Quantum Capacitance-Limited MoS₂ Biosensors Enable Remote Label-Free Enzyme Measurements
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Abstract
We have demonstrated atomically thin, quantum capacitance-limited, field-effect transistors (FETs) that enable the detection of pH changes with 75-fold higher sensitivity (∼4.4 V/pH) over the Nernst value of 59 mV/pH at room temperature when used as a biosensor. The transistors, which are fabricated from monolayer films of MoS₂, use a room temperature ionic liquid (RTIL) in place of a conventional oxide gate dielectric and exhibit very low intrinsic noise resulting in a pH resolution of 92×10⁻⁶ at 10 Hz. This high device performance, which is a function of the structure of our device, is achieved by remotely connecting the gate to a pH sensing element allowing the FETs to be reused. Because pH measurements are fundamentally important in biotechnology, the increased resolution demonstrated here will benefit numerous applications ranging from pharmaceutical manufacturing to clinical diagnostics. As an example, we experimentally quantified the function of the kinase Cdk5, an enzyme implicated in Alzheimer’s disease, at concentrations that are 5-fold lower than physiological values, and with sufficient time-resolution to allow the estimation of both steady-state and kinetic parameters in a single experiment. The high sensitivity, increased resolution, and fast turnaround time of the measurements will allow the development of early diagnostic tools and novel therapeutics to detect and treat neurological conditions years before currently possible.

Keywords: Field-effect transistor (FET), Room temperature ionic liquid (RTIL), MoS₂, Biosensor, Super-Nernstian, pH, Enzyme activity, Enzyme kinetics.

Introduction
Rapid and sensitive pH measurements based on field-effect transistors (FETs) are used in diverse applications that include determining the effects of ocean acidification on marine ecology,¹ biomanufacturing,² and low cost DNA sequencers.³ However, drastic improvements in
sensitivity and the resolution of electronic pH transduction are needed to accelerate their widespread use in important biotechnology applications. One such example is the measurement of the function of enzymes, macromolecular catalysts that accelerate biochemical reactions and serve an integral role in ensuring normal cellular function,4 where small changes in the solution pH act as a reporter of their function.5,6 Disruptions in normal enzyme function are known to give rise to debilitating neurological conditions including Alzheimer’s and Parkinson’s disease,7 several cancers,8 and even chronic neuropathic pain.9 As part of normal cellular function, enzymes catalyze the phosphorylation of substrate proteins by the hydrolysis of adenosine triphosphate (ATP) and the transfer of a single phosphate group. This results in the release of one or more protons into solution, and thereby a small change in the pH. The change in pH typically varies by less than 0.005 units10,11 under physiological conditions (i.e., for normal living organisms) or an order than magnitude lower than the resolution demonstrated with state-of-the-art ion-sensitive field-effect transistors (ISFETs).3,12

Several techniques have been developed over the past century for more accurate measurements of solution pH. The Harned cell is the primary pH measurement standard,13 but it requires an elaborate setup and long equilibration times making it unusable in the measurement of small and fast pH changes. As a result, pH measurements used in biotechnology applications rely extensively on electrode measurements or spectrophotometric techniques. These approaches lack adequate sensitivity and resolution for accurate measurements of enzyme-mediated pH changes.14,15 Over the past several years, there have been numerous developments in pH sensing technology using solid-state devices that are potentially suitable for biological applications.3,12,16,17 Improved sensitivity and dynamic measurements have been demonstrated with ISFETs3 and more recently dual-gate silicon FETs.16 In the latter case, pH sensitivity was
shown to be approximately two-fold higher than the Nernst potential of $\approx 59 \text{ mV/pH}$ at room temperature.\textsuperscript{17} Notably, the resolution of ISFETs has been reliably demonstrated to be 0.05 pH units.\textsuperscript{3,12} The resolution for these devices could be lower if the device parameters are optimized\textsuperscript{18} or if the measurements are performed under a very narrow bandwidth.\textsuperscript{19} However, resolution that is adequate for enzyme measurements under physiological conditions are yet to be experimentally realized with silicon FETs. These limitations have required FET-based enzyme catalyzed phosphorylation assays to be performed at concentrations that are about two orders of magnitude higher than physiological values, precluding their use in diagnostic and therapeutic development applications.\textsuperscript{6,20,21}

Here, we show that FETs with an atomically thin semiconducting channel and gated with an ionic liquid (2D-ILFET) allow label-free measurements of enzyme activity and kinetics at or below physiological concentrations. The measurements were performed by using a pH sensing element that is connected electrically to the 2D-ILFET (Figure 1a). This configuration allowed measurements with both a high intrinsic gain\textsuperscript{16} (i.e., sensitivity) and signal-to-noise ratio (SNR) that exceeded comparable silicon devices by more than an two orders of magnitude.\textsuperscript{22} We show that the newly-developed 2D-ILFET measurements are a quantitative first step to enabling their use in drug discovery and diagnostic applications. The ability to perform measurements within current testing frameworks and without resorting to surface modification\textsuperscript{5,20,23} or hazardous radioactive labeling will enable rapid adoption of the method. Furthermore, the higher sensitivity of the technique will allow its use in applications beyond enzymatic measurements, for example in critically needed early detection of neurodegenerative conditions,\textsuperscript{24} and more broadly to the measurements of biomolecular interactions that are important in many applications in biophysics and biotechnology.\textsuperscript{3,25-27}
In order to optimize the use of ionic liquid-gated 2D-ILFETs in enzyme activity measurements, we first characterized their electrical performance, followed by sensitive pH measurements to validate the approach. The optimized configuration was then used to measure the activity and kinetics of the proline directed kinase Cdk5, an enzyme strongly implicated in several neurodegenerative conditions.

**Experimental**

**Device Fabrication and Characterization:** High-performance FETs were fabricated using a technique we recently developed. Briefly, large area and high quality monolayer MoS2 flakes were exfoliated from bulk crystal using a gold-mediated exfoliation method on to oxidized, heavily doped silicon substrates that also served as a global back-gate. The thickness of the films was verified using photoluminescence and Raman spectroscopy as shown in Figure S8. The SiO2 substrates with a thickness of 300 nm and 70 nm were used to study the device performance scaling. After the monolayer MoS2 flakes were located and inspected using an optical microscope, optical photolithography was used to pattern the source, drain, and gate electrodes followed by electron beam evaporation of metal Ti/Au (2 nm/100 nm) and lift-off in acetone. A second photolithography step was used to define the active channel area, followed by reactive ion etching to remove excess MoS2 outside the channel area. After a final resist cleaning, a small droplet of the DEME-TFSI IL† (727679; Sigma Aldrich, St. Louis, MO) was carefully applied onto each device using a micromanipulator and an optical microscope. The droplet was sized to cover the MoS2 monolayer and the gate electrodes, as seen in the optical image of the final device in Figure 1b. It is important to note that for good ionic liquid-gate coupling with the device’s channel, the area of the gate electrodes that is in contact with the ionic liquid was designed to be much larger than the combined area of the source, drain contacts, and MoS2 channel that are in contact.
with the ionic liquid. Gate leakage was verified by measuring the current across the ionic liquid upon application of a potential across two patterned gate electrodes. The measurement scheme for electrical characterization is shown Figure 1a.

