disks, \(V_{\text{disk}} = S_i(x_{i+1} - x_i)\) along the x-axis, where \(S_i\) is the cross section of the sample. Assuming that the RF homogeneity in transverse direction \(B_1(x_i)\) is constant within each discrete disk volume, \(\delta_{\text{RF}}(V)\) is given by:

\[
\delta_{\text{RF}}(V) = \sum_{i=0}^{\text{num of disks}} \left\{ \delta(V_{\text{disk}}) \phi(x_i) \sin\left( \theta + \frac{\pi}{2} \frac{B_1(x_i)}{B_1(0)} \right) \right\}
\]

\(\delta(V_{\text{disk}})\) is the ΔB0 shift distribution of unit sample volume of \(V_{\text{disk}}\) given as delta function, and \(\phi(x_i)\) is the magnetic flux which penetrates the RF coil induced by a magnetic dipole \(\mu\) at the point \(x_i\). Note the following: (1) \(\phi(x) \propto B_1(x)\) by reciprocity, and

\[
\text{SNR} = \frac{S_{\text{NMR}}}{\text{noise}}
\]

\(\text{SNR}\) is the signal-to-noise ratio, and the noise is the natural proton line spectrum with a Lorentzian function.

**Fig. 3.** RF homogeneity based on FEM analysis for the different coil geometries at 300 MHz: (a) 4-turn coil, (b) 8-turn coil and (c) 17-turn coil. Contour lines show a ±2% error in B1 uniformity from the center of the RF coil. The circle in the center shows an estimated bead effective range diameter of 100–200 μm. The broken line shows the sample volume defined by a 75 μm ID capillary. Due to the cylindrical symmetry of the problem, a number of loop coils (diameter of 420 μm with 50 μm conductor) were used assuming a continuous multi-turn coil. The horizontal axis in the center is the symmetric axis. (d) RF homogeneity along the axis. Solid lines show inside of the coil regions and broken lines show outside of the coil regions.
more than 150 μm from the end of the coil would be excited. (3) A generic scaling constant \( k_0 \) has been used in the past to consider the effect of RF inhomogeneities on the NMR response of microcoil probes. However, if we know the RF inhomogeneity, the observable sample volume \( V_{\text{obs}} = k_0 V_{\text{sample}} \) is given by:

\[
v_{\text{obs}} = \int \left( \frac{S}{\sqrt{2}} \frac{B_1(x)}{B_1(0)} \sin \left( \theta + \frac{\pi B_1(x)}{2 B_1(0)} \right) \right) dx.
\]

The theoretical estimates of coil SNR and \( v_{\text{obs}} \) are shown in Fig. 4. The \( B_1 \) inhomogeneity of the coils, the local coil sensitivity, and the coil resistance including both skin effect and proximity effects have been used in the SNR calculation as discussed above.

Simulated NMR spectra are shown in Fig. 5. With a 17-turn coil, the peak height difference with and without beads is only 10%, and it is difficult to see the effect of a bead from the spectrum. With a 4-turn coil, the peak height drops by 25%, and the peak width increases to 0.9 Hz from 0.7 Hz and the peak shifts to -0.1 Hz. Peak reduction is an indication of the volume of affected spins, and the peak broadening is a measure of the \( \Delta B_0 \) distribution within that volume. In principle, these parameters can be used to determine the magnetic moment of the bead. The direction of the peak shift indicates the majority of the \( \Delta B_0 \) distribution within that volume is either positive or negative. Note that peak shift alone would not be a good way to estimate the effect of the magnetic moment of the bead. A larger RF coil has better SNR, however smaller RF coils have a smaller \( V_{\text{eff}}/V_{\text{sample}} \) ratio, and therefore are more sensitive to the influence of a single bead. Note that, one may think that a 1- or 2-turn coil having a high \( V_{\text{eff}}/V_{\text{sample}} \) ratio would be better for single bead detection, but the low SNR makes the detection limit volume smaller as shown in Fig. 4. Therefore one needs to select the proper number of RF coil turns to be from 3- to 15-turns, given the effective range of magnetic bead.

Moreover, the bead position in the sample region influences the NMR spectra, especially for smaller coils. The simulated NMR spectra for a 4-turn RF coil as a function of bead position along the \( x \)-, \( y \)-, and \( z \)-axis is shown in Fig. 6. In the transverse direction, the bead position has a small effect on the NMR spectra, except for the peak shift. Along the \( z \)-axis, peak shift reduces to 0. At this point the \( \Delta B_0 \) distribution polarity in the sample region moves from the negative side to the neutral. In contrast, the inhomogeneity of the RF field along \( x \)-axis causes significant spectral changes as a function of bead position.

