Phase-specific Raman analysis of $n$-alkane melting by moving-window two-dimensional correlation spectroscopy

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We use moving-window two-dimensional correlation spectroscopy (MW-2DCOS) for phase-specific Raman analysis of the $n$-alkane ($C_{21}H_{44}$) during melting from the crystalline solid phase to the intermediate rotator phase and to the amorphous molten phase. In MW-2DCOS, individual peak-to-peak correlation analysis within a small subset of spectra provides both temperature-resolved and spectrally disentangled Raman assignments conducive to understanding phase-specific molecular interactions and chain configurations. We demonstrate that autocorrelation MW-2DCOS can determine the phase transition temperatures with a higher resolving power than commonly used analysis methods including individual peak intensity analysis or principal component analysis.

Besides the enhanced temperature resolving power, we demonstrate that asynchronous 2DCOS near the orthorhombic-to-rotator transition temperature can spectrally resolve the two overlapping peaks embedded in the Raman CH$_2$ twisting band in the orthorhombic phase, which had been only predicted but not observed because of thermal broadening near the melting temperature. Published 2016. This article is a U.S. Government work and is in the public domain in the USA.

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Introduction

Understanding temperature-dependent structures of saturated linear hydrocarbons or $n$-alkanes is important for improving their petrochemical applications for oils, lubricants, and fuels, and for elucidating the hierarchical morphology of more complex materials, such as polyethylene (PE) and lipid bilayers.[1,2] In general, long carbon chain alkanes have an orthorhombic crystalline phase below the melting temperature and a randomly oriented amorphous phase above the melting temperature. Interestingly, previous X-ray and Raman studies show that some $n$-alkanes (20 $\leq n $ $\leq$ 37) can have mobile intermediate phases between the crystalline phase and the amorphous phase.[3,4] The intermediate phases are called rotator phases, where predominantly trans chains can rotate along the chain axis and are packed in the hexagonal lattice with long range order.[5]

Raman spectroscopy is widely used to characterize the phases of $n$-alkanes and PE by measuring vibration frequencies affected by short-range interchain interactions and chain conformations (trans vs gauche). Raman bands of the amorphous phase are characterized by relatively broad bandwidths because of disordered chain conformation and high gauche concentration. On the other hand, both the orthorhombic crystalline phase and the rotator phases are rich in trans conformation, together called the consecutive trans phase.[6] exhibiting relatively narrow Raman bandwidths. At the molecular length scale, the crystalline phase supports two different types of interchain interactions in the orthorhombic unit cell while the rotator phases have only one type in the hexagonal unit cell. The two types of interchain interactions in the orthorhombic phase can cause splitting in some Raman bands. For example, the CH$_2$ bending mode appears as a single peak at 1438 cm$^{-1}$ in the rotator phase but becomes split in the orthorhombic phase as much as by 25 cm$^{-1}$.[7] One of the split peaks, at 1417 cm$^{-1}$, is used as a metric to determine the mass fraction of the orthorhombic conformation.[7,8] For most other Raman bands, however, the crystal-field splitting in the orthorhombic phase is smaller than the Raman bandwidth at room temperature; therefore, the peak splitting has been observed only at extreme conditions, such as at liquid nitrogen temperature.[9,10] or from single crystals.[11] Such subtle spectral changes are challenging for conventional fitting-based individual peak analysis to decipher. In this work, we demonstrate that moving-window two-dimensional correlation spectroscopy (MW-2DCOS) analysis can unravel peak splitting from temperature-dependent Raman spectra measured near the melting temperature.

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The 2DCOS method is a versatile, qualitative analysis tool that has been used to analyze the effect of a perturbation, such as temperature, pressure, concentration, pH, and time, on the spectral response.\textsuperscript{13,14} 2DCOS is based on pair-wise (bivariante) analysis, which can be compared with univariate individual peak analysis and multivariate analysis (MVA). The individual peak analysis can provide more intuitive links between spectral changes and perturbation but is very limited in sensitivity specifically in crowded spectral regions. On the other hand, MVA, which considers intensity variation of a large number of spectral components, is able to detect and quantify spectral changes as a function of perturbation. However, MVA is limited in providing direct correlation of individual peaks with the variable perturbation. 2DCOS provides both direct spectral correlation with specific perturbation and resolving power to detect subtle spectral changes and overlapping peaks. Additionally, the in-phase and out-of-phase correlation spectral maps generated by 2DCOS elucidate the direction and sequence of spectral changes between pairs of spectral components over a perturbation range.\textsuperscript{13,14} In some cases, spectral changes occur over a narrow perturbation range; thus, it may be more useful to limit 2DCOS to this specific range in order to identify the relevant spectral features, which can be examined by moving-window 2DCOS (MW-2DCOS). In the MW-2DCOS analysis, a small subset or window of spectra is scanned over the whole perturbation range while analyzed by 2DCOS. This MW-2DCOS method has been previously demonstrated to determine phase transition temperature and the associated spectral features.\textsuperscript{15–18}