**Effect of contact resistance on device the performance:** For the ionic liquid gated MoS\(_2\) FET biosensors presented here, the effects of poor contacts should be minimal since the devices are always operated in the inversion regime to achieve high gain. The high channel carrier density in this regime greatly diminishes the effect to the Schottky barrier at the contacts allowing carriers to be injected into the channel with little difficulty. However, future work using these devices will build upon the contact engineering that we have developed\(^{29}\) to further improve sensitivity and the signal-to-noise ratio (SNR).

**Effects of ionic liquid hysteresis:** Room temperature ionic liquids can introduce considerable hysteresis during bidirectional voltage sweeps of the biosensor. This effect is insignificant when measuring very small pH changes, for example during enzyme measurements, and is not a very large source of error. However, hysteresis can be more pronounced for large pH measurements. To mitigate this effect, we always operate the device by sweeping \(V_{BG}\) in one direction when the liquid gate is connected to the measured solution. This method of operation minimizes hysteresis and allows reproducible measurements over a wide pH range.

**Quantum Capacitance Model:** For a monolayer MoS\(_2\) FET under positive ionic liquid-gate bias, the relationship between gate voltage, \(V_{LG}\), and the channel charge carrier density, \(n_{ch}\), is given by,\(^{33,34}\)

\[
V_{LG} - V_{t,LG} - V_{FB} = \frac{E_g}{2q} - \frac{k_B T}{q} \ln \left[ \exp \left( \frac{n_{ch}}{\gamma_2 D k_B T} \right) - 1 \right] + \frac{q n_{ch}}{C_{LG}} \tag{1}
\]
where \( V_{t,\text{LG}} \) is device threshold voltage, \( V_{FB} \) is the flat band voltage, \( Eg \) is the material band gap, \( q \) is elementary charge, \( k_B \) is Boltzmann’s constant, \( T \) is the temperature in Kelvin, \( g_{2D} \) is the band edge density of states, and \( C_{LG} \) is the liquid-gate capacitance. For a fixed \( V_{LG} \), we calculated \( V_{t,\text{LG}} \) as a function of channel carrier density,

\[
V_{t,\text{LG}} = V_{LG} - V_{FB} - \left( \frac{E_g}{2q} - \frac{k_B T}{q} \ln \left[ \exp \left( \frac{n_{ch}}{g_{2D} k_B T} \right) - 1 \right] + \frac{q n_{ch}}{C_{LG}} \right)
\]  

(2)

The channel quantum capacitance \( C_Q \) is dependent on the density of charge carriers within the channel and is given by, \(^{33}\)

\[
C_Q \approx q^2 g_{2D} \left[ 1 + \frac{\exp \left( \frac{E_g}{2k_B T} \right)}{2 \cosh \left( \frac{V_{ch}}{k_B T} \right)} \right]^{-1}, 
\]

(3)

where

\[
V_{ch} = \frac{E_g}{2q} - \frac{k_B T}{q} \ln \left[ \exp \left( \frac{n_{ch}}{g_{2D} k_B T} \right) - 1 \right]
\]

(4)

Using Equations 1—4 we calculated \( V_{t,\text{LG}} \) and \( C_Q \) as a function of \( n_{ch} \). Since \( C_{TG} \) and \( C_Q \) are in series as seen from Figure 1e, we calculate \( C_{TG}(C_Q) = C_{LG} \times C_Q / (C_{LG} + C_Q) \), where \( C_{LG} \) is the ionic liquid-gate capacitance. Similarly, the back-gate capacitance, \( C_{BG} = C_{ox} \times C_Q / (C_{ox} + C_Q) \), where \( C_{ox} \) is the back-gate oxide capacitance. Moreover, since \( C_Q \gg C_{ox} \), \( C_{BG} \approx C_{ox} \sim \text{constant} \). Under these limits, the expression for \( \alpha \) is given by,

\[
\alpha = \frac{C_{TG}}{C_{BG}} \approx \frac{C_{LG} C_Q}{C_{ox} (C_{LG} + C_Q)}
\]

(5)
and is limited by $C_Q$. At large values of $n_{ch}$, $C_Q$ approaches its theoretical limit, $C_{Q,max}$, and $\alpha$ is constant. As $n_{ch}$ decreases, $C_Q$ decreases exponentially from $C_{Q,max}$ and we observe a corresponding reduction in $\alpha$. The results from the model were compared with experimentally measured values of $\alpha$, which were extracted by numerically estimating the derivative $dV_{BG}/dV_{LG}$ (Figure 1d and Figure S2; Supplementary Information).

**Time-Series Field-Effect Transistor Measurements and PID Control:** Time-series measurements were performed following the schematic in Figure 2a. The signal on the ionic liquid-gate ($V_{LG}$) was switched between an arbitrary function generator (HF2LI; Zurich Instruments, Zurich, Switzerland) or a pH microelectrode (MI-4156; Microelectrodes, Bedford, NH). An offset voltage, $V_o$ (GS200; Yokogawa Corporation, Tokyo, Japan), was then added to $V_{LG}$ using a summing amplifier (SR560; Stanford Research Systems Inc., Sunnyvale, CA). The FET was operated in a constant current mode using a PID controller that varied $V_{BG}$ in response to changes in $I_D$. The channel current was first amplified using a current preamplifier (DLPCA-200; FEMTO, Berlin, Germany) with a transimpedance gain of $10^6$ V/A. The amplified voltage was input to a digital PID controller (HF2LI; Zurich Instruments, Zurich, Switzerland), filtered using a 4-pole Bessel low pass filter (LPF) with a bandwidth of 5 kHz and then sampled at 25 kHz using a 14-bit analog to digital converter. The PID controller varied $V_{BG}$ in response to changes in $I_D$ with a bandwidth of 1 kHz ($K_P=496.1$, $K_I=9.242 \times 10^3$ s$^{-1}$ and $K_D=8.02$ µs). The PID output was used to drive the back-gate voltage ($V_{BG}$) between -10 V to +10V.
**Ionic Liquid-Gate C-V Measurements:** In order to verify the capacitance of the ionic liquid ($C_{LG}$), we utilized a LCR meter (E4980A; Agilent, Santa Clara, CA) to make 2-probe, AC capacitance measurements across the ionic liquid, measuring across a frequency range of 20 Hz to 2 MHz. Figure S3 (see *Methods*) shows representative results of these capacitive measurements, highlighting that at low frequency (where our devices typically operate for sensing) the capacitance constant and approximately 1 nF. As seen in the inset, we observe a negligible bias dependence of the capacitance at all measured frequencies. The capacitance exhibits a less than 1% change over a ± 0.5 V range at the lowest frequency (20 Hz). Due to the design of our devices, we do not have a constrained contact area of the ionic liquid on electrodes, therefore we utilized optical estimates of ≈100 µm × 100 µm as the area of metal plates that are in contact with the ionic liquid used in the capacitance measurement. This allowed us to estimate the specific gate capacitance to the liquid-gate to be ≈10.7 µF/cm$^2$ at low frequency range (20 Hz to 2 kHz), in good agreement with values published in the literature.$^{35}$