3. Experimental setup

We fabricated three different NMR microfluidic capillary probes for use in a commercial pulsed NMR spectrometer operating at 7 T (300 MHz). The microcoil NMR probe design is based on that described by Olson et al. [5] with modifications based on the FEM results described above. A detailed schematic of the probe assembly is shown in Fig. 7. 17-, 8- and 4-turn coils were made from 50 μm diameter copper wire with varnish insulation. Microcoils were
to become lodged in the sample capillary. To reduce lary''. In this way, the coil capillary could be reused if debris were magnetic chip capacitors were also placed on the PCB to both tune to reduce the susceptibility effects of the PCB fiber epoxy. Non-(PCB), modified to eliminate as much material as possible in order Characteristics of the NMR probe.

Table 1

<table>
<thead>
<tr>
<th>Coil turns</th>
<th>Coil length</th>
<th>Sample volume ( (v_{\text{sample}}) )</th>
<th>Observable sample volume ( (v_{\text{obs}}) )</th>
<th>SNR</th>
<th>Detection limit ( (nL) (v_{\text{obs}}) (\text{SNR}) )</th>
<th>Spectrum resolution</th>
</tr>
</thead>
<tbody>
<tr>
<td>17-turn</td>
<td>1100 μm</td>
<td>4.8 nL</td>
<td>4.7 nL</td>
<td>71</td>
<td>0.07</td>
<td>0.7 Hz</td>
</tr>
<tr>
<td>8-turn</td>
<td>490 μm</td>
<td>2.2 nL</td>
<td>2.4 nL</td>
<td>38</td>
<td>0.06</td>
<td>0.7 Hz</td>
</tr>
<tr>
<td>4-turn</td>
<td>240 μm</td>
<td>1.1 nL</td>
<td>1.6 nL</td>
<td>27</td>
<td>0.06</td>
<td>0.6 Hz</td>
</tr>
<tr>
<td>5 mm NMR with 2 mm capillary</td>
<td>–</td>
<td>18 μL</td>
<td>18 μL</td>
<td>480</td>
<td>38</td>
<td>0.7 Hz</td>
</tr>
</tbody>
</table>

Sample solutions consisted of 1 μm polystyrene beads with embedded iron oxide nanoparticles (26% iron by weight) dispersed in water [9]. To achieve a concentration of a single bead per coil volume, the stock solution was diluted with deionized water to \( 3 \times 10^9 \) beads/mL or 1 bead per 30 nL. Bead concentrations were experimentally verified with an optical hemocytometer after dilution.

4. Measurements

All experiments were conducted at 7.05 T \( (f_0 = 300.18 \text{ MHz}) \). Each probe was shimmmed in situ with the shim coils of the spectrometer. Experiments were performed on pure de-ionized (DI) water without flow and on bead solutions. The water measurements were used to determine the baseline SNR and spectrum resolution. We also compared the characteristics of the microcoil probes with a conventional 5 mm commercial probe and a 2 mm sample tube. The spectral width for pure DI water samples was between 0.6 Hz and 0.7 Hz for all of the coils tested. Occasionally, we observed effects brought on by the susceptibility mismatches in the multilayered capillary geometry that made it difficult to reproduce spectral line widths of 0.6 Hz for pure water. For this reason, shimming target values were set to 1 Hz for practical use.

Measurements on bead solutions were made in the following way. First, we stepped the motor of the syringe pump one step (1.4 nL), then waited 60 s for the flow rate to decrease to 10 pL/s, corresponding to a bead velocity of 2 μm/s. We then measured the free induction decay (FID) four times. The 90° pulse widths were between 19 μs and 23 μs. Each FID measurement took 16.5 s (5 \( T_1 \) for pure water). The measurement sequence is shown in Fig. 8. It was difficult to predict when a bead would pass into the sample region of the probe, so we repeated this sequence as individual beads would occasionally enter the coil region of the capillary. We found that repeating the sequence 100 times was sufficient to see the signals from several beads as they passed though the coil. As a control and to check the stability of the experiment, DI water was measured with the same sequence in advance. During the sample flow experiments, measurements were stable. We could not see the effect of pumping or flow induced line broadening. A D2O lock was not used. The drift rate was less than 6.6 mHz/s \( (0.14 \text{ nT/s}) \), which was acceptable for the 15 s FID measurement period. Peak shift measurements were renormalized between each FID measurement to accommodate field drift.