In this paper, we analyze a series of temperature-dependent Raman spectra of melting \( n\text{-C}_{21}\text{H}_{44} \). We use various methods to analyze the data including fitting-based peak intensities, principal component analysis, simple 2DCOS over a wide temperature range, and MW-2DCOS with a narrow temperature window. We demonstrate that the autocorrelation spectra of MW-2DCOS can determine the transition temperatures (orthorhombic-to-rotator and rotator-to-amorphous) with the highest resolving power among the demonstrated analysis methods. Temperature dependences of peak positions and widths of several Raman bands confirm that the intermediate, rotator phase influences the Raman modes differently from the crystalline and the amorphous phases. Furthermore, our comparative analysis of asynchronous correlation maps of the \( \text{CH}_2 \) twisting mode indicates that the consecutive trans Raman band exists as two overlapping peaks in the orthorhombic phase but as a single peak in the rotator phase.

**Experimental section**

**Sample preparation**

Heneicosane (\( n\text{-C}_{21}\text{H}_{44} \)) was purchased from Sigma Aldrich (\( \geq 99.5\% \)) and used without purification. The original alkane flakes were broken into smaller pieces in order to generate a homogeneous scattering volume for Raman measurement and then loaded into a shear cell (Linkam Scientific Instruments, CSS 450) with quartz disks. The sample was compressed into a thickness of 1 mm. The shear cell provided optical access to the sample at a controlled temperature.

**Raman spectroscopy**

Raman spectra were measured with a triple grating Raman spectrometer (Horiba, T64000; spectral resolution = 0.8 cm\(^{-1}\)) in the 180° backscattering geometry. Linearely polarized light from a HeNe laser (632.8 nm) was focused into a spot with an approximately 60-\( \mu \)m diameter, and an average power of 15 mW. The sample was heated from 28 °C to 45 °C. Three consecutive Raman spectra were recorded and averaged at each temperature 2 min after the sample was equilibrated. It took approximately 3 min to acquire each spectrum for a scanning range of 950 cm\(^{-1}\) to 1550 cm\(^{-1}\), and 9 min for three spectra at each temperature. Between 30 °C and 42 °C, Raman spectra were measured with an increment of 1 °C. Raman spectra at 28 °C and 45 °C were found to be indistinguishable from those at 30 °C and 42 °C, respectively; therefore, when needed for MW-2DCOS, Raman spectra at 29 °C, 43 °C, and 44 °C were generated by interpolation with the neighboring, almost identical spectra. All spectra were detrended by a splined baseline subtraction method with zeros at four frequencies (950 cm\(^{-1}\), 1240 cm\(^{-1}\), 1350 cm\(^{-1}\), and 1550 cm\(^{-1}\)). To compensate irregular scattering, the baseline-detrended spectra were normalized by the area of the \( \text{CH}_2 \) twisting band (1240 cm\(^{-1}\) to 1350 cm\(^{-1}\)).\textsuperscript{7,8}

**Principle component analysis (PCA)**

PCA was performed with a commercial multivariate analysis package (Solo + MIA, Eigenvector Research, Inc). The intensity-scaled Raman spectra were mean-centered before performing PCA.

**Two-dimensional correlation spectroscopy (2DCOS)**

All 2DCOS analyses, including MW-2DCOS, were performed with the “2D Shige” software, which was developed by Shigeaki Morita (Kwansei Gakuin University).