**Resolution of pH Measurements:** The pH resolution was established by using two approaches: i) from a measurement of the power spectral density (PSD) of noise in $V_{BG}$ and ii) from the uncertainty in time-series measurements in constant current mode.

i) **Power Spectral Density Method:** The PSD of $V_{BG}$ was measured as shown in Figure S4. The broadband root mean squared (RMS) noise under PID control was then obtained using the expression $\delta V_{BG} = \sqrt{\int_{BW} S_{V_{BG}} df}$, where $S_{V_{BG}}$ is the noise density, $df$ is the frequency bin and $BW$ is the low-pass filter bandwidth. Using common conventions in signal processing and in the literature,$^{19,36}$ we defined minimum detectable value of $V_{BG}$ to be that at a SNR of 3 (or ≈10 dB). This allowed the determination of the pH resolution, represented throughout the
manuscript by $\delta p H_{PSD}$, using the expression, $\delta p H_{PSD}=3 \times \delta V_{BG}/(\alpha V_{Nernst})$, where $V_{Nernst}=59.5$ mV/pH is the Nernst voltage at room temperature.

ii) **Time-Series Uncertainty:** The pH resolution measured from the uncertainty of time-series measurements is represented by $\delta p H$. The uncertainty in $V_{BG}$ in constant current mode was obtained by first computing the histogram of the time-series at varying values of pH. Each resulting histogram was fit to a normal distribution with mean, $\mu_{VBG}$ and standard deviation, $\sigma_{VBG}$. The uncertainty in $V_{BG}$ is reported with an expanded uncertainty, $k=2$. This allows the pH resolution to be computed using the expression $\delta p H=k \sigma_{VBG}/(\alpha V_{Nernst})$.

**Kinase Measurement Reagents:** Static activity measurements of Cdk5/p25 phosphorylation of histone H1 were performed by suspending 100 ng of the enzyme (C0745; Sigma Aldrich, MO) in 50 $\mu$L of 1× kinase buffer to obtain a final concentration of 18.5 nM. The Cdk5/p25 concentration was reduced five-fold for dynamic measurements to obtain a final concentration of 3.7 nM. A stock solution of 5× kinase buffer was prepared by suspending 25 mM $\beta$-glycerol (G9422; Sigma Aldrich, MO), 50 mM MgCl$_2$ (5980; Millipore, MA), 5 mM EGTA (E0396; Sigma Aldrich, MO), 2.4 mM EDTA (1002264786; Sigma Aldrich, MO), 1.25 mM MOPS (M1254; Sigma Aldrich, MO) in deionized water (DIW) and diluting further to form 1× kinase buffer. Solutions of the substrate protein were prepared by adding 2 mg/mL of histone H1 (10223549001; Sigma Aldrich, MO) to the assay to obtain the final concentrations as described in the main text. The phosphorylation reaction was triggered with a cocktail of DTT and ATP. The final concentration of the ATP and DTT solution was adjusted to 250 $\mu$M and 5 mM in DIW respectively.

**Cdk5 $\gamma$-$^{32}$P-ATP Measurements:** Cdk5/p25 (C0745; Sigma Aldrich, MO) kinase activity was measured as described in the manufacturer’s protocol with some modifications. The kinase
reaction was initiated by adding $\gamma^{32}\text{P-ATP}$ (final concentration of 50 µM) to a preincubated substrate buffer cocktail and incubated at 30 °C for 1 hour. The reaction was terminated by spotting 20 µl of the reaction mixture on a P81 phosphocellulose pad. Dried pads were washed 3 times in 75 mM phosphoric acid, followed by rinsing with 95% ethanol. The radioactivity of the spotted pads was measured in a liquid scintillation counter. Appropriate controls, without added phosphoryl acceptor substrates, were also run and the values were subtracted from the total counts obtained in the presence of substrate protein.

Results and Discussion

Ionic Liquid-Gate 2D FET Performance. Initial characterization of 2D-ILFETs fabricated with monolayer MoS$_2$\textsuperscript{37} was performed with the set up in Figure 1a and using a representative device seen in Figure 1b (see Methods for fabrication details) where the sensing signal was connected to the top ionic liquid gate, while the silicon substrate was used as the measurement gate. The devices described in this work are fundamentally different from dual-gate silicon FETs\textsuperscript{16,38} in that the asymmetric, capacitively coupled, gates in the 2D-ILFET control the same atomically thin semiconducting channel giving rise to a large intrinsic gain in conjunction with ultralow noise performance. Furthermore, the measurement setup allowed the 2D-ILFET performance to approach the intrinsic quantum capacitance limit of the channel material.

The transfer characteristics of the device were measured by recording the drain current ($I_D$) as a function of the liquid-gate potential ($V_{LG}$) with the drain voltage ($V_D$) was held constant. The measurements were repeated for different back-gate voltages ($V_{BG}$) to determine the signal amplification ($\alpha$) due to the asymmetric capacitance of the ionic and back gates (Figure 1c). The
devices exhibited a dynamic range of \( \approx 5 \) orders of magnitude in \( I_D \) and a subthreshold slope between 69 mV/dec and 145 mV/dec at \( \approx 300 \) K.

For each curve in Figure 1c, the liquid-gate threshold voltage \( (V_{t, LG}) \) was determined from a linear extrapolation of the peak transconductance to the x-axis.\(^{39} \) The value of \( \alpha = \frac{dV_{BG}}{dV_{t, LG}} \) for representative devices was then determined numerically from the data in Figure 1d \((d=300 \text{ nm})\) and Figure S2 \((d=70 \text{ nm}; \text{ see } \text{Supplementary Information})\), where \( d \) is the thickness of the back-gate dielectric. From Figure 1d we can clearly discern two distinct regimes for \( V_{BG} \) as a function of \( V_{t, LG} \). At large and positive \( V_{BG} \) (Figure 1d; pink), where the device was in the limit of large 2D channel carrier density \( (n_{ch}) \), \( \alpha \) was constant and found to be \( 156 \pm 3 \) \((d=300 \text{ nm})\) and \( 41 \pm 4 \) \((d=70 \text{ nm})\). On the other hand, at negative \( V_{BG} \) and low \( n_{ch} \) (Figure 1d; blue), \( \alpha \) decreased exponentially. Both regimes of operation are explained by the quantum capacitance model discussed next. The error bars report the standard error defined as the standard deviation of the population mean.