5. Results

The SNR and the spectral resolution for pure DI water are shown in Table 1 for different coil geometries. The SNR for the microcoils was 6–14% of that of the conventional 5 mm tube NMR probe with a much larger sample volume. However the detection limit volume improved more than 600-fold for the 4-turn microcoil probe, compared to the 5 mm commercial probe.

We would observe a series of momentary anomalous spectra as a single bead moved through the coil during the flow experiments. The line shape of the anomalous spectra varied, which is to be

![Image](https://via.placeholder.com/150)
expected depending on the position of the bead within the NMR coil. A peak that was more than 2% lower than that for DI water was considered a signal for the presence of a bead in the coil. Sometimes the spectrum would become fixed after several FID measurements. We think this was due to a single bead sticking to the inner wall of the capillary. NMR spectra from three different probes are shown in Fig. 9. The presence of a bead in the coil lowered the peak height, broadened the peak, and shifted it to lower frequency. With the 17-turn coil, only the first 85 signals were analyzed. After 85 pulse sequences, a bead lodged in the capillary as discussed above. A total of 17 of 85 sequences indicated the transition of a bead through the coil. A representative spectrum in Fig. 9a shows only a 7% lower spectrum peak and detecting the differences between spectra, with and without a bead, was difficult. With the 8-turn coil, 74 of 400 signals indicated the transition of a bead. A representative spectrum in Fig. 9b shows a peak reduction of 34% and a peak broadening ranging from 1 Hz to 1.8 Hz. With the 4-turn coil, again a bead lodged in the capillary after 116 signals, of which 19 signals indicated the transition of a bead. A representative spectrum in Fig. 9c shows a 50% peak reduction, peak broadening ranging from 1 Hz to 2.2 Hz, and a shift of −0.2 Hz. In this case $T_1$ was reduced by two thirds from 320 ms to 140 ms.

6. Discussion

Experimentally we observed that the effect of a bead in a coil is substantially larger than expected based on our simulations. The magnetization of the bead would have to be four-times larger than our original estimate given the experimentally observed peak height reduction, and 20-times larger given the observed spectral broadening. The discrepancies between the experimental and simulated results may be due to several factors. These possibility that there is a residual inhomogeneity of the $B_0$ field even after the shimming procedure before making measurements. The simulations for the NMR spectra over estimates the peak height if the residual $B_0$ inhomogeneity is not accounted for. Thus, the effect of the beads would be less than what would be measured experimentally. Water diffusion may also be important in that the relaxation of spins in an inhomogeneous magnetic field [10] has to be considered. The field gradients near a magnetic bead are large and cause significant non-uniform dephasing of the protons as they pass nearby, which results in spectrum additional broadening. Finally, in our comparisons between theory and experiment we have assumed the bead is located at the center of the coil. The position of the bead within the coil gives rise to different $\Delta B_0$ distributions within the sample volume (as shown in Fig. 6) and so the challenge would be to precisely determine the position of the bead as it travels through the coil for quantitative estimates of the magnetic moment of the bead. At these small scales the flow through the capillary is laminar, so we at least know that its trajectory follows a line parallel to the axis of the coil. A series of spectra taken as the particle traverses the coil could therefore be used to uniquely determine its magnetic moment and position as a function of time.

7. Summary

We have developed a microcapillary NMR probe for detection of a single magnetic bead. The RF coil geometry was optimized to focus on a “limited-volume” sample that cuts off the background signal. The detection limit volume was enhanced 600-fold compared to a conventional 5 mm NMR probe. With the improved sensitivity we were able to measure significant changes in the NMR proton spectrum as a single magnetic bead passed through the coil. Simulations of the NMR spectra for different coil geometries were developed in order to find the optimum probe geometry for detection a single bead with a given magnetic moment. The simulations included calculations of the $B_0$ shift near a single bead, the $B_0$ inhomogeneity of the coil, the local coil sensitivity, the skin effect of the coil conductor, and quantitate estimates of the proximity effect between coil windings. The models are useful for probe design for single beads detection but are not as of yet adequate for quantitate measurements of the magnetic moment of a single bead.
Future work will focus on development of new pulse sequences and measurement protocols including gradients to detect the position of the beads in the coil. We plan to also develop more accurate models that include microscopic diffusion effects near the beads. Our goals include using microcoil probes to determine particle aggregation, the distribution of properties such as size and magnetic moments of particles within an ensemble, as well as provide deeper understanding of the relaxation mechanisms of surrounding water protons [11].

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References


[9] Dynabeads MyOne SYLANE. Any mention of commercial products does not imply recommendation or endorsement by NIST.