**Results and discussion**

Figure 1a shows selected Raman spectra acquired from \( n\text{-C}_{21}\text{H}_{44} \) while it was heated from 28 °C to 45 °C. Migler et al.\textsuperscript{8} analyzed peak intensities of several Raman bands representing the orthorhombic, consecutive trans, and amorphous phases of alkane and PE by fitting with Lorentzian functions. Similarly, Fig. 1b shows plots of the integrated area of the fitted peaks centered at 1417 cm\(^{-1}\), 1295 cm\(^{-1}\), and 1300 cm\(^{-1}\). The 1417 cm\(^{-1}\) peak results from the crystal field splitting of the \( \text{CH}_2 \) bending mode only in the orthorhombic crystalline phase and disappears in the rotator phase. The \( \text{CH}_2 \) twisting mode exists as a narrow peak at 1295 cm\(^{-1}\) in the consecutive trans conformation (from the orthorhombic and rotator phases) and becomes a broad peak at 1300 cm\(^{-1}\) in the amorphous phase. Later in the paper, we discuss fitting results of the consecutive trans peak at 1295 cm\(^{-1}\) with a pseudo-Voigt function, which does not change the peak intensity plot shown in Fig. 1b. In Fig. 1b, the consecutive trans peak decreases very gradually as the amorphous peak at 1301 cm\(^{-1}\) increases from 34 °C to 42 °C. In contrast, the orthorhombic peak at 1417 cm\(^{-1}\) disappears sharply at 33 °C, exhibiting a sharp transition from the orthorhombic crystalline phase to the rotator phase.\textsuperscript{8} This type of individual peak intensity analysis can provide explicit information of phase transitions when distinctive bands can be unambiguously associated with each phase. However, when bands are embedded in spectrally crowded regions, individual peak intensities become unreliable because of difficulty in separating the relative contributions of neighboring peaks. Also, for complex systems where multiple molecular conformations coexist, such as PE, it is not trivial to track subtle spectral changes of individual bands by fitting the overlapping peaks during phase transitions.
Multivariate analysis methods have been widely used to detect subtle changes over the multiple spectral components. Principal component analysis (PCA) is one of the simplest MVA methods that finds orthogonal spectral components (called loadings) and their relative amplitudes (called scores) with the orders of principal components determined from the highest variance. The plot of PCA scores as a function of temperature in Fig. 2a shows two distinctive components determined from the highest variance. The plot of PCA loading spectra of 13 Raman spectra of n-C21H44 shows the directionality of intensity changes of the two frequency components of ν1 and ν2. Positive φ(ν1,ν2) indicates that the two components change in the same direction while negative φ(ν1,ν2) indicates the opposite direction. On the other hand, the asynchronous correlation, ψ(ν1,ν2), represents the sequential order of intensity changes of the ν1 and the ν2 components. The sequence can be determined by considering both φ(ν1,ν2) and ψ(ν1,ν2) according to a general rule, proposed by Noda.\[12\] When φ(ν1,ν2) and ψ(ν1,ν2) are the same sign, the ν1 changes earlier than the ν2. When φ(ν1,ν2) and ψ(ν1,ν2) are the opposite sign, the ν1 changes later than the ν2. The 2DCOS maps can be useful not only to determine the sequential order of spectral changes but also to enhance spectral resolution by spreading highly overlapped peaks along a second orthogonal dimension.\[19,20\]

Figure 3 shows the 2D synchronous and asynchronous correlation maps of 13 Raman spectra of n-C21H44 measured between 30 °C and 42 °C, which covers the rotator phase and parts of orthorhombic and amorphous phases. Among the cross correlation pairs, we examine those between the 1417 cm\(^{-1}\) band (from the orthorhombic phase) and six other bands in (1040 to 1200) cm\(^{-1}\) regions. First, the consecutive trans conformation bands at 1062 cm\(^{-1}\), 1133 cm\(^{-1}\), 1170 cm\(^{-1}\), and 1295 cm\(^{-1}\), show positive φ(ν1,ν2), indicating that both the consecutive trans and the orthorhombic bands respond to the temperature increase in the same direction. The negative (opposite) signs of ψ(ν1,ν2) indicate that the orthorhombic band at 1417 cm\(^{-1}\) decreases earlier than the consecutive trans bands originating from the rotator phase. These correlation results are consistent with the previous observation that the orthorhombic phase precedes the rotator phase. Next, for the amorphous bands at 1080 cm\(^{-1}\) and 1301 cm\(^{-1}\), the negative (opposite) values indicate that the amorphous state bands and the orthorhombic state band respond to the temperature increase in opposite directions. The positive (opposite) ψ(ν1,ν2) indicate that the amorphous bands increase occurs after the orthorhombic peak decrease. The 2DCOS analysis results can be summarized as:
(orthorhombic phase) → (rotator phase) → (amorphous phase), which is consistent with the known individual peak intensity analysis and the PCA results.