**Quantum Capacitance-Limited Performance.** For devices with two gates, \( \alpha \) can also be determined from the ratio of the top \( (C_{TG}) \) and bottom gate \( (C_{BG}) \) interface capacitances, i.e., \( \alpha \approx \frac{C_{TG}}{C_{BG}} \) (see Supplementary Information for a detailed derivation).\(^{16,31,40} \) For dual-gate FETs where the individual gate oxide capacitances are considerably lower than those associated with the channel, \( \alpha \) is constant and can be calculated directly from the properties of the gate dielectric.\(^{35} \) However, due to the large capacitances associated with ionic liquids, for the devices reported here \( C_{TG} \) is limited by the intrinsic quantum capacitance \( (C_Q) \) of the 2D semiconducting channel. Importantly, \( C_Q \) approaches its theoretical limit, \( C_{Q,max} \) when \( n_{ch} \) is large.\(^{33} \) Under these conditions \( \alpha \) is constant. On the other hand, when \( n_{ch} \) is reduced, \( C_Q \) and therefore \( \alpha \) decrease.
exponentially (see Methods for a detailed explanation). This transition between the linear and exponential regimes can be observed in terms of the gate voltage in Figure 1d and $\alpha$ in Figure 1f.

Figure 1: Electrical characterization of ionic liquid-gate field-effect transistors (FETs). Error bars report standard errors defined as the standard deviation of the population mean. (a) Device schematic of an ionic liquid-gated FET for biosensing. A semiconducting channel formed between the source (S) and drain (D) terminals is controlled electrostatically by a voltage applied to the silicon substrate (B) or the ionic liquid top-gate (G). A voltage applied to the ionic liquid-gate ($V_{LG}$) can be switched between a voltage source for characterization or a biosensing element. The biosensing element used in this work is a glass pH microelectrode connected remotely to the gate contact. (b) An array of ionic liquid dual-gate FETs fabricated using a 2D MoS$_2$ film on a 300 nm SiO$_2$ substrate. The scale bar represents 100 µm. (c) Transfer characteristics show the drain current ($I_D$) as a function of $V_{LG}$ and varying back-gate voltage ($V_{BG}$). (d) The change in $V_{BG}$ as a function of liquid-gate threshold voltage ($V_{t,LG}$). A flat band voltage ($V_{FB}$) of -0.82 V was subtracted from $V_{t,LG}$ to enable comparison with theory. (e) The dual-gated FET was modeled with three capacitors in series. The quantum capacitance ($C_Q$) of the 2D channel controls the capacitive coupling between the back ($IF_B$) and liquid ($IF_L$) gate interfaces. (f) A plot of $\alpha$ as a function of $V_{t,LG}$ for two devices with back-gate oxide thickness of 300 nm (○) and 70 nm (□). The solid line shows the theoretical model for quantum capacitance limited device performance. $V_{FB} = -0.82$ V (d=300 nm) and $V_{FB} = +0.12$ V (d=70 nm) were subtracted from $V_{t,LG}$ to allow direct comparison between devices.

We see quantitative agreement between the model and measurements for two representative device structures shown in Figure 1f. In both cases, we assumed $C_{ox} = 0.0115$ μF/cm$^2$ (d=300 nm).
and 0.049 µF/cm² ($d=70$ nm), and $C_{LG}=10.7$ µF/cm² based on our own measurements (Figure S3; see Supplementary Information) and literature values. $C_{Q,max}$ was directly calculated from Equation 5 (see Methods) to be 2.16 µF/cm², and was in excellent agreement with the value of 2.2±0.05 µF/cm² extracted from a non-linear regression of the model to the data in Figure 1f. The only other free parameter in the model was the flat band voltage ($V_{FB}$), which depends in part on the fabrication process. The extracted value of $C_{Q,max}$ was within ≈45 % of the maximum theoretical value for monolayer MoS₂, and more than two times higher than previous measurements. This in turn allowed the devices to operate with high sensitivity when used for enzyme measurements. Furthermore, the ability to tune $\alpha$ with only the gate voltage is advantageous in biosensing applications to allow sensitivity to be offset for higher dynamic range.

Figure 2: Constant current mode electrical characterization of dual-gated ionic liquid-gated field-effect transistors (FET). (a) The FETs were operated in a constant current mode using a proportional-integral-derivative (PID) controller. $I_D$ was held constant by continually adjusting $V_{BG}$ in response to small changes to $V_{LG}$. (b) The response of $V_{BG}$, under PID control, as a function of time is shown upon application of a 1 Hz AC sine wave signal with varying amplitude to the ionic liquid-gate. Data are shown for a back-gate oxide thickness, $d=300$ nm. (c) The amplification at the back-gate ($\alpha$) increased with the applied liquid-gate offset voltage, $V_o$, allowing the device gain to be smoothly tunable. The error bars report the standard error defined as the standard deviation of the population mean. (d) The signal-to-noise ratio (SNR) was extracted with a bandwidth of 5 kHz as a function of AC signal amplitude for devices operated under PID control and in open loop (●). For devices fabricated with either a 300 nm ($\alpha=13$; ●) and
\( \alpha = 42; \) and 70 nm (\( \alpha = 5; \)) or 70 nm (\( \alpha = 50; \)) SiO\(_2\) back-gate dielectric, the SNR under PID control was higher than under open loop operation. The pH resolution (\( \delta pH \)) as a function of the measurement bandwidth and \( \alpha \) for devices with a 70 nm (\( \alpha = 5; \)) and 50\% SiO\(_2\) back-gate dielectric.

**Constant Current Operation for Biosensing.** The preceding results were used to maximize \( \alpha \) when operating the ionic liquid FETs in a constant current mode using a proportional-integral-derivative (PID) controller as shown in Figure 2a. The PID controller varied \( V_{BG} \) in response to \( V_{LG} \) to maintain a root mean square (RMS) channel current of 100 nA. PID performance was then compared with open loop operation where \( I_D \) was recorded in response to changes in \( V_{LG} \). The signal connected to the ionic liquid-gate was setup to allow switching between an arbitrary waveform generator to calibrate sensor performance or a biosensing element. In both cases, a fixed DC offset voltage (\( V_o \)) was added to \( V_{LG} \) to set the value of \( \alpha \) (see Methods).

**Device Sensitivity.** Device calibration was performed with a 1 Hz sine wave applied to the ionic liquid-gate. Figure 2b shows the change in \( V_{BG} \) (\( d = 300 \text{ nm} \)) under PID control with \( V_o = -0.56 \text{ V} \) for sine wave amplitudes of \( V_{LG} \) ranging from 0.7 to 5.7 mV\(_{\text{rms}}\), which resulted in \( \alpha = 28 \). Tuning \( V_o \) allowed sensitivity to be smoothly offset for dynamic range with the highest \( \alpha \) realized when operating near the linear regime determined from Figure 1d. Using this approach, we tuned \( \alpha \) smoothly from 5\( \pm 0.4 \) to 28\( \pm 1.8 \) (Figure 2c) when \( d = 300 \text{ nm} \) or from 5\( \pm 0.5 \) to 50\( \pm 1.5 \) when \( d = 70 \text{ nm} \). Moreover, the measured values of \( \alpha \) were consistent with those in Figure 1f, and more than an order of magnitude higher than dual-gate silicon FET measurements.\(^{16}\)

**Signal-to-Noise Ratio and Resolution.** The signal-to-noise ratio (SNR) is a true measure of sensor performance. To determine if the higher sensitivity of our FETs, relative to dual-gate silicon devices,\(^{16}\) translated to an improved resolution, we measured the noise in \( V_{BG} \) and \( I_D \) of the 2D-ILFET devices as shown in Figure S4. These measurements were then used to determine the SNR of the FET in PID and open loop modes. Figure S4 shows a representative power...
spectral density (PSD) of the back-gate voltage (top) under PID control ($d=300$ nm) and channel current (bottom) during open loop operation. The broadband noise under PID control was obtained using the expression $\delta V_{BG} = \sqrt{\int_{f_{BW}} S_{V_{BG}} df}$, from DC to the low pass filter bandwidth of 5 kHz and found to be 5.0 mV_{rms} ($d=300$ nm; Figure S4 top) and 0.45 mV_{rms} ($d=70$ nm; Figure S4 middle) for the measured devices, decreasing as expected with the back-gate oxide thickness. Furthermore, $\delta V_{BG}$ was found to be invariant with $V_o$, and thereby $\alpha$, over the measured range of biasing conditions. The channel current noise in the open loop case, $\delta I_d = \sqrt{\int_{f_{BW}} S_{I_d} df}$ was 700 pA_{rms} (Figure S4 bottom). The SNR was determined using the expressions $20 \log_{10}(V_{BG}/\delta V_{BG})$ under PID control and $20 \log_{10}(I_d/\delta I_d)$ in open loop mode and shown in Figure 2d as a function of $V_{LG}$. For a bandwidth of 5 kHz, SNR was found to increase $\approx$3-fold ($\alpha=13$, $d=300$ nm) to $\approx$30-fold ($\alpha=50$, $d=70$ nm) under PID control when compared to open loop operation.

The device structures described here are fundamentally different from silicon-based dual-gated FETs described in previous studies. In those devices, it was interpreted that two channels were formed and controlled independently by the top and bottom gates. In constant current mode, when the device was operated in the inversion-inversion regime, changes in the gate potential at one interface that drive the corresponding channel into strong inversion (increasing channel current), cause the other channel to be placed into weak inversion (with increasing channel noise). Regardless of the polarity of the applied potential at the sensing gate, the overall channel current noise is dominated by the channel in weak inversion. Channel noise could further limit SNR when the devices are operated in the inversion-depletion regime, for example as demonstrated with ultra-thin body double-gated silicon FETs. In this case, the noise
is dominated by the depleted channel and should result in lower performance compared to the inversion-inversion regime. Furthermore, this effect becomes more pronounced with increasing gain. As a result, extensive work with such devices has shown no measurable improvement in SNR of silicon devices despite large improvements in the sensitivity.\textsuperscript{38} In contrast, ultra-thin channels formed with 2D materials have a single conducting channel controlled by both the top ionic liquid-gate and bottom SiO\textsubscript{2} back-gate. Because the channel can always be placed in the inversion regime, the relative noise is low over a wide range of biasing conditions leading to improved SNR with these devices.

The pH resolution, $\delta \rho_{P_{PSD}}$ (as defined in the Methods) was obtained from the PSD of $V_{BG}$ at a temperature of 300 K. At a bandwidth of 5 kHz, the minimum detectable $V_{BG}$ was 3.8 mV ($\alpha=50$, $d=70$ nm) resulting in a $\delta \rho_{P_{PSD}}=0.0013$ pH units for these conditions. Since the measurements of the kinetics of biomolecules are relatively slow, resolution can be further improved at lower bandwidth. This is possible because applying a low-pass filter to the data reduces noise at frequencies outside the desired signal bandwidth, thereby increasing the SNR.\textsuperscript{43} When the signal was measured with a bandwidth of 10 Hz (Figure 2e; $\alpha=50$, $d=70$ nm), we extracted a $\delta \rho_{P_{PSD}}=92\times10^{-6}$ pH units, representing a greater than 10-fold improvement over state-of-the-art ISFET measurements.\textsuperscript{1,12,18,19} Importantly, in contrast to measurements made with dual-gate Si FETs, the resolution improved with increasing $\alpha$ as discussed above.

**Sensitive pH Measurements.** The ionic liquid-gate FETs were used to remotely measure the pH of buffered solution with high sensitivity. In this measurement, $I_D$ was measured as a function of $V_{BG}$ with a pH sensor measuring standard buffer solutions was connected to the liquid-gate as seen in Figure 3a. The change in the back-gate threshold voltage, $V_{t,BG}$ for each measured pH from 4 to 10 is apparent from the data in Figure 3b and was found to be linear (Figure 3c) as a
function of pH. The measurement sensitivity was \( \approx 4.4 \text{ V/pH} \) or 75\( \times \) higher than the Nernst limit of 59 mV/pH at room temperature\(^{17} \) (Figure 3c) and is a function of the device’s intrinsic \( \alpha \).

![Figure 3: Ionic liquid-gate field-effect transistor (FET) calibration with buffered pH solutions. (a) Measurements of pH were performed by connecting the ionic liquid-gate (G) to a pH sensing element. The dashed line shows the connection to the FET. (b) The change in the back-gate threshold voltage \( (\Delta V_{BG}) \) as a function of the solution pH showed a linear response over the measured range. When using a 300 nm SiO\(_2\) back-gate, the pH sensitivity was found to be 4.4 V/pH (C). (c) pH sensitivity of buffered electrolyte solutions was extracted from the shift in \( \Delta V_{BG} \). Measurements were performed over a wide range of solution pH from 4.01 to 10.01. (d) Time-series measurements of \( V_{BG} \) response to buffered pH solutions were measured in constant current mode with a bandwidth, \( B=10 \text{ Hz} \), and when the device gain, \( \alpha=33 \). The panel on the right shows the histogram of \( V_{BG} \) for data points between the gray dashed lines. (e) The back-gate voltage \( (V_{BG}) \) response to varying pH buffer solutions, resulted in a sensitivity of 2.1 V/pH. The error bars represent the uncertainty in the measurement, obtained from the widths of the histogram in panel d. (d) The measurement signal to noise ratio (SNR) was measured at a bandwidth of 10 Hz and found to average 75 dB (\( \approx 5600 \)). SNR was lowest in the vicinity of neutral pH (\( \approx 7 \)) where \( V_{LG} \) was very small.]