The 2DCOS analysis reconfirms the sequence of rise and fall of Raman bands associated with the multiple phases of \(n\)-C\(_{21}\)H\(_{44}\). However, performing 2DCOS over the whole temperature range from 30 °C to 42 °C cannot provide phase specific information of Raman bands. As an alternative, the MW-2DCOS partitions the spectra into small temperature windows and analyzes a series of the 2DCOS of the partitioned windows. The window size determines the temperature “resolution” of the analysis as well as the “signal-to-noise ratio” of the 2DCOS results. We find that the minimum window size of three temperature steps (\(\Delta T = 2 ^\circ C\)) still provides signal-to-noise ratio sufficient for the 2DCOS analysis. Figures 4a and 4b show two examples of the synchronous maps from the windows centering at 33 °C and 41 °C near the phase transition temperatures. The diagonal line is called the autocorrelation spectrum, which corresponds to the total intensity variation within the window range.\(^{[1,2]}\)

The moving-window autocorrelation spectra in Fig. 4c and 4d clearly show two distinctive phase transition temperatures, where intensity variation reaches local maxima. The moving-window autocorrelation plots also show which Raman bands are associated with a specific phase transition. The two distinctive transition temperatures of 33 °C and 41 °C correspond to the orthorhombic-to-rotator and rotator-to-amorphous transitions, respectively, as previously discussed in the individual peak analysis and the PCA. The two phase transition temperatures determined by MW-2DCOS are consistent with the previously reported values for \(n\)-C\(_{21}\)H\(_{44}\) by X-ray (32.55 °C and 40.55 °C), and differential scanning calorimetry (DSC) (30.84 °C and 40.01 °C).\(^{[21,22]}\) Interestingly, the autocorrelation intensity of the consecutive \(\Delta T = 2 ^\circ C\) still provides signal-to-noise ratio sufficient for the 2DCOS analysis. Figures 4a and 4b show two examples of the synchronous maps from the windows centering at 33 °C and 41 °C near the phase transition temperatures. The diagonal line is called the autocorrelation spectrum, which corresponds to the total intensity variation within the window range.\(^{[1,2]}\)

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metric that allows for comprehensible visualization of the phase transition. Our approach is to measure the correlation intensity of an identical region of both synchronous and asynchronous maps for all temperature windows. We set an isosceles right triangle because it is applicable to both synchronous and asynchronous maps, which are symmetrical and antisymmetrical across the diagonal line, respectively. The width of the triangle is set by the peak width determined from a synchronous map. The average values of synchronous and asynchronous correlation are plotted as a function of the average temperature ($T_{\text{ave}}$) of a temperature window in Figure 4.

### Figure 4.

Moving-window two-dimensional correlation spectroscopy (MW-2DCOS) analysis of the $n$-C$_{21}$H$_{44}$ Raman spectra with a temperature window size of three spectra ($\Delta T = 2$ °C). Examples of synchronous maps are presented for two selected average temperatures ($T_{\text{ave}}$) at (a) 33 °C and (b) 41 °C. (c) The autocorrelation or autopoint spectrum, corresponding to the diagonal line in a synchronous map, is plotted as a function of $T_{\text{ave}}$ of the moving window. (d) The identical data of (c) are re-plotted differently for determination of phase transitions over the whole range of Raman bands. The two phase transitions are indicated as the black dotted lines.
This new type of quantitative visualization from MW-2DCOS helps to determine the location of a phase transition, which corresponds to $T_{\text{ave}}$ for the maximum in spectral variation. The width of the peak indicates the sharpness of a phase transition. In Fig. 6g and 6h, the full-width-half-maximum (FWHM) is approximately 2 °C, which happens to be the width of the moving window for this analysis, indicating that the transition occurs within a temperature range equal to or narrower than 2 °C.