The solution pH was also measured in a constant current mode using PID control by setting \( \alpha=33 \ (V_0=-1.5 \text{ V}, \ d=300 \text{ nm}) \). Figure 3d shows time-series measurements of phosphate buffered saline (PBS) solution at a bandwidth of 10 Hz. A switch was used to alternatively connect the ionic liquid-gate to the PBS solution and to ground. A histogram of the time-series was then used
to determine the uncertainty in the measurement and the pH resolution, $\delta pH$, as discussed further below. Figure 3e plots the change in $V_{BG}$ with solution pH. Measurements were made relative to pH 7 ($V_{LG}$=0 V); acidic pH resulted in $V_{LG}>0$ V and basic pH in $V_{LG}<0$ V. A linear least-squares fit to the data returned a slope of 2.1 V/pH when $\alpha=33$. Similar to measurements in Figure 2, sensitivity can be tuned by varying $V_o$ to alter $\alpha$. For example, when $\alpha=23$ we obtained 1.2 V/pH, which could allow measurements over a larger range (data not shown). The maximum value of $\alpha$ obtained in the constant current mode was constrained by our control electronics, which can only source a maximum voltage of $\pm 10$V to control the back-gate voltage. This precluded measurements at the maximum value of $\alpha=159$ for this device as seen from the static pH measurements in Figure 3c.

The pH resolution was also measured from the uncertainty in the time-series measurements (see Methods for a description) in Figure 3d. The mean uncertainty from the Figure, $\sigma_{VBG}$ was found to be 300 $\mu$V. This value then resulted in $\delta pH \approx 300 \times 10^{-6}$ pH units ($\alpha=33$), which was found to be consistent with the resolution obtained from noise measurements. Furthermore, since SNR, and thereby resolution, improves with increasing $\alpha$ as seen from Figure 2d, the best possible resolution of the device at the maximum gain ($\alpha=156$) is predicted to be $\approx 70 \times 10^{-6}$ pH units. This is consistent with the experimentally measured value of $92 \times 10^{-6}$ pH units discussed above from an analysis of the noise floor (SNR 3; $\approx 10$ dB) for a bandwidth of 10 Hz.$^{19}$

**Enzyme Activity and Kinetics.** Protein kinases are an important subset of enzymes that facilitate post translational modifications, such as the phosphorylation of substrate proteins, to influence signaling pathways in the cell cycle and achieve homeostasis.$^{4,44}$ The deregulation of protein kinases is believed to underlie the onset of neurological conditions such as Alzheimer’s disease or Parkinson’s disease.$^{45,46}$ Therefore, the functional quantification of enzyme activity is
central to the development of therapeutics that restore physiological function. Existing methods
to measure enzyme activity, for example during protein phosphorylation, rely on radioactively
labeled adenosine triphosphate (ATP) analogs or fluorophores. Such techniques are expensive
because they need specialized molecule labeling and handling, require hours to yield results, and
often alter the kinase activity, thus limiting their effectiveness in rapid therapeutic screening.

We applied our ultra-sensitive FETs to measure the activity and kinetics of the proline-
directed kinase Cdk5. Under normal physiological conditions, Cdk5 is tightly regulated by either
the p35 or p39 inhibitory proteins. Oxidative stress causes a 10 kDa membrane anchored
fragment of p35 to be cleaved, forming the pathological activator p25, resulting in deregulation
and delocalization of the complex to the cytosol. The resulting pathological complex,
Cdk5/p25, has higher activity than its physiological counterpart, Cdk5/p35, and participates in
the indiscriminate phosphorylation of numerous proteins, which are known to result in
neurofibrillary tangles that are a hallmark symptom of Alzheimer’s disease.

The multi-protein pathological complex, Cdk5/p25, participates in the phosphorylation
reaction shown in Figure 4a. Cdk5 mediated phosphorylation results in the release of a proton
during ATP hydrolysis and the transfer of a single phosphate group to either a serine or threonine
residue immediately preceding a proline. Here, we demonstrate the ability of ionic liquid-gated
FETs to detect small changes in the solution pH during phosphorylation of the substrate protein,
histone H1 (see Methods for reagent conditions).

**Enzyme Activity.** Figure 4b shows the change in $V_{t,BG}$ as a function of histone H1
concentration under steady-state conditions. In each case, $V_{t,BG}$ was obtained from an $I_D-V_{BG}$ plot
shown in Figure S6 (see Supplementary Information). To account for instrument drift, each data
point in the figure was measured differentially with a control sample that was identical to the
measured vials except for the absence of ATP, thereby inhibiting the phosphorylation reaction. The kinase activity was then obtained using, $s = \gamma \frac{[H1]}{k+[H1]}$, where $k$ is the activity coefficient, $[H1]$ is the concentration of histone H1 and $\gamma$ is a scaling constant. For the FET measurements in Figure 4b, we obtained $k=17.5 \pm 1.3 \mu$M from a non-linear regression of the model to the measured data, consistent with previously published activity measurements for the pathological Cdk5/p25 complex.\(^\text{10}\) We compared the measurements in Figure 4b against enzyme activity measurements obtained from a radioactively labeled $\gamma^{-32}$P-ATP assay (see Methods) as seen in Figure 4c.\(^\text{53}\) The value of $k=12.1 \pm 2.3 \mu$M from those measurements was found to be statistically consistent with the FET measurements with 95% confidence.

Figure 4: Ionic liquid-gate field-effect transistors (FET) were used for label-free enzyme activity and kinetics measurements. (a) The proline directed kinase Cdk5 catalyzes the phosphorylation of substrate proteins (e.g., histone H1) in the presence of an activator (e.g., p25) and adenosine triphosphate (ATP). The hydrolysis of ATP results in the transfer of a single phosphate group to either a serine (Ser) or threonine (Thr) residue in the substrate protein and the release of a proton into solution, resulting in a change in solution pH. (b) Ionic liquid-gate FETs ($\alpha=159$) were used to measure the change in solution pH as a function of the histone H1 concentration ([H1]), and thereby infer the activity of Cdk5 under steady-state conditions. (c) The FET measurements were in quantitative agreement with a complementary assay that used radioactively labeled $\gamma^{-32}$P-ATP as a reporter of Cdk5 activity. (d) Time-series measurements of enzyme catalyzed phosphorylation as a function of [H1] (9.1 $\mu$M, ▲; 12.7 $\mu$M, □; 18.2 $\mu$M, ○) are shown and allow the direct estimation of the reaction dynamics. The solid lines depict the
reaction kinetics model that describes the time course of phosphorylation, while the dashed lines represent the reaction velocity during the first 100 s after a change in the signal was detected.

The change in the solution pH for the FET measurements was extracted from $\Delta V_{t, BG}$ in Figure 4b ($\alpha=159$). The expected change in the solution pH was obtained using the expression \[ \frac{d[H^+]}{d pH} = -2.303 \frac{C_a K_a [H^+]}{(K_a + [H^+])^2}, \]
where $C_a$ is the buffer concentration, $K_a$ is the acid dissociation constant and $[H^+]$ is the proton concentration.$^{11,54}$ The change in pH was consistent with $\approx 3$ phosphorylation sites on the substrate protein, assuming an electrolyte solution buffered with $C_a=250$ µM 3-(N-morpholino)propanesulfonic acid (MOPS).

**Enzyme Kinetics.** The FET-based measurements have a response time that allows the direct estimation of reaction kinetics and velocities as seen from Figure 4d and Figure S6 (see Supplementary Information). The concentration of the Cdk5/p25 complex used in Figure 4d was 3.8 nM (5-fold lower than the quantity used in Figure 4b and c, and about 5-fold lower than the concentrations found in physiological conditions). A control sample without histone showed no change in the measured potential upon addition of ATP. From Figure 4d, we observed that upon addition of ATP there was a decrease in $V_{BG}$ after $\approx 2$ min. The polarity of $V_{BG}$ is consistent with the release of protons into solution, which results in an increase in $V_{LG}$. The initial reaction velocities were extracted from a linear regression of the data for the first 100 s after a change in $V_{BG}$ was detected and were found to increase monotonically with [H1]. Furthermore, the initial linear change in $V_{BG}$ is consistent with an enzyme-limited reaction.$^{55}$ Finally, the time-course of each reaction in Figure 4d was fit with a first order rate law of the form, \[ V_{BG} = \beta (1 - e^{-k_1 t}), \]
where $\beta$ is a scaling constant and $k_1$ is a rate constant. The rate constant was consistent with previously reported values$^{55,56}$ and found to be $k_1=0.18\pm0.02$ per min, independent of the histone
H1 concentration. FET-based measurements are in excellent quantitative agreement with existing
techniques as seen from Figure 4, while providing results in minutes.

Based on the measurements in Figure 4 and the value of $\delta pH$ determined experimentally from
Figure 3, the ultimate limit of detection (LOD) for Cdk5/p25 can be substantially lower than the
value of 3.8 nM demonstrated here. When tested under weak buffering conditions (Figure 4), the
change in the pH measured for the lowest concentration of histone H1 (9.1 $\mu$M) was found to be
0.02 pH units at 300 s. Decreasing the concentration of Cdk5/p25 will require a longer time for
the solution pH to reach a comparable value under an identical histone H1 concentration.
However, the increased pH resolution of the ionic liquid gated FETs of $92 \times 10^{-6}$ can allow the
concentration of Cdk5/p25 to be decreased by 100-fold to 38 pM and still detect enzyme activity
at 300 s. Under such conditions, we expect the change in pH to be $\approx 200 \times 10^{-6}$, which is above the
resolution of the sensors demonstrated in this work.

Conclusions
We have demonstrated that dual-gate FETs with atomically thin channels and ionic liquid top-
gates allow performance limited by the intrinsic quantum capacitance of the channel material,
providing a robust and sensitive biosensing platform. The nearly 100-fold improvement in pH
sensitivity above the Nernst value and order of magnitude improvement in the resolution over
state-of-the-art silicon ISFETs at a bandwidth of 10 Hz allowed the measurement of small
changes in solution pH during enzyme mediated phosphorylation under physiological conditions.
The method eliminates the need for specialized labeling and hazardous material handling and can
decrease the cost and complexity of assays appreciably. Another key advantage of the
measurements is that they are time-resolved, enabling the estimation of both enzyme activity and
kinetics in a single assay. Because signal transduction is performed remotely, the measurements
are compatible with standard microtiter plates, and therefore amenable for use in high throughput screening to allow rapid evaluation of pharmaceutical candidates for neurological diseases.

The high sensitivity and SNR allowed measurements with 5-fold lower enzyme concentrations than physiological values and over an order of magnitude below previous demonstrations using FET. Furthermore, the pH resolution of $92 \times 10^{-6}$ demonstrated in this study can result in a further improvement of the LOD of Cdk5/p25 to only 38 pM (or $\approx$500-fold lower than the physiological concentration). The vastly improved LOD can in turn enable new biomarker measurements in blood or cerebrospinal fluid to be developed for use at early stages of neurodegeneration where the changes to kinase activity are subtle and currently undetectable. Importantly, these measurements can allow testing several years before any observable decline in cognitive function, allowing early interventions to be developed. The extended gate configuration of the sensors permit remote measurements, which allow them to be adapted for use in cell and tissue culture assays, where an increase in kinase activity has been correlated with pH imbalances. Such measurements can allow assays that interrogate mechanistic behavior across multiple spatial scales – from test tube to cell culture experiments – to better quantify the origin of disease states.

Conflicts of Interest
The authors declare no conflicts of interest.

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Footnotes
$\dagger$Certain commercial equipment, instruments, or materials are identified in this paper in order to specify the experimental procedure adequately. Such identifications are not intended to imply
recommendation or endorsement by the National Institute of Standards and Technology, nor it is intended to imply that the materials or equipment identified are necessarily the best available for the purpose.

References
Atomically thin, quantum capacitance limited, field-effect transistors, enable measurements of biological enzymes implicated in Alzheimer’s disease with unprecedented resolution.
Quantum Capacitance-Limited MoS2 Biosensors Enable Remote Label-Free Enzyme Measurements

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Fig. S1: The coupling between the ionic liquid and back gates was estimated from the transfer characteristics of the device. (a) When the back gate oxide thickness, $d=300$ nm, $\alpha=\frac{V_{BG}}{V_{t,LG}}$ was estimated to be 159 from the back gate voltage, $V_{BG}$, and shift in the liquid gate threshold voltage, $V_{t,LG}$. (b) When $d=70$ nm, $\alpha$ was lower as expected and estimated to equal 40.
Fig. S2: The shift in the back gate voltage ($V_{BG}$) plotted against the liquid gate threshold voltage ($V_{t, LG}$) allowed the estimation of the gate coupling ratio ($\alpha$). The flatband voltage ($V_{FB}$) in both cases was assumed to be 0. (a) When the back gate oxide thickness ($d$) was 300 nm, the maximum value of $\alpha$ was estimated to be $215\pm3$. (b) The corresponding maximum value of $\alpha$ when $d=70$ nm was $40\pm4$. 
Fig. S3: AC impedance data for ionic liquid on gold electrodes. $V_{AC} = 10 \text{ mV}$, bias = 0 V. (inset) Capacitance with fixed frequency and measured with a variable voltage bias. We extracted the quantum capacitance value following a standard practice used previously when analyzing the performance of ionic liquid gated MoS$_2$ field effect transistor (Refs. 30 and 32 of the main text). Since, the quantum capacitance is an intrinsic property of MoS$_2$ and it depends on the carrier concentration within the channel, we are not aware of a way to directly measure its value outside of a field-effect-transistor (FET) structure, and in particular without coupling the channel to a gate dielectric to control the carrier density. Here, we performed a separate measurement of the capacitance of the room temperature ionic liquid used as the top gate dielectric. The measured ionic liquid gate capacitance value allowed us to extract the maximum quantum capacitance value of MoS$_2$ channel using model presented in the Method section. The extracted value compares favorably with both theory and previous experiment data confirming the approach of the method that we used in this paper.
Fig. S4: The power spectral density of $V_{BG}$ (300 nm SiO$_2$, top and 70 nm SiO$_2$ middle) under PID control and $I_D$ (300 nm SiO$_2$, bottom) under open loop operation were used to estimate the signal to noise ratio (SNR).
Fig. S5: The response of the sensor to standard pH buffers was estimated from the device transfer curves. The threshold voltage of the back oxide gate decreased when the solution pH measured with the ionic liquid gate became more acidic. The threshold voltage exhibited linear relationship with the solution pH over a wide range.
Fig. S6: Changes in the solution pH during enzyme catalyzed phosphorylation were used to estimate Cdk5 activity and dynamics. (a) Steady state measurements of the change in sensor $I_d$-$V_{BG}$ characteristics allowed the estimation of phosphorylation as a function of the substrate protein concentration. (b) The measurements were also performed dynamically by recording the current across the field effect transistor (FET) channel upon the initiation of the phosphorylation reaction with ATP for three concentrations of the substrate protein.
Detailed Derivation of the Relationship Between the Gate Capacitances and Voltages