It needs to be noted that the non-zero asynchronous correlation, as shown in Fig. 6d, cannot be explained with a simple two state model where a spectrum is reduced into a linear combination of the unvarying spectra corresponding to the crystalline and amorphous states. We exclude the possibility of existence of a fourth phase because it is unlikely that there exists a new phase between the orthorhombic phase and the rotator phase and that it only exists between 33 °C and 34 °C. Previous X-ray and DSC studies also do not indicate any additional temporary phase between the orthorhombic and rotator phases. Therefore, we turn to the possibility of band shape changes in one or both of the phases. It is well known that band position shifts and line broadening can cause non-zero asynchronous correlation.[12] We examine the band position and linewidth of the 1295 cm$^{-1}$ band and the two other consecutive trans bands of 1062 cm$^{-1}$ and 1133 cm$^{-1}$ by fitting them with a single pseudo-Voigt function (a linear combination of one Gaussian and one Lorentzian function). We find that a pseudo-Voigt function can fit experimental data much better than a single Lorentzian or a single Gaussian function, shown in Fig. S1 (Supporting Information). From the fitting, we determined amplitude, band position, FWHM, and Lorentzian percentage of each band. We include the contribution of a broad amorphous band into the fitting and find that the results of the consecutive trans bands below 41 °C are not affected by the broad amorphous band. Figure 7 plots the band position and FWHM of the three peaks as a function of temperature. All three peaks exhibit changes in the temperature dependence of band position and width below and above the phase transition temperature at $\approx 33$ °C. In the orthorhombic phase ($T < 33$ °C), band position and width do not show a measurable temperature dependence. In contrast, in the rotator phase ($T > 33$ °C), it is clear that band position shifts and the width broadens with temperature. In addition, only in the rotator phase, Lorentzian percentage in the pseudo-Voigt function increases with temperature, shown in Fig. S2 (Supporting Information).
Previous studies based on peak intensity are focused on gradual decrease in consecutive trans contribution in the rotator phase with increasing temperature. Orendorff et al.\textsuperscript{23} analyzed the peak intensities, peak frequencies, and bandwidths of several Raman bands of octadecane and PE, but they assigned the intermediate state as a biphasic mixture where the (orthorhombic) crystalline phase and the (amorphous) liquid phase coexist. Our results of temperature-dependent peak position, width, and shape of the consecutive

![Figure 6](image-url)
trans Raman modes, in Fig. 7, clearly show qualitatively different temperature dependence of peak position and width between the orthorhombic and rotator phases. In particular, the kinks and the offsets at 33 °C in the peak position plot of Fig. 7a and 7c strongly suggest that the rotator phase provides the consecutive trans modes with a unique molecular environment that is qualitatively different from the orthorhombic phase. It is known that the unit cell of the rotator phase is hexagonal, which is different from the orthorhombic unit cell of the crystalline phase. It is interesting that the rotator phase exhibits a higher sensitivity to temperature in peak position and width compared to the orthorhombic phase. Orendorff et al.\[23\] ascribed the blue shift of the CH$_2$ twisting bands of octadecane at 1295 cm$^{-1}$ to a reduced coupling between alkane chains. Interestingly, in the same report, they correlated the bandwidth broadening of the same band with both an increase in rotational disorder and an increase in the number of gauche conformers. Their studies, though, were more focused on conformational differences between the crystalline and the amorphous phases. It remains unclear whether intermolecular chain interaction or intramolecular conformational order causes the unique temperature dependence of the consecutive trans bands in the rotator phase. However, it is clear that the molecular environment of the orthorhombic and the rotator phase are qualitatively different and that the trends of peak position, bandwidth, and Lorentzian percentage are monotonic with temperature in the rotator phase.

The temperature-dependent peak shifting and broadening explain the non-zero asynchronous correlation at the orthorhombic-to-rotator phase transition in Fig. 6. By using the empirical trend found by the peak fitting analysis, we construct and compare a few potential Raman band models to unravel the complex feature in the 2DCOS map in Fig. 6d. The first model assumes a single peak in the orthorhombic phase and an independent single peak in the rotator phase. In this model, the spectra at 32 °C and 34 °C are fit to single pseudo-Voigt profiles. The Raman spectrum at 33 °C is expressed as the linear combination of the peak function at 32 °C and the extrapolated peak function from the trend between 34 °C and 40 °C, and their relative amplitudes are determined by fitting with the experimental spectrum at 33 °C. The three spectra simulated from this “single orthorhombic peak” model, depicted in Fig. 8a, generate synchronous and asynchronous maps. The synchronous map from the simulated and experimental spectra looks similar in shape and intensity. However, the asynchronous map is quite different in both intensity and shape between the simulated and experimental results in Fig. 8c and 8i, respectively. Second, we calculated 2D correlation maps for a slightly modified model, which treats the intermediate rotator peak at 33 °C as a single

Figure 7. Peak fitting results of three selected consecutive trans bands in the temperature range corresponding to the orthorhombic and rotator phases. Peak position and FWHM determined from the fitting with a single pseudo-Voigt function are plotted as a function of temperature in the left and right columns, respectively. The error bars of ±0.018 cm$^{-1}$ in (a) and ±0.017 cm$^{-1}$ in (b) indicate the standard deviations of the peak position and FWHM fitted from three spectra, which were separately acquired at 28 °C. The red dashed lines are for guidance.
pseudo-Voigt function. The generated asynchronous map, shown in Fig. S3 (Supporting Information), is still far from the experimental results.

The third model assumes two overlapping peaks for the orthorhombic spectrum and a single peak for the rotator state. The motivation is that their subtle difference in two molecular configurations in the orthorhombic unit cell can cause splitting in consecutive trans Raman bands, as predicted by calculations.[25,26] In this "double orthorhombic peak" model, we fit the orthorhombic band with two peaks, as depicted in Fig. 8d. The rotator peak and the mixture peaks at the transition temperature are prepared in the same way as the first model. Figure 8e and 8f show the 2D correlation maps calculated based on the double orthorhombic peak model. The asynchronous maps from the simulated spectra and the experimental spectra are very similar in both shape and intensity. This similarity suggests that the CH₂ twisting band in the orthorhombic phase theoretical prediction[25,26] and experimental observation at different conditions.[9,11] It must be noted that the consists of resolved by this analysis is 1.4 cm⁻¹, which is extremely challenging for conventional spectral analysis methods to resolve from room-temperature Raman bands with a FWHM of two overlapping peaks, confirming the previous splitting (4 to 6) cm⁻¹. These results demonstrate that MW-2DCOS analysis can determine the orthorhombic-to-rotator phase transition temperature and unravel the overlapping peaks in the orthorhombic state. Figure 9 shows the CH₂ twisting Raman bands at the orthorhombic, rotator, and amorphous phases, accompanied by their schematic structures.

Figure 8. Two examples of Raman band models proposed to explain the 2D correlation maps observed at the orthorhombic-to-rotator transition. The single orthorhombic peak model (a – c) assumes a single peak in the orthorhombic phase while the double orthorhombic peak model (d – f) assumes two overlapping peaks in the orthorhombic phase. In both models, the Raman spectrum at 33 °C, the transition temperature, is assumed to be a mixture of the spectra corresponding to the orthorhombic (O) and the rotator (R) phases. Both synchronous and asynchronous maps calculated from the simulated Raman spectra for 32 °C to 34 °C are compared with the correlation maps obtained from experimental data (g – i). The 2D correlation maps are plotted on the same z scale for comparison: from 0 to 4.2 for the synchronous maps and from 0 to 0.2 for the asynchronous maps. The vertical dotted line at 1295.2 cm⁻¹ is for guidance.
**Figure 9.** Schematic of spectral evolution of the CH$_2$ twisting mode of $n$-C$_{12}$H$_{26}$ during melting. Two narrow overlapping peaks in the orthorhombic phase becomes a single peak in the rotator phase; then, it becomes broad and shifted to higher frequency in the amorphous phase.

**Conclusion**

We analyzed a series of variable temperature Raman spectra of $n$-C$_{12}$H$_{26}$ during melting from the orthorhombic phase to the rotator phase and to the amorphous phase. We found that MW-2DCOS can determine the orthorhombic-to-rotator and the rotator-to-amorphous transition temperatures with a higher resolving power than the commonly used, individual peak intensity analysis or the principal component analysis. Temperature- and phase-resolved spectral analysis on peak position, bandwidth, and Lorentzian percentage of several Raman bands shows that the intermediate rotator phase is not a simple biphasic mixture of the crystalline and amorphous phases but a unique phase that provides different spectral environment from the other two phases. By comparing with the 2DCOS of the model Raman spectra, we have learned that the CH$_2$ twisting band at 1295 cm$^{-1}$ consists of two overlapping peaks in the orthorhombic phase but becomes a single peak in the rotator phase, which had been only predicted but not observed because of thermal broadening near the melting temperature. This result demonstrates that MW-2DCOS can be used as a sensitive tool not only for determination of phase transitions but for unraveling subtle spectral features associated a specific molecular conformation.

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**References**


**Supporting information**

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