The detailed derivation of the relationship between $C_{TG}/C_{BG}$ and $dV_{BG}/dV_{LG}$ follows a classical model developed by Lim et. al\textsuperscript{1} and later adapted by Jang et. al\textsuperscript{2-4} for the case of ion sensing SiFET and ionic liquid-gated MoS$_2$ FET. Fig. S3 depicts a simplified one-dimensional view of the active region of a dual-gated metal-oxide semiconductor field-effect transistor (MOSFET).

![Diagram of a dual-gated MOSFET](image)

In analogy to bulk MOSFET theory,\textsuperscript{5} we can write:

$$V_{TG} = \gamma_{ST} + V_{ot} + F_{t,MS} \quad (1)$$

and

$$V_{BG} = \gamma_{SB} + V_{ob} + F_{b,MS} \quad (2)$$

where $V_{TG}$ and $V_{BG}$ are the top and back gate voltages, $\gamma_{ST}$ and $\gamma_{SB}$ are the top and back surface potential at the semiconductor top and bottom oxide interfaces respectively, $V_{ot}$ and $V_{ob}$ are the potential drop across the top and back gate oxide, $F_{t,MS}$ and $F_{b,MS}$ are the differences in the metal and semiconductor work-functions.

Under normal operating conditions, the semiconductor is completely depleted. The potential drop across the semiconductor is then given by the expression:

$$\gamma_b = \gamma_{ST} - \gamma_{SB} = (E_{st} - qt_bN_a/(2e_s)) \times t_b \quad (3)$$
where $y_b$ is the potential drop across the semiconductor, $E_{st}$ is the electric field at the top-surface edge of the depletion region, and $N_a$ is the doping density of the semiconductor (assuming p-type for an n-channel MOSFET), $t_b$ is the thickness of the semiconductor, and $e_s$ is the semiconductor dielectric constant.

Using Gauss’s theorem for the top oxide semiconductor interface

$$V_{ot} = \frac{1}{C_{ot}} (e_s E_{st} - Q_{ct}) \quad (4)$$

Similarly, for the bottom oxide semiconductor interface

$$-V_{ob} = \frac{1}{C_{ob}} (e_s E_{st} - q N_a t_b - Q_{cb}) \quad (5)$$

where $C_{ot(b)}$ is the top(bottom) oxide capacitance, $Q_{ct(b)}$ is the inversion charge at the top(bottom) oxide/semiconductor interface. For simplicity, we did not take into account the fix charges and the interface states at the interfaces. Using equations 1, 3, and 4 we obtain:

$$V_{TG} = (1 + \frac{C_b}{C_{ot}}) y_{ST} - \frac{C_b}{C_{ot}} y_{SB} - (Q_b/2 + Q_{ct})/C_{ot} + F_{t,MS} \quad (6)$$

where $C_b = e_s / t_b$ is the depletion charge capacitance and $Q_b = - q N_a t_b$ is the depletion charge density. Similarly using equations 2, 3, and 5 we obtain:

$$V_{BG} = (1 + \frac{C_b}{C_{ob}}) y_{SB} - \frac{C_b}{C_{ob}} y_{ST} - (Q_b/2 + Q_{cb})/C_{ob} + F_{b,MS} \quad (7)$$

Equation 6 and 7 describe the coupling between the front and back gate potentials. When the back oxide/semiconductor interface is in the inversion or accumulation regime, the top gate threshold voltage is virtually independent of the back gate voltage.\(^1\)

On the other hand, when considering the case of depleted back oxide/semiconductor interface, the threshold condition of the top oxide/semiconductor interface is $y_{ST} = 2F_B$ where $F_B = (kT/q)*\ln(N_a/n_i)$ where $k$ is Boltzmann constant, $T$ is temperature and $n_i$ is the semiconductor intrinsic carrier density.

Using equations 6 and 7, the top gate threshold voltage depends on back gate voltage using the relationship:

$$V_{t,TG} = V_{t,TG,A} - C_b C_{ob} / (C_{ot}(C_b + C_{ob}))* (V_{BG} - V_{BG,A}) \quad (8)$$

where the constants $V_{t,TG,A} = (1 + C_b/C_{ot}) 2F_B - Q_b/2C_{ot} + F_{t,MS}$ and $V_{BG,A} = F_{b,MS} - C_b/C_{ob}*2F_B - Q_b/2C_{ob}$.

From equation 8, we have:
\[ D V_{l,TG} = - \frac{C_b C_{ob}}{(C_{ot}(C_b+C_{ob}))} * D V_{BG} \]  \hspace{1cm} (9)

In order to apply equation 9 to our ionic-liquid gated MoS\(_2\) FET, we need to modify the model slightly. For a monolayer MoS\(_2\), \(t_b\) is \(~0.7\)nm, which in turn causes \(C_b \gg C_{ob}\). Additionally, \(C_{ob} \approx C_{BG}\) and \(C_{ot}\) need to be replaced by \(C_{LG} = C_{ot} C_Q/(C_{ot} + C_Q)\) to take into account the effect of the quantum capacitance. Finally, equation 9 must be rewritten as:

\[ D V_{l,TG} = - \frac{C_{BG}}{C_{LG}} * D V_{BG} \quad \text{or} \quad D V_{BG} = - \frac{C_{LG}}{C_{BG}} * D V_{l,TG} \]  \hspace{1cm} (10)

The negative sign in equation 10 implies that increasing \(V_{BG}\) will decrease \(V_{l,TG}\) since it is easier to accumulate carriers in the channel at positive back gate voltages.
Fig. S8: (left) Photoluminescence (PL) spectra of monolayer and bilayer MoS₂. Monolayer MoS₂ (black), which was used to fabricate devices in this study, possess a direct bandgap and exhibit a high PL intensity and a peak at ≈1.8 eV. In contrast, bilayer MoS₂ (red), which has an indirect bandgap has a greatly reduced PL intensity. (right) Raman spectra of MoS₂ used in this study. The A₁g and E₂g peak frequencies of 404.1 cm⁻¹ and 385.0 cm⁻¹ were used to verify that the film was a monolayer (black). The peak shifts of bilayer (red) and bulk films (blue) exhibit a distinct shift in the Raman peaks. Adapted with permission from Guros et. al.⁶ Copyright 2019 American Chemical Society.
References: